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PREDICTION OF LIGHT AIRCRAFT HORIZONTAL TAIL ONSET FLOWS - A REVIEW AND ANALYSIS

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of the two computer program	ns (WASH and WAKE) ar	e then dev	eloped in detail	I. WASH calculates			
the location of wake-sheet streamlines behind the wing, and upwash and downwash angles ahead							
of and behind the wing, res	of and behind the wing, respectively. WAKE computes two-dimensional velocity profiles						
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NOMENCLATURE

- A_n constants used to represent the Γ distribution in the downwash section.
- a vector from a vortex filament to a point in space.
- wing span in downwash section or wake width in boundary layer section.
- C_n wing drag coefficient.
- C₁ wing lift coefficient.
- c wing chord.
- c_{λ} wing section drag coefficient.
- c_o wing section lift coefficient.
- ${\sf c_1}$ eddy viscosity parameter in boundary layer solution.
- D total drag.
- d cylinder diameter in boundary layer section.
- d profile drag per unit wing span.
- $f(\xi,\eta)$ function of ξ and η which will appear as the unknown in the transformed boundary layer equations.
- H turbulent boundary layer form factor.
- cylinder length in boundary layer section or perpendicular distance from the point of interest to vortex filament in downwash section.
- $\bar{\ell}$ vector having direction of infinitesimal vortex filament.
- streamwise index in boundary layer finite difference solution.
- m_ wing section lift curve slope.
- n normal index in boundary layer finite difference solution.
- q dynamic pressure.
- T unknown in finite difference boundary layer recursive relation.
- t wing thickness.

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NOMENCLATURE (Continued)

- U freestream velocity in boundary layer section.
- induced freestream velocity component in the downwash section or velocity component parallel to streamline direction in boundary layer section.
- V freestream velocity vector in downwash section.
- induced spanwise velocity vector in downwash section or normal velocity.
- W total velocity induced at a point by a vortex.
- w induced total velocity vector in general downwash section or induced vertical velocity component.
- freestream coordinate in downwash section or streamline coordinate in boundary layer section.
- y spanwise coordinate in the downwash section or normal coordinate in boundary layer section.
- z vertical coordinate in the downwash section.
- α angle of attack.
- Γ strength of the bound vortex at any wing section.
- e downwash angle in downwash section or eddy viscosity in boundary layer section.
- nondimensional wake width.
- n nondimensional normal coordinate in boundary layer section or normalized loss of wake dynamic pressure.
- Λ sweep angle.
- ξ nondimensional distance behind wing trailing edge.
- ρ density of air.
- τ turbulent shearing stress.
- ψ two-dimensional stream function.
- ~ subscript denoting freestream conditions.

INTRODUCTION

The primary function of an aircraft's horizontal tailplane is to balance the pitching moment which arises when the lift force developed by the wing is not applied through the airplane's center of gravity. Control of the airplane in the vertical plane is accomplished by varying this balancing moment so that the wing seeks a new equilibrium lift. The size of the horizontal tail thus determines the allowable c.g. travel as well as the lift coefficient which can be generated at any time. One does not gain a higher degree of control capability, however, without accepting at the same time a performance decrement resulting from the higher drag of the larger surface.

Since the advent of the airplane, designers have pondered the problem of positioning and sizing the horizontal tail to achieve both good aircraft performance and acceptable longitudinal stability and control. Their problem is compounded by the passage of the wing through the air ahead of tail. This produces (1) a downward inclination or downwash in the air approaching the tail, and, if the tail is directly in the wing wake, (2) a lower velocity at the tail due to the wing drag force. If the tail is sized assuming the onset flow to be freestream but is instead immersed in the wing wake. it will be unable to generate the expected trim moment. Thus, to maintain control capability one must either locate the tail such that it never encounters such momentum deficiencies or else increase its size proportional to the kinetic energy deficiency actually encountered. The latter course entails a performance penalty. Because of the non-linear response of the tailplane to onset flow angle, it is important to know the local flow direction everywhere in the tail region as well as those areas where momentum deficiencies exist. One would like to predict the wake location and the velocity deficit in the region of the horizontal tail to facilitate the process of positioning and sizing.

As part of its program to provide technical support to the light aircraft industry and to aeronautical education in general, the National Aeronautics and Space Administration funded the present study at North Carolina State University. This work seeks to provide rigorous, easy-to-use methods (which now means computer programs) to predict the downwash and velocity profiles in the vicinity of the horizontal tailplane as well as detailed descriptions of the methods used, their historical antecedents, and some worked out examples. The study is thus analogous to previous studies (Ref. 1,2,3,4) which treat riding and handling qualities, aircraft performance, and wing and body lift and drag in a similar fashion.

As will become evident from the literature review, the procedures for estimating downwash angle and wake position are better-defined than those for estimating wake velocity profiles. The downwash calculation is usually approached by replacing the wing with a series of horseshoe vortices representing both the wing lift and the vorticity shed by the wing. The downwash is a result of the interaction of the flow due to these horseshoe vortices with the freestream flow. It is most intense in a curved plane emanating from the trailing edge of the wing. The locus of this plane is usually obtained by integrating the local downwash angle from the wing trailing edge to some downstream point of interest. More rigor may be added to this method by permitting the trailing vortices to deflect both spanwise and vertically so that their paths become streamlines. These streamlines then define the wake centerline position. This approach permits both upwash ahead of the wing and downwash behind to be calculated with a greater degree of accuracy than does the more conventional straight vortex method. The downwash computer program presented in this report employs the deflected vortex approach.

Since the purpose of the present work is to provide a rigorous yet relatively simple method for determining the <u>onset flow in the immediate neighborhood of the horizontal tail</u>, it is not necessary to continue the calculation beyond this region to the point where the trailing vortices rollup into the familiar vortical flow patterns observed far downstream of the aircraft. While the method employed herein can treat the inviscid flow aspects of this region satisfactorily, other simpler methods are entirely adequate for developing the essential features of this "far field" problem; further, the method used here to determine the viscous dissipation present about the wake centerline is valid only in regions of quasi-planar flow, certainly not in vortical flow regions. For this reason also, no attempt should be made to extend the calculation downstream beyond the region of the horizontal tail.

The perceptive reader will note that no mention is made in the ensuing pages of the obvious contributions of the fuselage, both viscous and inviscid to the character of the flow field downstream of the wing. While the downwash method used does include a treatment of the effects of fuselage interference on the wing lift distribution, it does not include the effect of diminishing fuselage size as one moves aft on the downwash field nor the effects of the rapidly growing boundary layer on the aft fuselage. These were regarded as small perturbations whose determination would be excessively difficult given presently available analytical tools; for this reason they are not included. The user must therefore consider this fact in applying the results to new design situations.

Another contribution which has been neglected in the computation is the modification in the wing's downwash field due to the upwash field of the horizontal tail. Since the upwash angles are inherently smaller than the downwash angles and since the tail lift is generally less than 1/5 the wing lift, this contribution has been neglected.

The method used herein is based on the lifting line representation of the wing; it is therefore applicable only to situations where the wing is of moderate-to-high aspect ratio, unswept, and relatively lightly loaded (the fuselage does not cover a very significant portion of the wing area). Situations where these conditions are not satisfied will usually demand a much more complex lifting surface treatment.

Another consequence of the lifting line representation is that the induced field in the immediate neighborhood of the wing is distorted by the concentration of the wing's bound vortices along a single line instead of being distributed over the whole surface. Thus the downwash and upwash angles in this region may be excessive while at greater distances they will be indistinguishable from those obtained from a lifting surface representation. Since, the region of interest in light aircraft is located more than 1.5 wing chords downstream of the wing's trailing edge, a lifting line representation should be quite adequate.

The variation in flow velocity as one moves vertically across the wing plane of symmetry is usually approximated by empirical relations derived from experimental data given the wing section drag coefficient and the distance behind the wing trailing edge. A more exact approach solves the two-dimensional boundary layer equations, using a finite difference technique, for the wake flow and then applies this solution along various streamlines displaced spanwise as given by the wake position procedure above. The result is a quasi-three-dimensional solution. The starting conditions for the integration are the viscous velocity profiles on both upper and lower wing surfaces. This approach is used here to determine the vertical variation in flow magnitude.

The work presented here begins with a two-part review of the pertinent literature dealing with the determination of (1) downwash angles and wake sheet location, and (2) velocity profiles in the wing wake. General theory and discussion of results sections are then presented for both the downwash (WASH) program and the velocity profile (WAKE) program. User instructions, program listings, and sample outputs of both programs are given in the appendices.

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LITERATURE REVIEW

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DOWNWASH AND WAKE POSITION

In order to estimate the lift and drag forces experienced by an aircraft's horizontal tail, it is imperative that the magnitude and direction of the local onset flow be known. The disturbance produced by the wing is the major contributer to non-uniform horizontal tail onset flows. Dwinnell (Ref. 5) points out that a wing generating a lifting force must have a pressure differential from the lower to the upper surface with the higher pressure on the lower surface. At the wing tips the air tends to flow laterally from the lower to the upper surface in an attempt to remove this differential. This lateral or spanwise flow is from wing tip to wing root on top and from wing root to wing tip on the bottom (see total velocity vectors in Figure 1). The air immediately aft of the wing trailing edge is given a swirling motion due to the

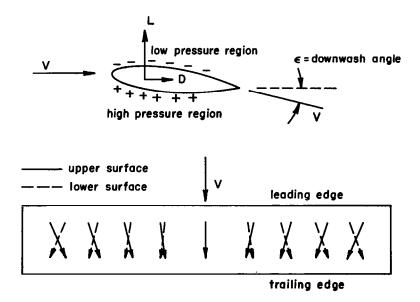


Figure 1. Side and planform views of flow over a wing (bound and trailing vortex patterns not shown in sketch).

shearing of the transverse velocity components on the upper and lower surfaces. These swirls or vortices, more predominant at the wing tips, are referred to as trailing vortices, and they tend to give the air behind the wing an average downward inclination, usually called downwash (see Figure 1 for definition of downwash angle). The spanwise variation of the downwash is a function of the wing planform shape.

The circulation theory developed in the late 1800's and early 1900's to account for lift in an inviscid fluid proved to be very useful in estimating downwash. In 1878 Lord Rayleigh showed that the swerving flight of a "cut" tennis ball could be explained best in general terms by comparing it to the case of a cylinder placed in an inviscid uniform stream. By imposing a circulatory flow upon the cylinder, the cylinder developed a force normal to the direction of the uniform stream (a lift force), directly proportional to the strength of the circulatory flow. In 1910 Joukowski showed that when a cylindrical body of arbitrary cross section moves with a velocity V in a fluid whose density is ho and there is a circulation of magnitude Γ around it, a force normal to the velocity is produced equal to the product $pV\Gamma$ per unit length of the cylinder. Joukowski made the assumption that the flow must leave the sharp trailing edge of airfoil-like bodies smoothly. Using this hypothesis, usually referred to as the Kutta-Joukowski condition because Kutta reached the same assumption independently somewhat earlier, the problem of lift became purely mathematical: one has only to determine the amount of circulation so that for zero vertex angle at the trailing edge, the velocity of the flow leaving the upper surface is equal to that leaving the lower surface. For finite vertex angles the trailing edge must be a stagnation point.

Although the work of Rayleigh and Joukowski was concerned with wings having infinite aspect ratios (no spanwise flow), the circulatory flow idea was extended to wings with large aspect ratios and little or no sweep by Prandtl in his now well-known Lifting-Line Theory. von Karman (Ref. 6) summarizes Prandtl's theory in the following way: (a) the wing is replaced by a lifting line perpendicular to the flight direction; (b) the lifting line is assumed to consist of a bound vortex with circulation variable in order to account for the fact that the lift may change along the span; (c) in accordance with the change in circulation along the span, free vortices are born and extend downstream; however, (d) the flow produced by the vortex system is considered as a small perturbation of the fundamental stream relative to the wing, and therefore (e) it is assumed that the free vortices approximately follow the original direction of the streamlines parallel and opposite to the flight direction; (f) the flow in the immediate neighborhood of a wing section is determined by the two-dimensional solution given by Kutta and Joukowski.

In the lifting line theory the wing surface is replaced by a line vortex of varying strength, called the bound vortex. A sheet of trailing vortices extends from the lifting line downstream to infinity: The perturbation in the flow field due to an infinitesimal segment of each vortex is found from the Biot-Savart Law (expressed here following Reference 7 in Vector notation).

$$\bar{w} = \frac{\Gamma}{4\pi} \frac{d\bar{k} \times \bar{a}}{|\bar{a}|^3} \tag{1}$$

where

w = induced velocity vector at a point in the flow field

 Γ_{-} = strength of the vortex whose segment is being considered

 $d\hat{l}$ = vector having the direction and length of the infinitesimal

vortex filament

a = the vector from the vortex filament to the point

the local value of Γ on the bound vortex is determined from

$$\Gamma(y) = \frac{\text{Vc } C_{\ell}(y)}{2} \qquad (2)$$

where

 \mathbf{C}_{ℓ} is the section lift coefficient of the wing \mathbf{V}^{ℓ} is the free stream velocity

c is the wing chord

The strength of a particular trailing vortex is determined by the change in the Γ of the bound vortex which occurred as one moved outboard from the spanwise position where the previous trailing vortex was shed. All of the vorticity on the wing must eventually be shed downstream. The flow direction in the field downstream (or upstream for that matter) of the lifting line is then a sum of the contributions of all the trailing vortices, the bound vortex, and the free stream. The perturbation in the free stream velocity field resulting from these contributions is most intense in a sheet which for positive lift moves downward and to the rear from the lifting line. In the physical situation which this model represents this sheet is essentially the center of the wing wake. From equation (2) it is evident that the greater the wing lift the greater the vortex strength; thus it is reasonable to expect that the greater the wing lift the greater will be the downward deflection of the wake centerline as it moves aft.

Attention will now be directed to ways of evaluating the Γ distribution over the wing since it is essential for downwash calculations. Reference 8 notes that the main problem of lifting line theory is the determination of the spanwise distribution of air loads on wings from the fundamental equation of the theory. Its simpliest form relates the absolute and effective angles of attack,

$$\alpha_{a} = \alpha_{o} - \alpha_{i} \tag{3}$$

where

 α_a = absolute angle of attack

 α_{α} = effective angle of attack

 α_i = induced angle of attack.

The effective angle of attack may be expressed in terms of Γ by writing the section lift equation as

$$\rho V \Gamma = \rho V^2 c m_0 \alpha_0 / 2 \qquad \text{or} \qquad \alpha_0 = \frac{2\Gamma}{m_0 V c}$$

where p = density of air m = section lift curve slope.

Now the induced angle of attack may be written as - $\tan^{-1}(\frac{w}{V}) \approx - w/V$ and since w can be expressed in terms of Γ , then the only unknown in the fundamental equation is Γ . Using the Biot-Savart Law the downwash velocity w at the point y on the bound vortex, induced by a vortex behind the wing at the point y may be written as

$$w_{y_{O}} = \frac{d\Gamma}{4\pi} \frac{1}{y_{O} - y} . \tag{4}$$

Replacing dr by (dr/dy)dy and noting that the downwash at y resulting from all the trailing vortices may be obtained by integrating w from - b/2 to b/2 (b is the wing span), then

$$w_{y_0} = +\frac{1}{4\pi} \int_{-b/2}^{b/2} \frac{d\Gamma/dy}{y_0 - y} dy$$
 (5)

The fundamental equation can now be written in the form

$$(\alpha_a)_{y_o} = (\frac{2\Gamma}{m_o Vc})_{y_o} + \frac{1}{4\pi V} \int_{-b/2}^{b/2} \frac{d\Gamma/dy}{y_o - y} dy$$
 (6)

where the subscript refers to the variable evaluated at the point y_0 .

Probably the best known procedure for solving the fundamental equation is given by Glauert in Reference 9. The first step is to invoke the following substitutions:

$$y = b/2 \cos \theta \tag{7}$$

and

$$\Gamma = Vb \sum_{n=1}^{\infty} A_n \sin n\theta .$$
 (8)

The sine series rather than the cosine series is chosen for Γ because the boundary conditions of $\Gamma=0$ at both wing tips $(\theta=0$ and $\theta=\pi)$ are automatically satisfied for all values of A. The constants A_n are found by determining the values necessary to force the flow over the wing to be tangent to the mean camber surface. It can then be shown that the fundamental equation can be written as

$$\sum_{n=1}^{\infty} \left[A_n \sin n\theta(\mu n + \sin \theta) \right] = \frac{\mu}{2} \alpha_a \sin \theta$$
 (9)

where $\mu = m_{o}c/(4b)$.

The above equation is valid for any spanwise station (θ between 0 and π), and in general μ and α will be functions of θ . The problem has been reduced to one of determining the values of the coefficients A, which will satisfy the above equation at every desired value of θ along the span of the wing in question. If a 5 term series is desired for Γ then equation (9) must be applied at 5 spanwise stations yielding 5 equations in the 5 unknown A 's. Once the A 's have been obtained then Equation 8 will yield Γ for different spanwise positions.

As an alternative to solving Equation 9 at several spanwise stations, the computer programs given in Reference 4 are quite useful. Programs are presented to (1) calculate the lift, drag, and moment coefficients of conventional airfoils (two-dimensional) and (2) given the wing planform shape and airfoil characteristics for the root and tip sections, extend these two-dimensional characteristics to three dimensions. By using a lifting line theory, the three-dimensional extension yields local lift, drag, and moment coefficient information at several spanwise stations along the wing span. The section lift coefficients may be used directly in Equation 2 to compute the strength of the bound vortex.

With the foregoing as background, attention will now turn to literature specifically treating the calculation of downwash. Two 1939 NACA Reports have become classics in the field: NACA TR-648 (Ref. 10) and NACA TR-651 (Ref. 7). The latter presents methods for predicting important wake parameters in terms of the distance behind the airfoil trailing edge and the profile drag coefficient for plain and flapped wings. The methods were based on a correlation of extensive experimental measurements of downwash angles and wake characteristics. Downwash was computed in the wing chord plane using the Biot-Savart equation

operating on a vortex system made up of a bound vortex at the wing quarter chord and a planar vortex sheet extending straight behind the quarter-chord line to infinity. It is pointed out that the wing wake coincides with the trailing vortex sheet because of their common origin at the trailing edge and their equal freedom to move in the induced velocity field behind the wing. The vertical displacement of the vortex sheet can therefore be approximated by integrating the downwash angle in the streamwise direction from the trailing edge to some specified distance downstream. Silverstein, Katzoff, and Bullivant used the idea of superposition to obtain maps of constant downwash angles behind the wing. First, using a planar vortex system, downwash angles were calculated at several points in the plane of symmetry to yield a contour map similar to that of Figure 2. This map was then distorted in the vertical plane to account for the vertical displacement of the vortex sheet. The distorted contour map is also shown in Figure 2. Using this procedure, which neglects spanwise curvature of the wake sheet as well as vortex roll-up effects, agreement with experimental data is good at distances typical of to the tail plane locations.

In NACA TR-648 (Ref. 10) Silverstein and Katzoff prepared downwash charts to make the methods presented in TR-651 more readily useable in design activities. Included in the report are curves of the lift and drag of flapped airfoil sections and charts for finding the contribution of the different types of flaps to the total wing lift. The downwash charts are for elliptical wings and wings of taper ratios 0.1, 0.2, 0.3, and 0.5, with aspect ratios of 6, 9 and 12, having flaps covering 0, 40, 70 and 100 percent of the wing span. These charts may be used without a prior knowledge of the material in TR-651. Although written some 35 years ago, these reports are still the basis of current downwash predictions for light aircraft.

The interest in high speed flight led to some new downwash investigations in the late 40's and early 50's. In Reference 11 a study was made in the Langley 7- by 10-foot wind tunnel to determine downwash angles behind wings of various sweep angles and aspect ratios. Although the emphasis was on sweep effects, downwash characteristics were also measured for some unswept wings. The results are displayed graphically as curves of constant downwash angles. In 1954 an experimental investigation was conducted by Tothurst (Ref. 12) to define the downwash field and vortex sheet shape behind a large-scale wingfuse lage combination incorporating a 63° swept-back wing of aspect ratio 3.5. Data is presented for 9 vertical-transverse planes behind the wing for 3 angles of attack at a Reynolds number of 6.1 million. A comparison of these experimental results with theory showed that an acceptable approximation to the downwash distribution within the distance surveyed could be obtained if the vortex sheet were assumed to be flat and the spanwise vorticity distribution were assumed to be that of the wing. Rogers (Ref. 13) studied the application of two-dimensional vortex theory to the prediction of flow fields behind wings of wing-body combinations at subsonic and supersonic speeds. The wing trailing vortex was represented initially by line vortices distributed to approximate the spanwise distribution of circulation along the trailing edge of the exposed wing panels; however, a bound wing vortex was not included.

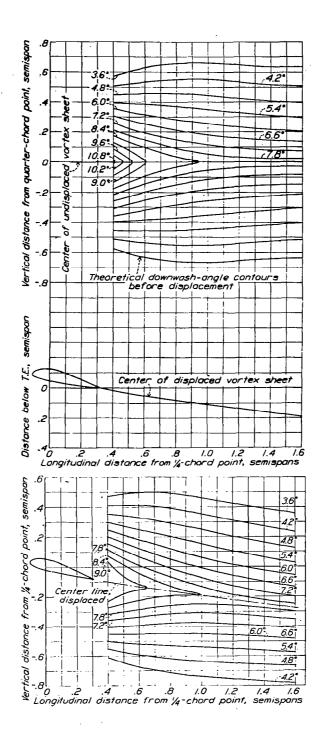


Figure 2. Example of downwash calculation procedure (Ref. 7) in the plane of symmetry for a USA 45 airfoil at $\rm C_L$ = 1.175.

The afterbody was represented by corresponding image vortices within the body. Two-dimensional line-vortex theory was then used to compute the induced velocities at each vortex, and the resulting displacement of each vortex was calculated by means of a numerical stepwise integration procedure. The displacement of each vortex independently permits inclusion of both the roll-up phenomenon and the spanwise wake-sheet curvature. Rogers found that this method predicted vortex paths at high speeds with reasonable facility and accuracy.

In 1970 Butter and Hancock presented a method (Ref. 14) for calculating the shape of the trailing vortex system behind a swept wing at low speed. The authors were concerned about the two-dimensional approaches which omit the main wing bound vortex; they believed that when C_i is large the wing circulation effects are significant. A method was therefore proposed which would include the effect of the main wing bound vorticity and the three-dimensional pattern of trailing vorticity. The wing is replaced by a single lifting-line bound vortex which represents the circulation distribution around the wing while the trailing sheet is approximated by a number of discrete line vortices. Starting with a nearly planar system (i.e., bound vorticity on the wing and trailing vorticity streamwise as in Figure 3) and using a step-by-step process, working downstream aft of the wing trailing edge, the vertical and spanwise displacements of the trailing sheet are determined. To calculate the position of the ith vortex at station 1, δx behind the 3/4-chord line (station 0), the sidewash and downwash velocities, (v, and w.) due to all the other vortices are calculated at $\delta x/2$. The change in vertical and spanwise position (δz and δy) for the ith vortex from station 0 to station 1 is then given by

$$\delta y = v_1 \delta x / V$$
 and $\delta z = w_1 \delta x / V$ (10)

This procedure is used to obtain the new position of each vortex at station 1. Downstream of station 1 each vortex extends to infinity using the y and z coordinates at station 1. Once the locations are established at station 1, the remainder of the stations downstream may be analyzed in a similar manner. Butter and Hancock found that the principal factors governing the accuracy of the results are the downstream step-size and the number and position of the vortices chosen to represent the trailing vortex sheet. They note that if too many trailing vortices are taken numerical difficulties may arise; induced velocities calculated at a point between two such vortices will be given by the difference of two large velocities of opposite sign. When compared with experimental results, the downwash angles were found to be too large near the trailing edge due to the concentrated nature of the bound vortex; however, further downstream agreement was good.

In Reference 15 Labrujere presents a method for calculating the vortex location behind a thick lifting wing. The flow around a wing in uniform onset flow is determined with the aid of a source distribution on the surface of the

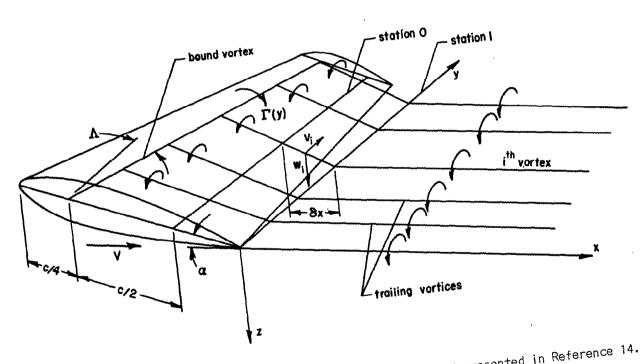


Figure 3. Coordinate system and wing placement for the method presented in Reference 14.

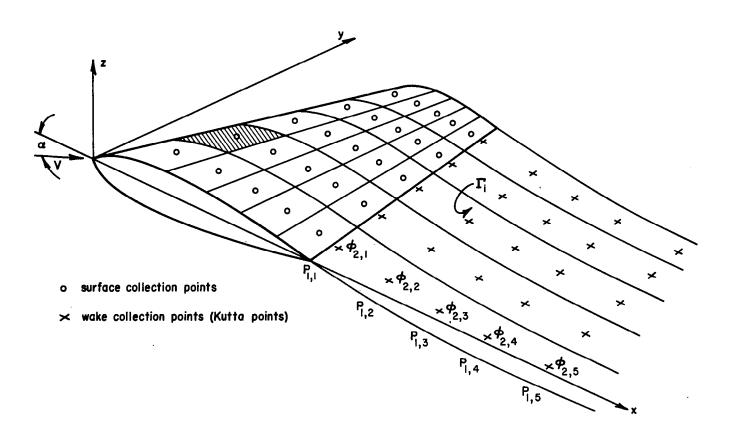


Figure 4. Representation of wing and wake by a source distribution on the wing surface and discrete vortices inside and behind the wing (Ref. 15).

wing and a vortex distribution on its camber surface and wake. The wing and camber surface are divided into a number of strips whose edges are formed by lines y = constant and which are each subdivided in a number of quadrilateral panels. Along the periphery of each camber panel a line vortex is located (see Figure 4). The strengths of these "singularities" are determined by imposing the boundary condition of tangential flow to the wing surface at a number of surface points and the condition of tangential flow to the trailing vortex sheet at a number of "Kutta points" noted in Figure 4. Since the position of the vortex sheet and the strength of the singularities are related "non-linearly", an iterative procedure is required in order to determine the shape of the sheet as well as the singularity distributions for a given wing and at a given angle of attack. Although only a limited comparison with experimental results was made using this method, the agreement was good.

Comparing Labrujere's technique with that of the previous reference, there are three reasons why the Butter and Hancock method is preferred as the basis for further work: (1) Labrujere combines the problems of the flow over the wing and the flow in the wake, solving them simultaneously; for a large number of panels both on the wing and in the wake this requires both more computer storage and a longer execution time than is required for the two problems independently (necessary in the Butter and Hancock approach). (2) The iterative nature of Labrujere's method may necessitate several executions unless the initial estimate of the wake shape is accurate. (3) Although Butter and Hancock's method may be used iteratively to improve accuracy, they found that for step sizes of a quarter semispan and smaller, subsequent iteration did not significantly affect the position of the trailing vortices.

In the last few years the interest in trailing vortex sheets has turned to the far field problem. At large distances behind the wing, vortex roll-up has occurred, and the hazard of one aircraft flying into the vortex core of another aircraft has spurred interest in trying to analytically predict the shape and velocities of a rolled vortex pair as well as the dissipation of this vortex pair with time. References 16, 17, and 18 cover the topic very well and discuss the pertinent work which has been done to the present time.

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WAKE VELOCITY PROFILE

While an inviscid theory is acceptable for predicting the location and inclination of the wing wake, the estimation of actual velocities requires a viscous analysis. The velocity deficit behind a wing is a function of the wing drag, a viscous phenomenon caused by the shear forces which the wing introduces in the fluid. The only really correct way to attack the problem is to solve the full, time-dependent Navier-Stokes equations of motion in three-dimensions over a substantial region. With present computers and computational techniques, computers will have to grow in storage size and speed by one or two orders of magnitude in order to obtain an accurate solution to the problem in the space of a few hours.

Boundary layer theory, which has been a valuable tool in solving for the viscous flow over airfoils and even bodies at zero or small angles of attack (Refs. 19 and 4), has also been applied to the flow in jets and wakes. Boundary layer theory consists of simplifying the Navier-Stokes equations so that they are applicable in the viscous flow near the surface of a body or in a wake. For the flow over a body the region where viscous effects are dominant is usually very thin compared to the body size. The equations are simplified by estimating the order of magnitude of each term and neglecting those which are small compared with the other terms. As might be expected, these simplified equations are much easier to solve, yet they retain the correct physical description of the flow in most cases. The conventional way of approaching the wake problem is to assume that the flow downstream of the trailing edge can be described by the boundary layer equations which are then solved by a momentum integral or finite-difference method. The remainder of this section will review some of the pertinent literature on the determination of wake velocity profiles.

Two-dimensional wakes were probably first investigated by H. Schlichting In his thesis presented to Goettingen University in 1930. In his general text, Boundary Layer Theory (Ref. 20), he notes that a wake is formed behind a solid body which is being dragged through a fluid at rest or behind a solid body which has been placed in a stream of fluid. The velocities in a wake are smaller than those in the main stream and the velocity losses in the wake amount to a momentum loss in the fluid due the body drag. The spread of the wake increases as the distance from the body is increased, and the differences between the velocity in the wake and that outside become smaller. A wake is a free turbulent flow (not confined by solid walls) and therefore of boundary layer nature. This means that (1) the region of space in which a solution is being sought does not extend far in the transverse direction, as compared with the main flow direction, and (2) the transverse gradients are large. The problem can therefore be studied using the two-dimensional, steady, boundary layer equations given below:

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = \frac{1}{\rho} \frac{\partial \tau}{\partial y} \qquad (x-momentum equation)$$
 (11)

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \approx 0$$
 (continuity equation) (12)

where x and u are the coordinate and velocity along the wake centerline, y and v are the coordinate and velocity normal to the wake centerline, p is the density of the fluid, and τ is the turbulent shearing stress (see Figure 5).

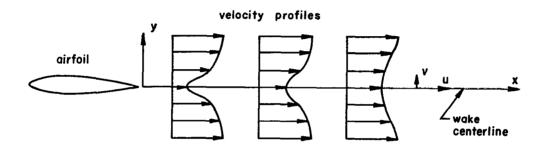


Figure 5. Sample velocity profiles in an airfoil wake.

The pressure gradient term has been dropped from the x-momentum equation because, from a certain distance behind the body on downstream, the pressure remains essentially constant in the y-direction. This assumption is not necessarily true near the airfoil trailing edge. To integrate Equations 11 the turbulent shearing stress must be expressed in terms of the main flow parameters. One of the simpliest and most widely used wake flow models for τ is that given by Prandtl in Equation 13.

$$\tau = \rho \varepsilon \frac{\partial u}{\partial y} = \rho cb \left(u_{\text{max}} - u_{\text{min}} \right) \frac{\partial u}{\partial y}$$
 (13)

where b denotes the width of the wake, c is an empirical constant, and ϵ is the virtual kinematic viscosity or eddy viscosity, assumed constant over the whole wake width. Schlichting points out that experience has shown that for two-dimensional turbulent wakes, the wake width increases as \sqrt{x} while the centerline velocity decreases as $1/\sqrt{x}$.

As noted in Reference 20 Goertler and Reichardt investigated the twodimensional wake behind a circular cylinder. Goertler found that if he assumed:

- (1) $u_1 = U u$ which at large distances from the body is small compared to U, the freestream velocity,
- (2) the drag on the cylinder is obtained by applying the momentum theorem far downstream so that

$$D = h\rho \int_{y=-\infty}^{y=+\infty} u_1(U - u_1) dy$$
 (14)

where D is the drag on the cylinder of height or length h, (3) that the second term of Equation 11 is small compared to the first,

then, by integrating the simplified version of Equation 11

$$\frac{u_1}{U} = \frac{1}{4\sqrt{\pi}} \frac{UC_D d}{\varepsilon_0} \frac{1/2}{(\frac{x}{C_D d})^{-1/2}} e^{(-\eta^2/4)}$$
(15)

where: C_D = cylinder drag coefficient

 ε_0 = constant eddy viscosity

d = cylinder diameter

x = distance downstream behind the cylinder

 η = nondimensionalized y-coordinate = y $\sqrt{\frac{U}{\epsilon_{\rm O} x}}$.

Upon comparison with experimental measurements made by Schlichting, Goertler evaluated the constant in Equation 13 with the relation

$$\epsilon_{o} = (0.047)(2b_{1/2} u_{1_{max}})$$

where: $b_{1/2}$ = half the wake width halfway between u_1 and u_1 at some u_1 = the maximum value of u_1 in the wake at that x-station.

Using similar assumptions and a slightly different eddy viscosity model, Reichardt arrived at the following expression for $\mathbf{u}_1\colon$

$$\frac{u_1}{U} = \frac{\sqrt{10}}{18(.18)} \left(\frac{x}{C_D d}\right)^{-1/2} \left\{1 - (y/b)^{3/2}\right\}^2.$$
 (16)

Schlichting (Ref. 20) notes that the two solutions for the wake velocity actually do not differ much one from the other.

While the above work was concerned with the wake of a circular cylinder, in 1939 Silverstein, Katzoff, and Bullivant (Ref. 7) generalized the available experimental results so that velocity profile and wake width information behind airfoils could be predicted in terms of the downstream distance and the profile drag coefficient. The profile drag of an airfoil may be approximately equated to the loss of momentum in the wake by the relation:

$$d_{O} = \rho \int_{-\infty}^{\infty} u(U - u) dy$$
 (17)

where $d_{\rm O}$ is the drag per unit span. At distances behind the wing comparable with tail-plane location, where the static pressure in the wake has reached that of freestream, experimental investigations have shown that Equation 17 may be approximated in coefficient form by the more elementary expression:

$$c_{d_{O}} = \frac{1}{c} \int_{-b/2}^{b/2} (1 - \frac{q}{q_{O}}) dy$$
 (18)

where,

 $c_{\mbox{\scriptsize d}}^{}$ = section profile drag coefficient $q/q_{\mbox{\scriptsize O}}^{0}$ = ratio of dynamic pressure in the wake to that in the free-stream $$\mbox{\scriptsize b}$$ = wake width

c = wing chord.

The wake may be completely described by the width b, the loss of dynamic pressure at the wake center Δq , and the shape of the wake profile. As an aid in generalizing the results, the following nondimensional ratios were adopted:

$$\begin{split} \eta &= \frac{\Delta q}{q_0} = (1 - q/q_0) \\ \zeta &= \frac{1}{2} \left(\frac{\text{wake width}}{\text{wing chord}} \right) = \frac{b}{2c} \\ \xi &= \frac{\text{distance behind trailing edge of wing}}{\text{wing chord}} = \frac{\ell}{c} \; . \end{split}$$

Using Prandtl's proportionality relations

$$\zeta \sim \xi^{1/2} c_{d_0}$$
 and $\eta \sim \frac{c_{d_0}^{1/2}}{\xi^{1/2}}$ (19)

the available experimental data was used to find the proportionality constants which should be used in Equations 19. It was found that:

$$\zeta = 0.68 \, c_{d_0}^{1/2} \, (\xi + 0.15)^{1/2}$$
 (20)

$$\eta = \frac{2.42 \text{ c}_{d}^{1/2}}{\xi + 0.3} \tag{21}$$

fit the data very well. The equation for η was found to vary with $1/\xi$ rather than $1/\xi^{1/2}$ as mentioned previously. The authors point out that discrepancy is probably associated with the high values of η near the trailing edge of the experimental data used for correlation; in Prandtl's formulation η was assumed small. For a complete wake description, the shape of the profile must also be defined. The profile shape was found to be closely approximated by either of the following empirical relations:

$$\frac{\eta'}{\eta} = \begin{bmatrix} 1 - (\frac{\zeta!}{\zeta}) \end{bmatrix}^{1.75}$$
 (22)

or

$$\frac{\eta'}{\eta} = \cos^2(\frac{\pi \zeta'}{2\zeta}) \tag{23}$$

where η' = relative loss in dynamic pressure ζ' = distance from wake centerline (ζ' < ζ).

The profiles given above are assumed symmetric about $\zeta'=0$ and for ξ values in the vicinity of the tail plane this is not a bad approximation even for unsymmetric airfoils.

In TR-648 (Ref. 10) Silverstein and Katzoff made the methods presented in TR-651 easily adaptable to design by preparing charts for determining the velocity profile at the horizontal tail. Over the years both TR's have been very valuable in predicting tail plane velocity profiles for light aircraft.

In 1947 an investigation of free turbulent mixing was presented by Liepmann and Laufer in Reference 21. The investigation examined the various ways turbulence had been modeled up to that time and discussed the physical significance of the models using experimental measurements of the mean velocity, the intensity and scale of turbulent fluctuations, and the turbulent shear in a two-dimensional mixing zone. The authors decided that the assumptions of constant mixing length and constant exchange coefficients (as in Equation 13) across the wake width were, strictly speaking, incorrect. Measurements of the field fluctuating velocities in a turbulent mixing zone show that both the mixing length and exchange coefficient vary across the mixing region, contrary to the assumptions made by Prandtl and others. They concluded that if only the mean-velocity distribution of a turbulent flow problem is desired, it usually can be obtained by dimensional considerations, assuming a reasonable curve (e.g., an error function in the case of a mixing region), and determining one constant from experiment. (This agrees with the methods already presented from References 20 and 7). Also, for an understanding of turbulent flow in general, a study of various mean-velocity distributions is of little use; the field of turbulent fluctuations must be studied in detail probably requiring a knowledge of the diffusion of turbulent energy. The constant exchange coefficient as presented in Equation 13 can therefore be used in a turbulence model with good success if only mean velocity profiles are desired; but for any deeper understanding of turbulence, the microstructure must be investigated more fully.

The subject of eddy viscosity models is treated to some extent in References 22 and 23. Elassar and Pardolfini, using a multilevel linear difference scheme examined four eddy viscosity models and evaluated the constants in these models by comparing calculated velocity profiles with experimental data in the similarity region. The thrust of the report is directed toward high-speed compressible flow, and all the models are more complex than Equation 13. In Reference 23 similarity solutions of the boundary layer equations in wakes with tailored pressure gradients were obtained. Experimental data was used to obtain a value for the constant eddy viscosity and the agreement between theory and experiment is described as good. While both of these reports are valuable in a general nature, it would be desirable to have viscosity constants evaluated using data obtained in the wake behind an airfoil. References 24 and 25 indicate that boundary layer solution procedures are being applied to high-speed turbulent mixing layers using more elaborate viscosity models than that given in Equation 13. These same techniques should be readily adaptable to low speed turbulent mixing and could be very useful if computer storage requirements and execution times are not excessive.

In order to improve upon the turbulent wake prediction methods, more experimental data are necessary for wake profiles at several stations behind an airfoil rather than at the tail-plane location only. References 26 and 27 are very helpful in this respect in that they present two-dimensional velocity profiles in the wakes of symmetrical Joukowski and Piercy airfoils respectively.

An 11.8 percent thick Joukowski airfoil was tested at angles of attack of 0 and 6 degrees for a Reynolds number of 0.42 million. Velocity profiles were measured at stations of 0.0005, 0.0025, 0.01, 0.25, and 0.5 chord lengths behind the airfoil trailing edge. A similar investigation on the 12 percent thick Piercy airfoil, with wires on the leading edge to force transition, yielded velocity profiles at 0.0005, 0.0025, 0.01, 0.25, and 0.4 chord lengths. In addition to the profiles, the drag coefficient and other boundary layer information was also measured.

A recent report by Goradia and Lilley (Ref. 28) also present some experimental data for profile measurements behind a modified NACA 0015 airfoil at several angles of attack. The report describes a procedure developed by the authors to improve two-dimensional drag predictions for single and multi-element airfoils by describing the airfoil wake using regions of similarity. Although correlations are given for only two or three airfoils and the computer program is not provided, the procedure seems to have improved the drag predictions given in CR-1843 (Ref. 29). Experimental data, taken in connection with this work is presented in both tabular and graphical form; however, the tabular data, particularly at stations near the airfoil trailing edge, indicate profiles which fail to return to freestream velocity at the upper and lower edge.

While the data given in the three references cited above are valuable, they were taken in the wake of symmetrical airfoils. More data is obviously needed, particularily for unsymmetric airfoils, but the lack of data is due in part to the high cost of wind tunnel testing and the difficulty of measuring wake velocities accurately.

A review of the literature revealed several papers concerning the effect of flow curvature on the formulation and solution of the two-dimensional boundary layer equations. Murphy (Ref. 30) formulated the boundary layer equations with curvature and indicated that even for laminar flow these equations are at their simplest more complex than the no-curvature case. Williams (Ref. 31) obtained a solution for a free jet flowing off a step only by assuming a curvature function which made the boundary layer equations similar (the streamwise coordinate did not appear explicitly). One encounters similar increases in solution complexity when treating three-dimensional boundary layers. Although the problem can be formulated, the computer storage requirements and execution times required with present machines and methods are excessive. Add to this the complexity of curvature and it is understandable why attention is still directed toward solving the simplified problem. Solution to such a problem, hopefully, preserved the qualitative aspects of the physical situation even though it cannot duplicate it quantitatively in all respects.

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PROGRAM FOR DOWNWASH AND

WAKE POSITION CALCULATIONS

GENERAL THEORY

For many years the vertical displacement of the wake centerline location and downwash behind wings has been calculated using a bound vortex and a finite number of trailing vortices. The spanwise curvature of the trailing vortices and their roll-up may be included in the calculation by allowing the vortices themselves to be deflected in both the vertical and spanwise directions (Ref. 13 and 14). Analyses have also been conducted by representing the wing and vortex sheet as a single vortex lattice and using an iterative solution procedure with boundary conditions of no flow normal to the vortex panels to determine the wake location (Ref. 15). Because of the paneled wake procedure (lattice) achieves only a slight improvement in wake location at a large increase in computer cost, the WASH program presented here uses a method similar to those given in References 13 and 14. For simplification the x, y, and z coordinates are non-dimensionalized by the wing semispan, and a unity freestream velocity is assumed since only ratios of induced velocities to freestream velocity are required to estimate the downwash and sidewash angles.

The first step in computing the downwash characteristics and wake position is that of representing the wing by a bound vortex at the wing quarter-chord and by a trailing vortex system running aft from the quarter-chord line. The symmetric half-wing is placed in the coordinate system shown in Figure 6. The root chordline is in the xz-plane at y = 0, with the origin at the trailing of the wing root. The root chordline has an incidence, α , with the negative x-axis.

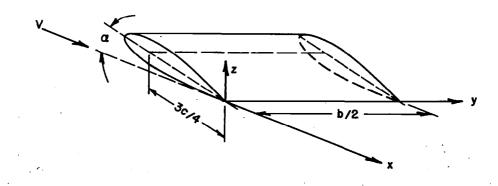


Figure 6. Definition of coordinate system and wing placement used in WASH program.

The analysis will be limited to unswept wings; therefore, the ${\sf x}$ and ${\sf z}$ coordinates of the wing quarter-chord are given by

$$x_b = -\frac{3c \cos \alpha}{2b}$$
 and $z_b = \frac{3c \sin \alpha}{2b}$

where

 (x_b, y_b, z_b) = the coordinates of the bound vortex normalized by the semispan

b = wing span

c = wing root chord

 α = wing angle of attack.

The strength of the bound vortex is calculated using Equation 2 once the section lift coefficient distribution is known. Although the WASH program was designed to use the output of the three dimensional aerodynamic characteristics program given in Reference 4, any procedure may be used to calculate the section lift coefficients. The lift coefficients at 10 different normalized spanwise stations must be read into the WASH program. The specification for both is ordered from positive wing tip to wing root* (see Figure 7).

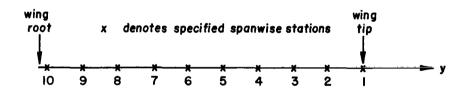


Figure 7. Ordering scheme for spanwise station and section lift specification.

Recall of course that the wing and its flow field is being represented by a system of horseshoe vortices. The initial streamwise position of the various trailing vortices is defined by assuming the vortices are shed at stations midway between the 10 specified y values on each semi-span, <u>i.e.</u>, on each half of the lifting line. In carrying out the computations, advantage can be taken of the assumed symmetry in the loading and the geometry. In this fashion, the section lift coefficients as well as the input y stations and the positions of the shed vortices for the negative y axis can be defined. A schematic of the

^{*} The root value for y cannot be zero; it may be a very small number, but because of the technique used for estimating the bound vortex contribution, the value must be non-zero.

20 stations at which the section lift coefficients are specified and the 18 shed vortex stations for the entire wing is given in Figure 8.

x denotes specified spanwise stations for complete wing

I denotes shed vortex stations for complete wing

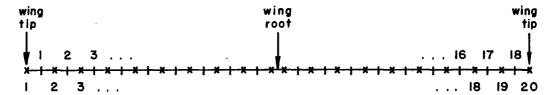


Figure 8. Reordered specified spanwise stations and shed vortex stations for complete wing.

Once the bound vortex strength is calculated using Equation 1 at the specified y stations, the strength of the shed vortices is computed by the change in Γ from one station to the next. Thus, for the right half of the wing the trailing vortex system is similar to that given in Figure 9.

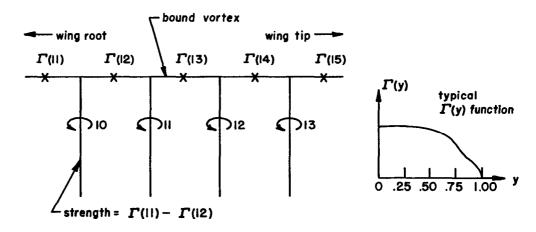


Figure 9. Example of indexing procedure used for the trailing vortex system on the right half of the wing with a typical $\Gamma(y)$ distribution.

Each initial trailing vortex is made up of two straight line segments, one from the bound vortex to the trailing edge and another from the trailing edge to infinity in the x-direction parallel to the freestream (see Figure 10).

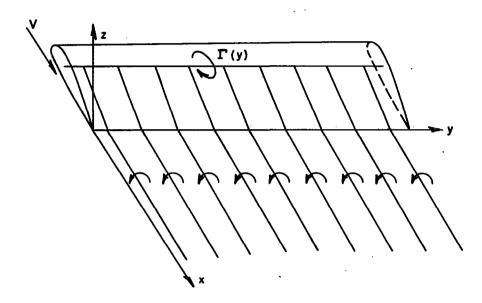


Figure 10. Example of initial approximation of trailing vortex system.

The net velocity induced by the vortex system at a point in the vicinity of the wing is computed by summing the contributions from the bound vortex and every straight line segment of each trailing vortex. The velocity induced at a point due to a vortex is defined by the Biot Savart law (Equation 2). An alternate form of this equation for straight line filaments is given in Reference 5 as

$$dW = \frac{\Gamma}{4\pi} \frac{\sin \theta \ d\ell}{r^2}$$
 (24)

where

dW = total velocity induced at a particular point by a filament dl

 Γ = strength of the vortex filament

r = distance to increment of filament at the point the velocity is induced

 θ = angle between the length r and the filament.

The contribution of the bound vortex is calculated by integrating Equation 24 from the negative wing tip to the positive tip. Expressing $\sin \theta$ and r in terms of the x, y, and z coordinates, and noting that $d\ell$ becomes dy, the induced velocity at a point (x, y, z) due to the bound vortex is written as

$$W_{b} = \int_{-1}^{1} \frac{\Gamma(y_{o}) b/2 \sqrt{(x - x_{b})^{2} + (z - z_{b})^{2}} dy_{o}}{4\pi [(x - x_{b})^{2} + (y - y_{o})^{2} + (z - z_{b})^{2}]^{3/2}}$$
(25)

where all coordinates are non-dimensionalized by the semispan. Equation 25 may be solved numerically, or if a functional form is known for $\Gamma(\gamma_0)$, it may be integrated in closed form. In order to use the closed form technique, two successive specified values of $\Gamma(\gamma)$ for the bound vortex were fitted using the cubic spline given in Reference 33 matching first and second derivatives at the end points. The cubic spline fit is of the form

$$\Gamma(y) = A_{1j}y^3 + A_{2j}y^2 + A_{3j}y + A_{4j}$$
 (26)

where
$$y_{j} \le y \le y_{j+1}$$
, $j = 1,2,...,19$.

Note that for each of the 19 intervals the cubic coefficients depend on the interval (y_j, y_{j+1}) in which the spanwise station lies, but they are constant in a given interval. It is this variation of the coefficients that gives the spline fit its remarkable curve fitting properties. Using the cubic representation Equation 25 is integrated (Ref. 34) in each of the 19 intervals yielding the total velocity induced by the bound vortex at the point (x, y, z). This total velocity is divided into a freestream component, u, and a vertical or downwash component, w, by the relation given below:

$$u_{b} = W_{b}(x - x_{b}) / \sqrt{(x - x_{b})^{2} + (z - z_{b})^{2}}$$

$$w_{b} = W_{b}(z - z_{b}) / \sqrt{(x - x_{b})^{2} + (z - z_{b})^{2}}$$
(27)

w and W are defined as positive in the negative z direction, and u is positive in the positive x direction. Since the bound vortex is always parallel to the y-axis, there is no sidewash component in \mathbf{W}_{b} . The streamwise component \mathbf{u}_{b} is usually very small compared with the freestream velocity.

The velocity induced by a trailing vortex is calculated by summing the effect of each straight line segment of the vortex. The total velocity induced at a point by a straight line vortex segment is also calculated using Equation 24; the evaluation is however, much simplier than the bound contribution because I along all segments of a trailing vortex is constant. Thus, expressing dl and r in terms of θ , one has

$$W_{t} = \frac{\Gamma}{4\pi} \int_{\theta_{A}}^{\theta} \frac{\sin \theta}{h} d\theta$$
 (28)

where

W_t = is the total velocity induced at a point (x, y, z) by a vortex of length AR

vortex of length AB, θ_{A} and θ_{B} = angles between the length r and the filament at points A and B respectively, and h is the perpendicular distance from the point (see Figure 11).

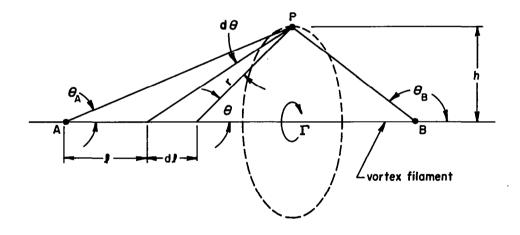


Figure 11. Nomenclature diagram for velocity induced by a straight-line vortex filament (Ref. 5).

Carrying out the integration indicated in Equation 28 yields

$$W_{t} = \frac{\Gamma}{4\pi h} (\cos \theta_{A} - \cos \theta_{B}) . \tag{29}$$

This total induced velocity must also be divided into its component parts: freestream, sidewash, and downwash velocities. As seen in Figure 12, the total induced velocity at P_0 due to a line vortex from P_1 to P_2 of strength Γ may be rewritten as

$$W_{t} = \frac{\Gamma(\cos\theta_{1} + \cos\theta_{2})}{4\pi b/2 d_{01} \sin\theta_{1}}$$
 (30)

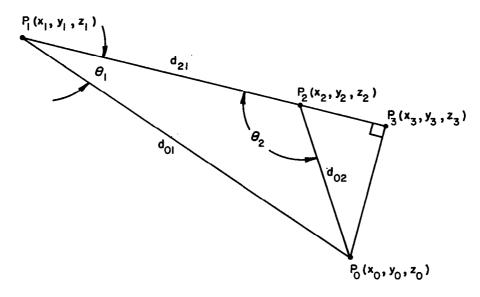


Figure 12. Schematic for velocity induced at P_0 due to a vortex from P_1 to P_2 .

The components are derived using the following relations to obtain the direction cosines:

$$d_{21} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

$$d_{01} = \sqrt{(x_0 - x_1)^2 + (y_0 - y_1)^2 + (z_0 - z_1)^2}$$

$$d_{02} = \sqrt{(x_0 - x_2)^2 + (y_0 - y_2)^2 + (z_0 - z_2)^2}$$
(31)

$$\theta_{1} = \cos^{-1}[(d_{21}^{2} + d_{01}^{2} - d_{02}^{2})/(2d_{21}d_{01})]$$

$$\theta_{2} = \cos^{-1}[(d_{21}^{2} + d_{02}^{2} - d_{01}^{2})/(2d_{21}d_{02})]$$

$$\times_{3} = x_{1} + d_{01} \cos \theta_{1} (x_{2} - x_{1})/d_{21}$$

$$y_{3} = y_{1} + d_{01} \cos \theta_{1} (y_{2} - y_{1})/d_{21}$$

$$z_{3} = z_{1} + d_{01} \cos \theta_{1} (z_{2} - z_{1})/d_{21}$$

$$A = (y_{2} - y_{1})(z_{3} - z_{1}) - (y_{3} - y_{1})(z_{2} - z_{1})$$

$$B = -[(x_{2} - x_{1})(z_{3} - z_{1}) - (x_{3} - x_{1})(z_{2} - z_{1})]$$

$$c = [(x_{2} - x_{1})(y_{3} - y_{1}) - (x_{3} - x_{1})(y_{2} - y_{1})].$$

The components can therefore be written as

$$u_{t} = W_{t} A/\sqrt{R}$$

$$v_{t} = W_{t} B/\sqrt{R}$$

$$w_{t} = W_{t} C/\sqrt{R}$$
(32)

where $R = A^2 + B^2 + C^2$.

In summary, the induced velocity components at a point are calculated due to (1) the bound vortex using Equations 25 and 27 and (2) a straight line segment of a trailing vortex using Equations 30 and 32. The velocity due to the entire vortex system is computed by summing the contributions from the bound vortex and each segment of the 18 trailing vortices.

The spanwise curvature in the trailing vortex system is modeled by representing each vortex by a number of straight-line segments which are free to follow the local direction of the flow. The position of these vortex segments is determined using a stepwise downstream marching procedure which will now be discussed.

As previously mentioned, the first approximation of the vortex sheet consists of the 18 trailing vortices with 2 segments each, one segment from the bound vortex to the y-axis and another from the y-axis to $x = \infty$ parallel to the x-axis. Since the actual vortex system behind a wing is displaced in both the y and z directions, the following procedure is used to compute the position of each trailing vortex at a length Δx behind the trailing edge. Noting Figure 13 and considering vortex #10 at station #2, the v and w induced velocity components due to all the other vortices are calculated halfway between stations #2 and #3 ($x = \Delta x/2$) using the y and z coordinates at station #2. The changes in spanwise and vertical position of vortex #10 in moving from station #2 to #3 is approximated by Equations 10 as

$$\Delta y = v\Delta x$$

$$\Delta z = w\Delta x .$$

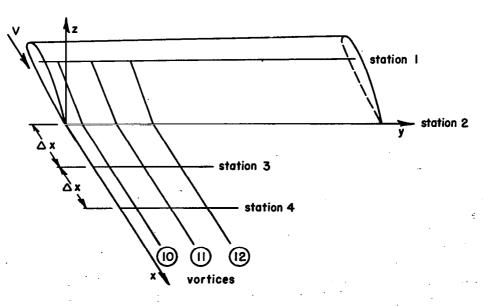


Figure 13. Schematic of downstream stepwise technique used in WASH program.

The position of the vortex at station #2 was (0, y(vortex #10), 0) and the position at #3 becomes (Δx , y(vortex #10) + Δy , Δz). A similar procedure is used to calculate the position of the other 17 trailing vortices at station #3. Downstream of station #3 the trailing vortices are assumed to go to infinity in the streamwise direction. After the position is determined at station #3 the procedure is reapplied at stations #4, #5, etc. until the vortex sheet is traced as far downstream as desired. The WASH program prints the coordinates of each vortex as well as the total vortex length from the trailing edge at each downstream station. The procedure discussed above is equivalent to that used in Reference 14 where it was found that for stepsizes as large as .25 semispans an accurate wake location was predicted. Butter and Hancock did note that numerical difficulties were sometimes encountered when more than 5 spanwise stations for the half-wing were used; however, the WASH program using double precision arithmetic utilizes 9 spanwise stations without numerical difficulty as long as the specified y stations are approximately evenly spaced. An example of a wake sheet calculated using the above procedure is given in Figure 14. The two views of this wake sheet were plotted using the PLOT program of Reference 4. The WASH program will punch a data set which may be read directly into the PLOT program; the data set requires only the addition of view cards at the rear defining the type of view desired.

Once the location of the trailing vortex sheet is determined then both downwash and upwash angle may be computed behind and ahead of the wing respectively using the bound vortex and the new vortex sheet. The WASH program is designed to calculate, at the user's option, three basic sets of information:

- (1) downwash and sidewash angles in a plane behind the wing at a constant x-station (a negative value for the x-station yields upwash angles ahead of the wing) indicating the variation with y and z,
- (2) downwash angles in the y = 0 plane of symmetry for 1.75 semispans downstream with z varying from .5 semispans above and below a user specified z-station,
- (3) upwash angles in the y = 0 plane of symmetry for 0.5 semispans upstream with z varying from .25 semispans above and below the leading edge z coordinate.

For each option presented above, a grid of coordinates, at which the downwash information is calculated, must be established. The first option was originally designed to compute the downwash in any x = constant plane at all the grid points determined by y varying from 0 to 1.1 semispans in steps of .05 semispans with z ranging from .25 semispans above and below a specified z station in steps of .05 semispans. This required calculating downwash and sidewash angles at 253 points. Numerical difficulties were usually encountered at one or more of the grid points because of the grid points being located very near a vortex segment. The vortex velocities by definition are unbounded

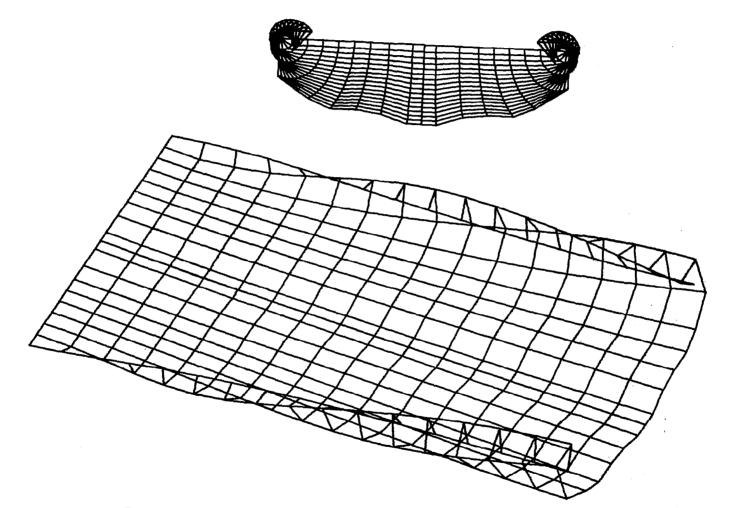


Figure 14. Sample of wake sheet end view and orthographic projection.

at the vortex center; thus, unrealistic velocities may be predicted if the grid point is too near a vortex segment. To correct this difficulty an attempt was made to determine an optimum distance to a filament such that the filament's contributions would be included or excluded depending on whether the distance to the filament was greater or less than the optimum. While this procedure was successful in producing reasonable values of downwash angle, it does not guarantee a smooth variation in downwash in either the y or z direction since the downwash at one of two closely-spaced points may include the contribution from a filament while the downwash computed at the other point may not.

To insure a smooth variation, the following procedure is used. The user-specified x-station at which the downwash information is required must be a multiple of the stepsize; for upwash calculations any negative x-station ahead of the wing leading edge may be used. The y and z coordinates for the 6 most inboard vortices on the positive y-axis are used to establish a new grid system. Using the y coordinate at one of the six vortices as constant, the total flow angularity (vector sum of downwash and sidewash angles) and the sidewash and downwash angles are calculated for z ranging from .25 semispans above and below the z coordinate of that vortex. This procedure is also carried out for the other five most inboard vortices yielding a grid system similar to that given in Figure 15.

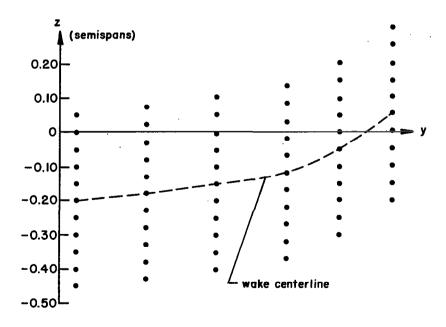


Figure 15. Example spacing for downwash calculations using NXORY=1 option (spanwise variation).

The numerical difficulties encountered because of the contribution of the vortex segment to the field in its immediate vicinity are eliminated by (1) excluding, for example, the contribution of vortex 11 when calculating the flow angles above and below the z coordinate of vortex 11, and (2) calculating downwash above only the six most inboard vortices which, for x-distances comparable to horizontal tail locations, have not rolled-up and therefore do not pass above or below another vortex trace. The exclusion of vortex 11 when determining the flow angles above and below it will not affect the downwash; however, the sidewash will be in error. Since the downwash and not sidewash is the quantity which the program is designed to predict, the error in sidewash is tolerated. The option discussed above is produced when the input variable NXORY is specified as 1 and STAT is read as the desired x-station in semispans. A detailed description of these and the other necessary input variables is given in the User Instructions section of Appendix A.

Option number two in the WASH program computes the downwash angles in the plane of symmetry, y = 0. The grid is specified by varying x from .25 to 1.75 semispans behind the trailing edge in steps of .05, and z ranging from .5 semispans above and below a midpoint z-value specified as the variable STAT. As above, numerical difficulties were encountered in some cases using this option because the most inboard shed or trailing vortex on a half-wing may be too close to some of the grid points. To remedy the problem in general, the downwash angles were calculated using only the 8 most-outboard vortices on both sides of the y = 0 plane, and the WASH program is written in this fashion. However, if the user desires to include the effect of the inboard vortex, the DO LOOP parameter may be changed from 8 to 9 on card PLA 110 of the WASH program. Inasmuch as the computations are made in the plane of symmetry, only half the wing need be analyzed to compute the downwash, and the sidewash is identically zero. This downwash information is computed in the plane of symmetry when the variable NXORY = 2 and STAT is the desired midpoint value of z in semispans.

If NXORY = 3, then upwash information is calculated in the plane of symmetry. The grid points at which upwash is computed are established by x ranging from the wing leading edge value of x at the wing root to .5 semispans ahead of the leading edge in steps of .05 semispans, and z varying from .25 semispans above and below the leading edge z coordinate. The upwash is calcuated using all 18 trailing vortices without numerical difficulty. It should be pointed out however that the upwash values at the leading edge are excessively large because of the proximity to the bound vortex at the wing quarter-chord.

The WASH program is made up of a mainline, four subroutines, and a function subroutine. The mainline is the control center for reading and writing the specified and calculated information as well as the coding responsible for tracing the position of the vortex system downstream. The mainline calls the following subroutines: (1) SPLINE to obtain a spline fit of the bound vortex strength versus semispan distance, (2) WB which computes

the induced velocity components at a point due to the bound vortex using the function WBB, (3) WTRAIL to calculate the induced velocity components at a point due to a straight-line trailing vortex segment, and (4) PLANE to determine the downwash information in the plane specified by the user. The mainline contains the coding responsible for tracing the shed vortices downstream using a maximum of 18 steps behind the trailing edge. Using this deflected vortex system the downwash information is calculated at each of the grid points given by subroutine PLANE for the user specified plane of interest.

The program listing, sample data set, and sample output are presented along with User Instructions in Appendix A. The next section of this report presents a brief discussion of results obtained by running the program for several test cases, some of which are compared with experimental data.

DISCUSSION OF PROGRAM RESULTS

Results given by the WASH program were compared with two separate examples of USA 45 wings (Ref. 7) at different angles of attack, and, in addition, a sample calculation of the wake sheet location and downwash at the tail was obtained for the ATLIT (Advanced Technology Light Twin) aircraft. The theoretical section lift distribution taken from Reference 7 and given in Figure 16 served as the basis of the calculations in the WASH program. Figures 17 and 2 show the experimental lines of constant downwash angle in the plane of symmetry behind the wing and the angles predicted in Reference 7, respectively. The results of the WASH program are given in Figure 18. Reference 7, notes that the theoretical downwash of Figure 2 along the wake centerline at large distances (two semispans) appears to be approaching a value of 7.8° , while the experimental value is less than 6.6°. Reference 7 indicates that the theoretical value given in Figure 2 is too large because the method did not include spanwise curvature. The WASH program, which includes spanwise curvature, gives a value closer to the experimental result in the vicinity of the horizontal tail location. Near the wing trailing edge the theoretical method of Reference 7 over-predicts the downwash angles while the WASH program underpredicts it as compared with the experimental value. It should be noted that some difference between theory and experiment may be attributed to the fact that the I distribution is theoretical rather than experimental.

The experimental I distribution given in Figure 19 for the USA 45 airfoil was inserted in the WASH program to compare the spanwise variation in downwash with experimental values presented in Figure 20. The WASH program results are presented in Figure 21. A comparison of these two figures indicate that the total flow angular deviations computed by WASH are smaller in general than the experimental values; also, Figure 20 depicts positive sidewash angles both above and below the wake centerline while WASH predicts positive below and negative above as would be expected by vortex theory.

The wake sheet is given for each USA 45 Γ distribution discussed above in Figures 22 and 23. Each wake sheet figure was obtained by executing the plot data set from the WASH program in the PLOT program of Reference 4. While both distributions are for the same airfoil section, an examination of Figures 16 and 19 gives an indication of how wake sheet shape is affected by the section lift distribution.

NASA is currently supporting the development of the ATLIT aircraft to investigate the potential of new aerodynamic techniques for improving the performance of light twin engine aircraft. A three-view of the ATLIT is given in Figure 24 and a perspective view is given in Figure 25. A contributer to this program, N. C. State University, is currently involved in both a performance prediction and a flight evaluation program for the ATLIT, the results of which should be published as a NASA Contractor's Report early in 1977. In conjunction with this program, it was decided to analyze the ATLIT wing using the WASH program to find the downwash characteristics at the horizontal tail

in the plane of symmetry. The section lift coefficient distribution of the wing with fuselage was obtained by the methods given in Reference 4. The nacelles were neglected for this test case. The program input data set is given in Figure A-2. Figure A-3 gives typical program output: tabulated data for the spanwise variation of the downwash and sidewash in the plane of the horizontal tail, the downwash in the plane of symmetry, and the upwash ahead of the wing for a wing lift coefficient of 1.22. The wake sheet plot (Figure 26) indicates that the high wing aspect ratio (ten) yields relatively low values of downwash in the vicinity of the horizontal tail. Figure 27 is included to show the variation of upwash ahead of the wing in the plane of symmetry along with the downwash variation behind the wing. The excessively large upwash angles at the leading edge are due to the nearness of the bound vortex at the wing quarter-chord.

The cases presented above, although limited in number, show good agreement with experimental data. These test cases also indicate the type of information yielded by the WASH program; to the extent that interference effects from the fuselage and horizontal tail can be neglected, the program fulfills the design objectives of defining both the wake sheet location in the vicinity of the horizontal tail and the downwash distribution in both the spanwise and freestream directions. The program's capability for computing upwash ahead of the wing has also been demonstrated.

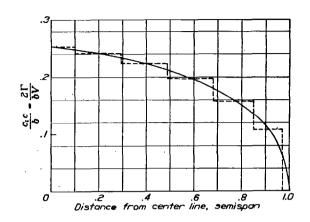


Figure 16. Theoretical $\Gamma(y)$ distribution for the 3.66 m USA 45 tapered wing with $C_L = 1.175$ (Ref. 7).

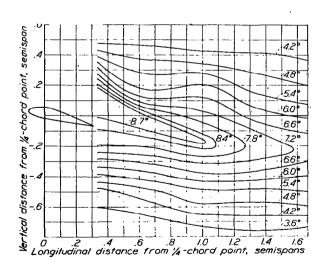


Figure 17. Experimental downwash angle contours in the plane of symmetry behind a 3.66 m USA 45 tapered wing with $\rm C_L$ = 1.175 (Ref. 7).

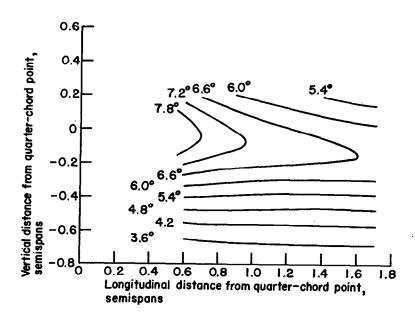


Figure 18. Downwash angle contours in the plane of symmetry behind a 3.66m USA 45 tapered wing at $\rm C_L$ = 1.175 using WASH program.

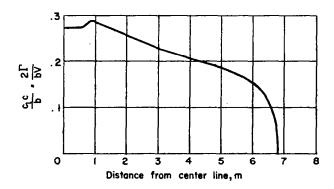


Figure 19. Experimental span load distribution for the USA 45 wing at C_L = 1.35 (Ref. 7).

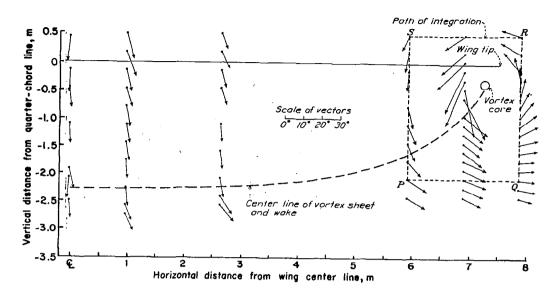


Figure 20. Experimental air flow 7.92m behind c/4 line of USA 45 wing at $C_L = 1.35$ with vectors denoting deviation from freestream (Ref. 7).

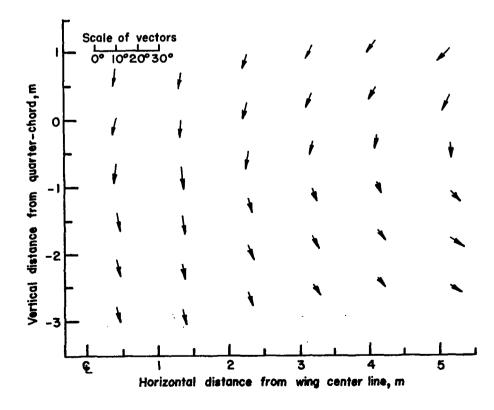


Figure 21. Air flow 7.92m behind c/4 line of the USA 45 wing at C_L = 1.35 using WASH program with vectors denoting deviation from freestream.

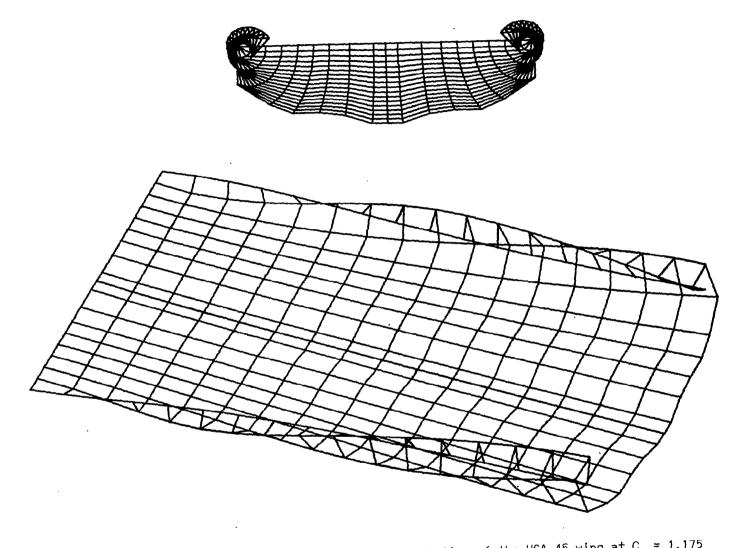


Figure 22. Wake sheet end view and orthographic projection of the USA 45 wing at C_L = 1.175 (Γ distribution taken from Figure 16).

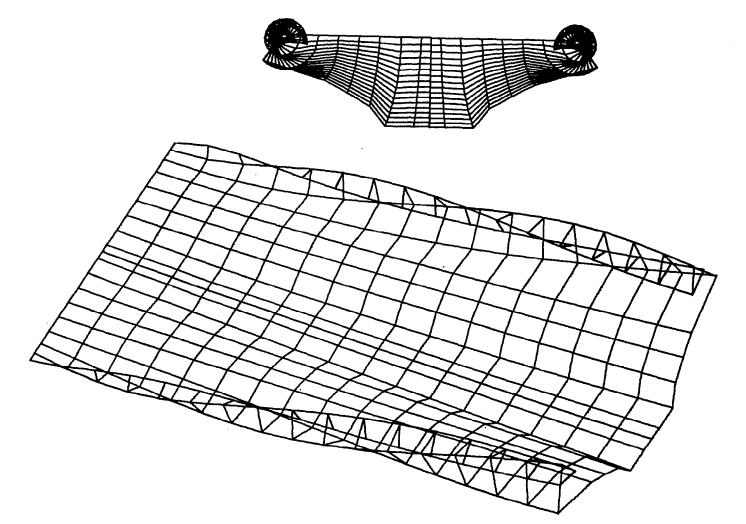


Figure 23. Wake sheet end view and orthographic projection of the USA 45 wing at C_L = 1.35 (Γ distribution taken from Figure 19).

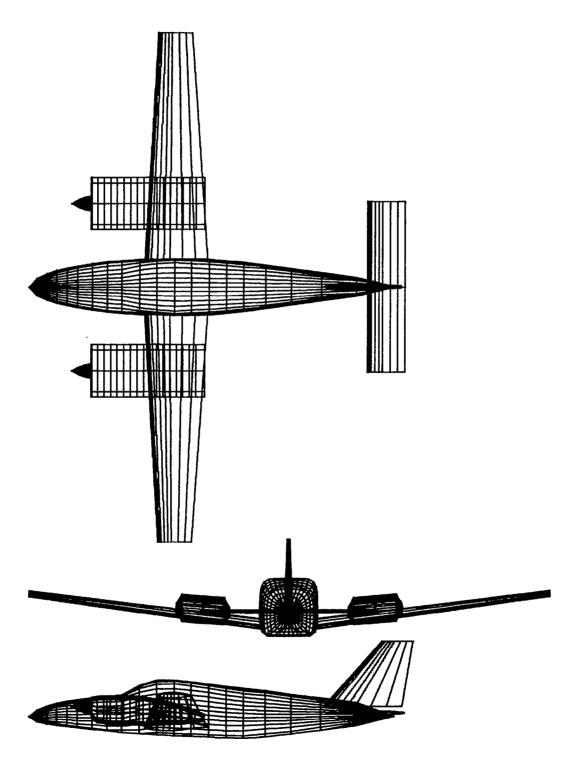


Figure 24. Plotted 3-view of ATLIT aircraft.

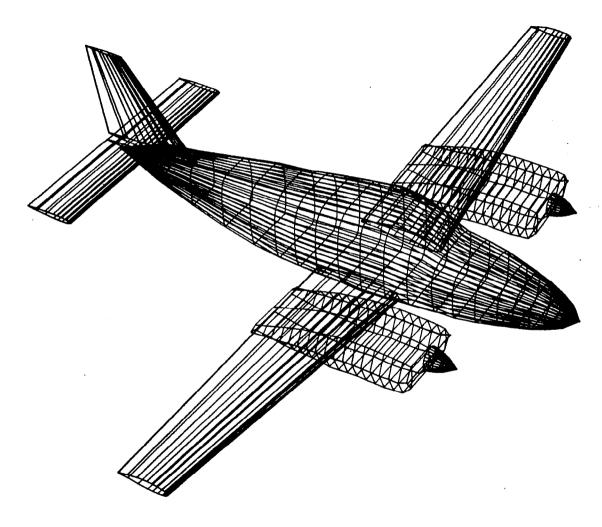


Figure 25. Perspective view of the ATLIT aircraft.

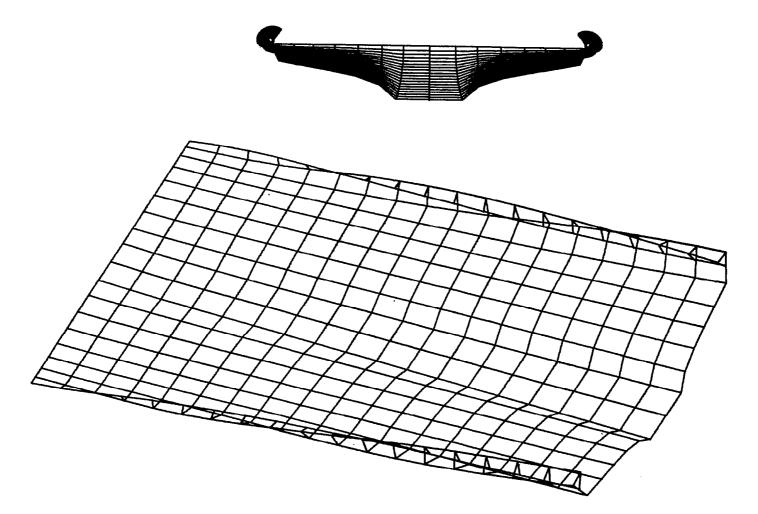


Figure 26. Wake sheet end view and orthographic projection of the ATLIT wing at C_L = 1.22.

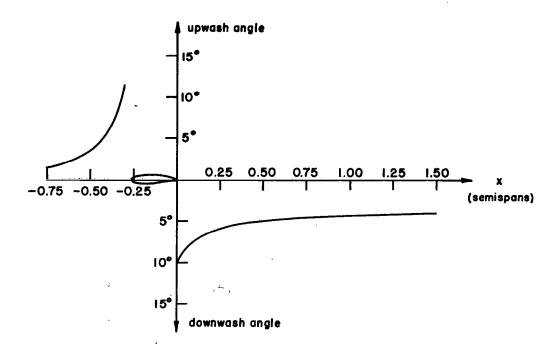


Figure 27. Upwash and downwash angles in the plane of symmetry of the ATLIT wing at $\rm C_L$ = 1.22.

* PROFILE CALCULATION

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GENERAL THEORY

Once the location of the wake sheet centerline has been established using the WASH program, a viscous solution behind the wing may be obtained by solving the two-dimensional boundary layer equations along wake streamlines defined by the shed vortex paths. This same technique was applied to boundary layer solutions over arbitrary bodies with good success in Reference 4, and the results should be reasonable in this application as long as (1) the spanwise flow is small compared to the freestream flow, and (2) the streamline curvature is not large. These conditions of course are violated as one moves downstream from the wing tip and the vortices begin to roll-up. However, for streamlines which pass near the horizontal tail the conditions for the use of two-dimensional boundary layer analysis are usually satisfied quite well. Thus, this approach should be adequate for the purpose of this study which is to determine the magnitude and direction of the flow in the vicinity of the horizontal tail. The WASH program permits only nine shed vortices to the half-wing; thus, probably no more than the three most inboard vortex traces will pass inboard of the tail tip section.*

As noted in the literature review, the inclusion of curvature in the boundary layer equations greatly increases the complexity. In order to determine whether or not curvature effects should be included in the analysis results from several executions of the WASH program were examined. When vortices for typical cases of spanwise lift distributions were traced downstream, it was found that while the inboard vortex streamlines were deflected in the vertical and spanwise directions, the curvature of these streamlines was small due to the relatively slow rate of change of downwash and sidewash angles (see Figures 14 and 26) along a given vortex path. Since the curvature of the inboard vortices is small, it should not play a dominant role in a boundary layer solution near the horizontal tail. Consequently, the curvature terms in the boundary layer equations were neglected, greatly simplifying the solution process.

In order to find the flow velocities along streamlines in the vicinity of the horizontal tail including the effects of fluid viscosity, the computer program WAKE was written. Given an initial velocity profile at the airfoil trailing edge^{+†}, the nonsimilar two-dimensional boundary layer equations are solved using a finite difference method with even stepsize in the transverse direction and unequal stepsize in the streamwise direction. The remainder of this section will be concerned with a discussion of the WAKE program theory.

The boundary layer equations (Equations 11 and 12) are written in a form more amenable to numerical solution through use of both the stream function ψ (defined by $u = \frac{\partial \psi}{\partial y}$ and $v = -\frac{\partial \psi}{\partial x}$) which automatically solves Equation 11, and a proper scaling of the x and \tilde{y} variables. The scaling variables η and ξ and the stream function ψ were assumed to be of the form

^{*} Because of typical span loadings, the third vortex out from the fuselage will probably be positioned at around 0.4 semi-spans, a location which should be further outboard than the tip of the horizontal tail plane on most light aircraft.

⁺⁺The computer program providing this initial velocity profile is given in Ref. 4.

$$\eta = \frac{y}{\sqrt{100c_d tx}} \quad \text{and} \quad \xi = \frac{x}{c}$$
 (33)

and

$$\psi(x,y) = U_{\infty}\sqrt{100c_{d}^{\dagger}x} f(\xi,\eta)$$
 (34)

where

c = wing chord

t = wing thickness

c_d = wing section drag coefficient

 U_{∞} = freestream velocity

 ξ = nondimensional distance downstream of the trailing edge

n = nondimensional, scaled y coordinate normal to the x-direction

 $f(\xi,\eta)$ = function of ξ and η which will appear as the unknown in the transformed boundary layer equations.

Since the continuity equation is identically satisfied by the definition of the stream function, it is necessary only to solve the momentum equation given by Equation 12 and rewritten, using Equation 13, as

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = \varepsilon \frac{\partial^2 u}{\partial y^2}.$$
 (35)

Introducing the definition of the stream function and replacing x and y by the scaled variables, Equation 35 becomes

$$\{U_{\infty}f'\}\{U_{\infty}(\frac{\partial f'}{\partial \xi}\frac{1}{c} + f''\frac{\partial n}{\partial x})\} - U_{\infty}\sqrt{100c_{d}+x} \{\frac{f}{2x} + \frac{\partial f}{\partial \xi}\frac{1}{c} + f'\frac{\partial n}{\partial x}\}\{\frac{U_{\infty}}{\sqrt{100c_{d}+x}} f''\}$$

$$= \frac{\varepsilon U_{\infty}}{100c_{d}+x} f'''', \qquad (36)$$

where the primed quantities denote derivatives with respect to the variable n. Simplifying the above equation, one has

$$\frac{f'}{c} \frac{\partial f'}{\partial \xi} - (\frac{f}{2x} + \frac{\partial f}{\partial \xi} \frac{1}{c})f'' = \frac{\varepsilon}{U_{\infty}(100c_{d} + x)} f''', \qquad (37)$$

or, multiplying by x and rearranging,

$$\frac{\varepsilon}{100c_d + U_{\infty}} f'''' + \frac{1}{2} ff'' - \xi \{f' \frac{\partial f'}{\partial \xi} - f'' \frac{\partial f}{\partial \xi}\} = 0.$$
 (38)

Equation 38 must therefore be solved at every ξ station (non-similar solution) downstream in order to obtain the velocity as a function of η . It is a third order partial differential equation in f requiring the three boundary conditions:

$$u(x,y\to\infty) = U_{\infty} \to u(\xi,\infty) = U_{\infty} \to f'(\xi,\infty) = 1$$

$$u(x,y\to\infty) = U_{\infty} \to u(\xi,-\infty) = U_{\infty} \to f'(\xi,-\infty) = 1$$

$$v(x,y=0) = 0 \to f(\xi,0) + 2\xi \frac{\partial f}{\partial \xi} \Big|_{\xi=0} = 0.$$
(39)

Equation 38 together with the boundary conditions given in Equations 39 is solved in the WAKE program by the finite difference technique described below. Let f' = T; then

$$T'' + \frac{c_1 f}{2} T' - c_1 \xi \{ f' \frac{\partial T}{\partial \xi} - T' \frac{\partial f}{\partial \xi} \} = 0 , \qquad (40)$$

where $c_1 = 100c_d + U_{\infty}/\epsilon$.

Simplify Equation 40 to read

$$T'' + \alpha_1 T' + \alpha_2 \frac{\partial T}{\partial \xi} = 0 , \qquad (41)$$

where

$$\alpha_1 = c_1(\frac{f}{2} + \xi \frac{\partial f}{\partial \xi})$$
 and $\alpha_2 = -c_1\xi f'$. (42)

Equation 41 has, through this process, been converted into a second order "linear" equation in T with supposedly known coefficients. This equation is solved by assuming a solution to evaluate the α 's and then, using an iterative process, T is computed numerically and the α 's are corrected after each iteration until convergence is attained. Consider the grid system shown in Figure 28. If the solution is known at some station m for all n, then using central and backwards difference formulas, the solution is constructed at the station m + 1 for all n. The derivatives are approximated with the following relations taken from Reference 19:

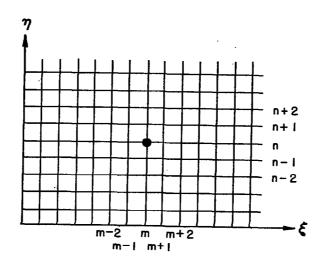


Figure 28. Grid system for finite difference solution.

$$\frac{\partial^{2}T}{\partial \eta^{2}}\bigg|_{n,m+1} = \frac{T_{n+1,m+1} - 2T_{n,m+1} + T_{n-1,m+1}}{(\Delta \eta)^{2}}$$

$$\frac{\partial T}{\partial \eta}\Big|_{n,m+1} = \frac{T_{n+1,m+1} - T_{n-1,m+1}}{2\Delta \eta}$$

$$\left. \frac{\partial T}{\partial \xi} \right|_{n,m+1} = \left[\frac{h_2}{h_1(h_1 + h_2)} \right] T_{n,m-1} - \left[\frac{h_1 + h_2}{h_1 h_2} \right] T_{n,m} + \left[\frac{h_1 + 2h_2}{h_2(h_1 + h_2)} \right] T_{n,m+1}$$

where $h_1=\xi_m-\xi_{m-1}$, $h_2=\xi_{m+1}-\xi_m$, and $\Delta\eta=$ equal stepsize in the η direction. Equation 41 is now rewritten as

^{*} This method is based on that presented by Cebeci and Smith in McDonnell-Douglas Aircraft Co. Inc. Report No. DAC-67130, October 1968, "A Finite-Difference Solution to the Incompressible Turbulent Boundary Layer Equations by an Eddy-Viscosity Concept".

$$\left[\frac{1}{(\Delta \eta)^{2}} + \frac{\alpha_{1}}{2\Delta \eta}\right] T_{n+1,m+1} + \left[\frac{-2}{(\Delta \eta)^{2}} + \alpha_{2} \left\{\frac{h_{1} + 2h_{2}}{h_{2}(h_{1} + h_{2})}\right\}\right] T_{n,m+1} + \left[\frac{1}{(\Delta \eta)^{2}} - \frac{\alpha_{1}}{2\Delta \eta}\right] T_{n-1,m+1} + \alpha_{2} \left[\left\{\frac{h_{2}}{h_{1}(h_{1} + h_{2})}\right\}\right] T_{n,m-1} - \left\{\frac{h_{1} + h_{2}}{h_{1}h_{2}}\right\} T_{n,m} = 0 \tag{44}$$

or,

$$A_{n}T_{n+1,m+1} + B_{n}T_{n,m+1} + C_{n}T_{n-1,m+1} = D_{n},$$
 (45)

where

$$A_{n} = \frac{1}{(\Delta \eta)^{2}} + \frac{\alpha_{1}}{2\Delta \eta}$$

$$B_{n} = \frac{-2}{(\Delta \eta)^{2}} + \alpha_{2} \frac{h_{1} + 2h_{2}}{h_{2}(h_{1} + h_{2})}$$

$$C_{n} = \frac{1}{(\Delta \eta)^{2}} - \frac{\alpha_{1}}{2\Delta \eta}$$

$$D_{n} = \alpha_{2} \left\{ \frac{-h_{2}}{h_{1}(h_{1} + h_{2})} \right\} T_{n,m-1} + \left\{ \frac{h_{1} + h_{2}}{h_{1}h_{2}} \right\} T_{n,m} . \tag{46}$$

The total number, n , of n-stations must be odd. The bottom of the wake $(\eta \to -\infty)$ is defined by n = 1 while the top $(\eta \to +\infty)$ is defined by n = n . The wake center is defined by n = $(n \to -1)/2 + 1$. The boundary conditions can therefore be specified using the index n as

@ n = 1
$$T_{n,m+1} = 1$$

@ n = n_{mid} $f(\xi,0) + 2\xi \frac{\partial f}{\partial \xi}|_{(\xi,0)} = 0$ (47)
@ n = n_{max} $T_{n,m+1} = 1$.

Equation 45, when written in matrix form, becomes:

The solution procedure for this set of equations can be greatly simplified because the matrix is tridiagonal. If the matrix is denoted by A, then

$$A T = D . (49)$$

Now let

$$A = L X \tag{50}$$

where

$$L = \begin{bmatrix} \omega_1 & 0 & 0 & & & & & \\ \beta_2 & \omega_2 & 0 & & & & \\ 0 & \beta_3 & \omega_3 & & & & \\ & & \ddots & & & & \\ & & & \beta_{n-1} & \omega_{n-1} & 0 \\ & & & 0 & \beta_n & \omega_n \end{bmatrix}, \quad X = \begin{bmatrix} 1 & -E_1 & 0 & & & \\ 0 & 1 & -E_2 & & & \\ & & \ddots & & & \\ & & & 0 & 1 & -E_{n-1} \\ & & & 0 & 0 & 1 \end{bmatrix}$$

and

$$\mathsf{LX} = \begin{bmatrix} \omega_1 & -\omega_1 \mathsf{E}_1 & 0 & 0 & 0 & 0 \\ \beta_2 & (-\mathsf{E}_1 \beta_2 + \omega_2) & -\mathsf{E}_2 \omega_2 & 0 & 0 \\ 0 & \beta_3 & (-\mathsf{E}_2 \beta_3 + \omega_3) & -\mathsf{E}_3 \omega_3 & 0 \\ 0 & 0 & \beta_4 & (-\mathsf{E}_3 \beta_4 + \omega_4) & -\omega_4 \mathsf{E}_4 \\ & & & & & & & & & & & & & & & \\ & & & & & & & & & & & & & \\ & & & & & & & & & & & & & \\ & & & & & & & & & & & & \\ & & & & & & & & & & & \\ & & & & & & & & & & & \\ & & & & & & & & & & & \\ & & & & & & & & & & \\ & & & & & & & & & & \\ & & & & & & & & & & \\ & & & & & & & & & & \\ & & & & & & & & & \\ & & & & & & & & & \\ & & & & & & & & & \\ & & & & & & & & & \\ & & & & & & & & & \\ & & & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & &$$

Applying the above equations, a step by step procedure is used to evaluate the β 's, ω 's, and E's given the A_n 's, B_n 's, and C_n 's. From Equations 49 and 50 ;

$$LXT = D, (51)$$

and if

$$X T = e , (52)$$

then

$$Le = D, (53)$$

or .

If e_1 = 1 and E_1 = 0 then all the e's and E's are evaluated using the relations below

$$e_n = \frac{D_n - C_n e_{n-1}}{B_n + C_n E_{n-1}}$$
 and $E_n = \frac{-A_n}{B_n + C_n E_{n-1}}$. (54)

The matrix Equation 52 may now be written as

$$\begin{bmatrix} 1 & -E_1 & 0 & 0 & 0 & & & & & \\ 0 & 1 & -E_2 & 0 & & & & & \\ 0 & 0 & 1 & -E_3 & & & & & \\ & & & & \ddots & & & \\ & & & & 0 & 1 & -E_{n-1} \\ & & & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ \vdots \\ T_{n-1} \\ T_n \end{bmatrix} = \begin{bmatrix} e_1 \\ e_2 \\ e_3 \\ \vdots \\ e_{n-1} \\ e_n \end{bmatrix}$$

Starting with $T_{\rm n}$, the n values of T are obtained by using the recursive relation given below:

$$T_n = e_n + E_n T_{n+1}$$
 (55)

These T_n values represent the solution at the ξ station m + 1.

The general procedure given above may be summarized in the following manner:

- (1)
- The solution is assumed to be known at the station ξ_m for all n. An approximate solution, $T_{\mbox{old}}$ is assumed at the ξ_{m+1} station in order to evaluate the A_n 's, B_n 's, C_n 's, D_n 's, e_n 's, and E_n 's. (This approximate solution at station m+1 is usually taken to be the solution found for station m.)
- Using the computed values of e and ${\rm E}_{\rm n}$, the solution T $_{\rm new}$ is calculated using Equation 55.
- (4) Told and T are then compared to see if they are the same at every n station to within a certain accuracy; if not the T $_{\rm old}$ is set equal to T $_{\rm new}$ and steps (2) and (3) are repeated.
- This iteration procedure is continued until T_{old} and T_{new} are sufficiently close signaling a converged solution at the $\boldsymbol{\xi}$ station m+1. Usually, no more than two or three iterations are required.
- The procedure given in steps (1) through (5) is merely repeated for each subsequent downstream station.

As noted in (1) above, the finite difference technique requires that a solution be known at some ξ station in order to compute solutions downstream. While an actual velocity profile in the wing wake is not known in general, a profile shape can be found at the trailing edge of an airfoil on both the upper and lower surfaces whenever the flow over the airfoil is calculated. One method of finding the viscous solution over an airfoil is given in the 2-D Airfoil program of Reference 4. The flow is computed by solving the boundary layer flow over the airfoil with a momentum integral technique. Using the program output, the velocity profiles on both surfaces may be determined from their respective boundary layer thicknesses and form factors using the equations below:

$$\frac{u_{\underline{u}}}{U_{\underline{\omega}}} = (\frac{y}{\delta_{\underline{u}}})^{(H_{\underline{u}}-1)/2} \quad \text{and} \quad \frac{u_{\underline{k}}}{U_{\underline{\omega}}} = (\frac{y}{\delta_{\underline{k}}})^{(H_{\underline{k}}-1)/2}$$
 (56)

where

 δ = boundary layer thickness at the trailing edge H = turbulent form factor of the trailing edge u & l = subscripts denoting upper and lower surfaces.

Although Equations 56 do yield an initial velocity profile, there is still a problem due to the singular nature of the boundary layer equations at the airfoil trailing edge. From Equation 33, it is evident that n is unbounded at ξ = 0. Some procedure or technique must therefore be used to provide an initial profile downstream of the trailing edge. An investigation of the experimental

data given in Reference 26 and 27 indicated that at small distances downstream of the trailing edge, the velocity profile shape is still much the same as at the trailing edge. Based on this information, the assumption was made that the profile shape at a small distance downstream, say .01 chord lengths, is the same as the profile at the trailing edge. This technique was used to establish a profile at $\xi=.01$ in the WAKE program, and by assuming this profile satisfies the wake boundary layer equations, the initial requirements for the finite difference solution are satisfied. Although the program permits initial values other than .01 by requiring the value to be read into the program, this value was found to be satisfactory for all test cases presented in a later section of this report. Values of ξ less than .01 tended to make the maximum value of η too large, requiring an excessive number of steps in the η direction (Equation 33). For values larger than .01 the profile shape can no longer be approximated adequately by the trailing edge profile shape as seen from the experimental profiles.

Another problem which must be discussed arises from the fact that the boundary layer equation (Equation 35) contains no terms to account for pressure fluctuations in the y-direction. In the development of the boundary layer equations the pressure was assumed constant in the direction normal to the flow, eliminating the pressure gradient term. Far downstream this pressure variation is obviously small. Near the airfoil trailing edge, however, the deviations from freestream static pressure may be large. The fluctuations are virtually impossible to predict unless the complete Navier Stokes equations are solved which at the present time is an unrealistic task. The WAKE program was written with the pressure terms excluded with the hope that it would still match experimental data reasonably well. The results obtained indicated that these hopes were attained. Correlations with several test cases are given in the next section of this report.

The eddy viscosity model used in the WAKE program is that given by Equation 13 in the literature review. This model was derived by Prandtl for a fully-developed wake flow. In general, the velocity term in parentheses represents the difference between the maximum and minimum velocity in a profile while b represents the wake thickness or height at a velocity station halfway between the maximum and minimum velocity values. These parameters can be estimated given a velocity profile in a fully-developed wake, but if the initial profile is the trailing edge profile, then another set of parameters must be defined which will correlate with experimental measurement. It should be emphasized that while some experimental data exist for velocity profiles in the wakes of airfoils, these data must be described as very limited (Refs. 7, 26, 27, 28). Noting Figure 29, the velocity difference for the trailing edge profile would always be u since u is zero, while in the fully-developed profile it is never as large as u Also, the wake width at half-depth for the trailing edge profile is always smaller than the same width for a fully-developed wake.

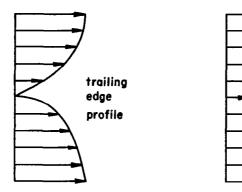


Figure 29. Sample velocity profiles at airfoil trailing edge and in a fully developed wake.

A value for the constant, c, in the eddy viscosity model must also be chosen which will bring about a match between experimental and theoretical data. In Equation 40 the eddy viscosity appears in the parameter c_1 as

$$c_1 = 100c_d + U_{\infty}/\epsilon$$
 where $\epsilon = bc(u_{max} - u_{min})$.

This may also be written in the following form

$$c_1 = 100c_d^{\dagger/\epsilon}$$
 where $\epsilon = bc(u_{max} - u_{min})/U_{\infty}$. (57)

fully developed

wake

For wakes considered in this report, the maximum velocity in the profile will be the outer edge velocity, U_{∞} . Then $\varepsilon = bc(1-\frac{u_{min}}{U})$. If c is defined as a positive constant, then the value of c_1 is obviously positive. By making several test runs of the WAKE program, it was found that at a given distance downstream of the initial profile the larger the value of c_1 , the lower the value of the centerline velocity and the smaller the wake width. Thus, it was necessary to find new definitions of the terms b and $(1-u_{min}/U_{\infty})$ to be used

with the trailing edge profile shape to evaluate ϵ . New definitions were sought which would, in general, produce the proper variation of ϵ with wing angle of attack without making the functional relationships more complex. As seen in Figure 29, in order to achieve approximately the same wake widths using these two profiles, the width of the trailing edge profile must be measured at a y station with a larger velocity. Using this new wake width, a relationship was sought between the term $(1-u_{\min}/U)$ and the profile drag coefficient. Based on a comparison of many computer runs of the WAKE program and their correlations with experimental profiles, it was found that (1) if b is defined as the wake width at the y station where the velocity is 75 percent of the freestream value, and (2) if u_{\min}/U_{∞} is represented by the expression $(1-c_{\min}/c_{\infty})$, then good agreement with downstream wake profiles is obtained.

Having defined new relationships for b and $(1-u_{\text{min}}/U_{\infty})$, the only remaining parameter needed to complete the definition of ϵ is the constant c. While the value of c for wakes behind circular cylinders using the conventional definitions of b and $(u_{\text{max}}-u_{\text{min}})$ is given as .047 in Reference 20, little has been published in the open literature regarding the value of c in airfoil wakes. For profiles generated using the WASH program with the new parameters defining the eddy viscosity, a constant value of c = .03 was found to work very well for all the airfoils tested. Although this value produces good correlation, the value of c is read into the WAKE program to allow the user the option of modifying the constant if he desires. The parameters b and $(1-c_{d})$ are also defined on cards FIN 51 and 52, respectively, in the program isting given in Appendix B. This permits the user to experiment with new ideas when more experimental data become available.

It is well to note here that a constant value of ϵ for all x locations is realistic only for relatively weak wakes, <u>i.e.</u>, $C_d \rightarrow 0$. ϵ is really a measure of the eddy size and intensity in the wake. In high drag situations, large eddies are shed. These have very large internal shears which cause them to disintegrate progressively into smaller eddies with smaller shears as one moves downstream. For such a situation a constant eddy viscosity is obviously not realistic. It will be noted, however, that the procedure for computing the boundary layer on the wing does not admit significant regions of separated flow. Since the wing drag is always relatively small when the boundary layers are attached and since the airfoil boundary layers are computed with constant eddy viscosities, it seems reasonable to continue this practice in the wake computations. As a result, however, the determination of the momentum defect must be limited to those cases where these conditions of unseparated flow and low drag are always satisfied: generally for section lift coefficients of 0.8 or less.

In order to carry out the numerical integration of the WASH program, the user must specify the grid spacing in both the ξ and η direction. The program is designed to use a maximum of 2001 points in the η direction or 1000 points

on each side of the centerline. The maximum values of η for the initial upper and lower profiles are computed using the boundary layer thickness δ in Equation 33:

$$(\eta_{\text{max}})$$
 = $\frac{\text{or}}{\text{lower}}$ (58)

or
lower

Dividing the larger of the two η values by 1000 yields the minimum stepsize in η . While the program is written for the general case (unequal stepsize) it is recommended that only even stepsize be used. If the specified even stepsize is too large, very small oscillations in u/U at the outer edge of the wake profile may result; hence, a stepsize which increases with η would only compound the oscillations. For every case presented in this report a stepsize of .00125 was found to be satisfactory. Using this stepsize and η_{max} from Equation 58, the number of points in the η direction may be computed from

NPTS =
$$2k_1 \eta_{max}/.00125 + 1$$

where NPTS is the total number of η stations for the entire wake and k_1 is a factor to insure that an η region is defined which is a little larger than the actual wake thickness at the initial station; k_1 should therefore have a value of 1.1 or 1.2. NPTS must be an odd integer. For the cases presented in this report it was usually specified as 1201, 1401, 1601, 1801, or 2001, depending on the maximum value of η . Since the value of NPTS is directly proportional to execution time it is suggested that less than 2001 points be used if possible; however, inexperienced users will probably want to choose one of the suggested values of NPTS given above depending on the value of η_{max} .

Along with an η stepsize, a stepsize must also be specified in the streamwise or ξ direction. For ξ an uneven stepsize which is very small initially and progressively larger downstream is recommended. The WAKE program is designed to use a stepsize which increases every step by the factor (1 + DXSTEP). If DXSTEP = 0 then equal step downstream will be taken. Unequal steps are suggested because the initial solutions are very sensitive to stepsize while downstream they are relatively insensitive. The user must specify both the initial stepsize DX and the stepsize increment DXSTEP. For most of the cases presented here, an initial stepsize in ξ of .00005 was used with DXSTEP = .05; thus, at every step the stepsize increased by 5 percent from its previous value. Using this stepsize and increment, approximately 150 steps

are required to traverse a distance of two chord lengths downstream ($\xi=2.0$). One disadvantage of the unequal stepsize is that if the solution is desired at $\xi=2.0$ it is very difficult to choose DX and DXSTEP so that one of the steps falls on this ξ station; the solution nearest the desired station must therefore be used. Figure 30 presents a list of downstream station number (NXPRNT in the WAKE program) and ξ distance for the different stepsize increments .05, .075, and .10 all starting with an initial stepsize of .00005. This data should be helpful in determining the station number at which a solution is printed as well as the total number of steps required downstream (NXSTEP in the program) to achieve a desired ξ distance.

The WAKE program consists of a mainline and five subroutines. The mainline (1) reads and prints the input data set, (2) calls subroutine PROFIL to obtain the initial profile at ξ = .01, (3) calls subroutine GETF to obtain a value of f (Equation 41) at the first ξ station downstream given the derivative f' or T, (4) calls subroutines ABCR, COEFF, and SOLVE to obtain a new value for the profile T at the ξ station, (5) compares the new profile with the last profile calculated at the ξ station to see if convergence is attained, and (6) after convergence, prints the solution and repeats the same procedure for the next downstream station. A listing of the WAKE program with user instructions, a sample data set, and sample output are given in Appendix B. The sample data set should be particularly valuable to the unfamiliar user in giving examples of stepsizes and possible print options.

	DISTANCE FR	OM TRAILING ED	GE IN CHCRDS		DISTANCE FR	OM TRAILING ED	GE IN CHORDS
REGMUN	DXSTEP#.05	DXSTEP=.075	DXSTEP=.01	STATION NUMBER	DXSTEP=.05	OXSTEP=.075	DXSTEP=.01
	0.010000	0.010000	0.010000	84	0.066374	0.278990	1.372710
2	0.010050	0.010050	0.010050	85	0.069242	0.299214	1.509031
3	0.010103	0.010104	0.010105	86	0.072254	0,320955	1.658985
4	0.010158	0.010162	0.010166	87	0.075417	0.344327	1.623933
5	0.010216	0.010224	0.010232	68	0.078738	0.369452	2.005376
6	0.010276	0.010290	0.010305	59	0.052225	0.396460	2.204964
7	0.010340	0.010362	0.010386	90 91	0.085886	0.425495	2,424510
8	0.010407	0.010439	0.010474	91	0.089730	0.456707	2.666011
10	0.010477 0.010551	0.010522	0.010572 0.010679	92	0.093767 0.098005	0.490260 0.526330	2.931662 3.223879
11	0.010629	0.010707	0.01077	94	0.102455	0.565104	3.545317
12	0.010710	0.010810	0.010927	95	0.107128	0.606787	3.898898
13	0.010796	0.010921	0.011069	96	0.112035	0.651596	4.287838
14	0.010886	0.011040	0.011226	97	0.117186	0.699766	4.715672
15	0.010980	0.011168	0.011399	98	0.122596	0.751546	5.186289
16	0.011079	0.011306	0.011589	99	0.128276	0.807215	5.703968
17	0.011183	0.011454	0.011797	100	0.134239	0.867056	6.273415
1.0	0.011292	0.011613	0.012027	101	0.140501	0.931385	6.899806
19	0.011407	0.011784	0.012260	102 103	0.147076	1.000539	7.588837
20 21	0.011527	0.011968	0.012556 0.012864	103	0.153980 0.161229	1.074879	8.346770 9.180498
52	0.011786	0.012378	0.013200	105	0.168841	1.240705	10.097597
23	0.011925	0.012606	0.013570	106	0.176833	1.333057	11.106407
24	0.012072	0.012851	0.013977	107	0.185224	1.432337	12.216098
25	0.012225	0.013115	0.014425	108	0.194035	1.539062	13.436757
26	0.012386	0.013399	0.014917	109	0.203287	1.653792	14,779463
27	0.012556	0.013704	0.015459	110	0.213002	1.777126	16.256482
26	0.012733	0.014032	0.016055	111	0.223202	1.909711	17.551150
29	0.012920	0.014384	0.016710	112	0.233912	2.052239	19.668348
30	0.013116	0.014763	0.017432	113	0.245157	2.205457	21.634232
31 32	0.013322	0.015170 0.015608	0.018225	114 115	0.256965	2.370166	23.796706
32	0.013536 0.013765	0.015008	0.019097 0.020057	116	0.269363 0.282382	2.547228 2.737571	26.175426 28.792019
34	0.014003	0.016584	0.021113	117	0.296051	2.942188	31.670271
35	0.014253	0.017128	0.022274	116	0.310403	3.162152	34.836348
36	0.014516	0.017713	0.023551	(19	0.325473	3.396614	38.319033
37	0.014792	0.018341	0.024956	120	0.341297	3.652810	42.149986
38	0.015081	0.019017	0.026502	121	0.357912	3.926071	46.364034
39	0.015365	0.019743	0.028202	122	0.375358	4.219826	50.999488
40	0.015705	0.020524	0.030072	123	0.393675	4.535613	56.098487
+1	0.016040	0.021363	0.032130	124	0.412909	4.875084	61.707385
42 43	0.016392 0.016762	0.022265	0.034393 0.036882	125 126	0.433105 0.454310	5.240015 5.632316	67.877174 74.663941
44	0.017150	0.023235	0.039620	127	0.476575	6.054040	82.129385
45	0.017557	0.025398	0.039620	128	0.499954	6,507393	90.341374
46	0.017985	0.026603	0.045945	129	0.524502	6.994748	99.374561
47	0.018434	0.027898	0.049590	130	0.550277	7.518654	*******
4.6	0.018906	0.029291	0.053599	131	0.577341	8.081853	*******
49	0.019401	0.030788	0.058009	132	0.605758	8.687292	*******
50	0.019921	0.032397	0.062859	133	0.635596	9,338138	*******
51	0.020467	0.034126	0.068195	134	0.666926	10.037799	********
52	0.021041	0.035986	0.074065	135	0.699822	10.789934	*******
53 54	0.021643	0.037985 0.040134	0.060521	1 36 1 37	0.734363 0.770631	11.598479	*******
55	0.022939	0.040134	0.087624	138	0.808713	13.402040	*******
56	0.923636	0.044927	0.104030	139	0.848698	14.406493	*******
57	0.024367	0.047597	0.113463	140	0.890683	15.486279	*******
56	0.025136	0.050466	0.123981	141	0.934767	16.647050	*******
59	0.025943	0.053551	0.135319	142	0.981056	17.894879	*******
60	0.026790	0.056868	0.147901	143	1.029659	19.236295	*******
61	0.027679	0.060433	0.161741	144	1.080691	20.678317	******
62	0.028613	0.064265	0.176965	145	1.134276	22.228491	*******
63 64	0.029594	0.068385	0.193711	146 147	1.190540	23.894928	*******
65	0.030623	0.072814	0.212133	148	1.249617	25.686348 27.612124	********
66	0.032840	0.082693	0.254685	149	1.376780	29.682333	*******
67	0.032040	0.088195	0.279204	150	1.445169	31.907808	********
68	0.035263	0.094110	0.306174	151	1.516977	34.300193	********
69	0.036595	0.100468	0.335842	152	1.592376	36.872008	*******
70	0.037978	0.107303	0.368476	153	1.671545	39.636709	*******
71	0.039426	0.114651	0.404373	154	1.754672	42.608762	*******
72	0.040948	0.122550	0.443861	155	1.841956	45.803719	*******
73	0.042545	0.131041	0.487297	156	1.933604	49.238298	*******
74 75	0.044222	0.140169	0.535077	157 158	2.029834	52.930470	******
		0.149982 0.160530	0.587634		2.130876	56.899555	********
76 77	0.047833 0.049774	0.160530	0.645448 0.709042	159 160	2.236970 2.348368	61.166322 65.753096	********
78	0.051813	0.171870	0.778997	161	2.465336	70.683878	********
79	0.053954	0.197165	0.855946	162	2.588153	75.984469	*******
80	0.056201	0.211252	0.940591	163	2.717111	81.682604	*******
8 t	0.058561	0.226396	1.033700	164	2.852516	87.808100	*******
82	0.061040	0.242676	1.136120	165	2.994692	94.393007	*******
83	0.063641	0.260177	1.248782	166	3.143977	*******	*******

Figure 30. Tabulation of downstream station number and ξ distance for stepsize increments of .05, .075, and .10.

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DISCUSSION OF PROGRAM RESULTS

Correlations of the WAKE program results with available experimental velocity profiles are presented in Figures 31 through 37. The figures show the experimental data, results obtained by the theoretical method of Reference 7, and the WAKE program results for specified stations downstream of the trailing edge. Each airfoil was analyzed using an initial x/c value of .01 and an eddy viscosity constant of .03. The profiles presented are not intended to show the relative distance of the profile above or below the trailing edge, but only the profile shape about the wake centerline as it moves downstream. In Figures 31 through 34 the WAKE program results are shown for two Reynolds numbers. In order to achieve a theoretical drag coefficient approximately equal to the experimental drag measured in References 26 and 27, it was necessary to run the two-dimensional airfoil program of Reference 4 at a Reynolds number of approximately half (.21 million) the indicated test value of .42 million. Tunnel turbulence or model surface conditions during the wind tunnel test may have produced more drag on the airfoil than would normally be expected at the test Reynolds number. The experimental drag was measured using a momentum rake which indicates the momentum defect in the wake at a station downstream of the trailing edge. Since the velocity profiles depend on drag coefficient, the calculated profiles should agree better with experiment if a theoretical drag coefficient is used which agrees with the experimental value. It was therefore decided to compute and compare profiles using both the specified test Reynolds number and a "corrected" Reynolds number, i.e., one at which the theoretical drag matches the experimental drag.

Figures 31 and 32 show that the WAKE program results agree well with experiment for the symmetrical Joukowski airfoil at both angles of attack (0° and 6°). While results at both Reynolds numbers show good agreement, that for the lower Reynolds number case is better. Although no experimental data were available at x/c = 2.0, the results are shown at this station for this and all other airfoils to give the reader an idea of the profile shape in the vicinity of the horizontal tail.

Figures 33 and 34 present program results for a symmetrical Piercy airfoil at angles of attack of 0° and 6°, respectively. The experimental points were taken from Reference 27. The WAKE program profiles give good agreement with experiment except near the minimum velocity region of the wake centerline. While the method of Reference 7 predicts the minimum velocity quite well, it over-predicts the wake thickness at other velocity stations in the profiles.

Experimental measurements of a modified 15 percent symmetrical airfoil at an angle of attack of 8° are presented in Reference 28, and these results are compared with the WAKE program prediction in Figure 35. Both the WAKE program and the method of Reference 7 predict the profile shape accurately as compared with experimental data except near the outer edge where the experimental data points appear questionable.

As a final test case the USA 45 airfoil was analyzed at angles of attack of - 5.3° and 1.6° and compared with experimental data presented in Reference 7. It should be pointed out that the profiles given in Reference 7 were not presented to make comparisons of this type, but rather only to give approximate dynamic pressure profile shapes in the general sense. The reader should bear this in mind when considering these two figures because the experimental profile shapes in Reference 7 have been greatly enlarged to make these comparisons. For the angle of attack - 5.3° the WAKE program did a better job of predicting the profile shape; however, for α = 1.6° the method of Reference 7 appears to match experiment better.

In general, agreement between the WAKE program profiles and experiment was good and, in most cases, better than the method of Reference 7. The minimum velocity at x/c stations near the trailing edge was generally larger than experiment while centerline velocities at stations greater than 1.0 were generally smaller than experimental values. The correlation of profile width using the WAKE program with experimental profile shape was excellent. The reasons the coefficients of the eddy viscosity were chosen to give a better fit to the experimental data further downstream of the wing rather than at the trailing edge were first that downstream is the region of major interest and second that a boundary-layer-type analysis obviously cannot describe the initial portion of a base flow wake adequately. Thus to favor a data match in a region where the analytical model is known to be inadequate is to lose the opportunity to attain a match in a region where it should be reasonably correct.

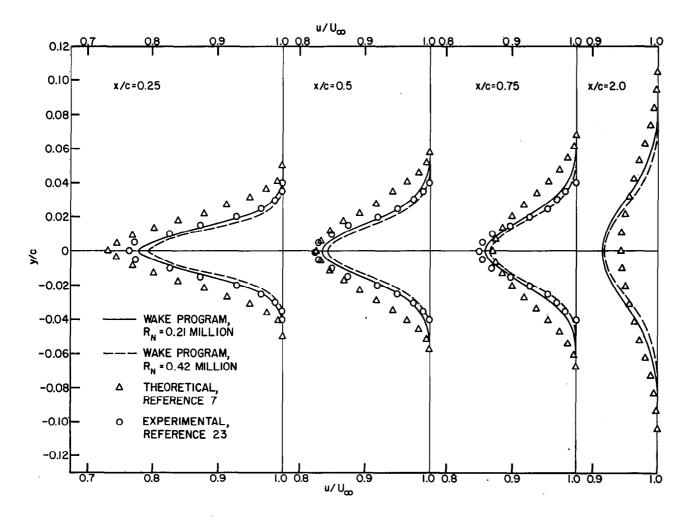


Figure 31. Comparison of velocity profiles with experiment (Ref. 26) for the Joukowski airfoil at α = 0°.

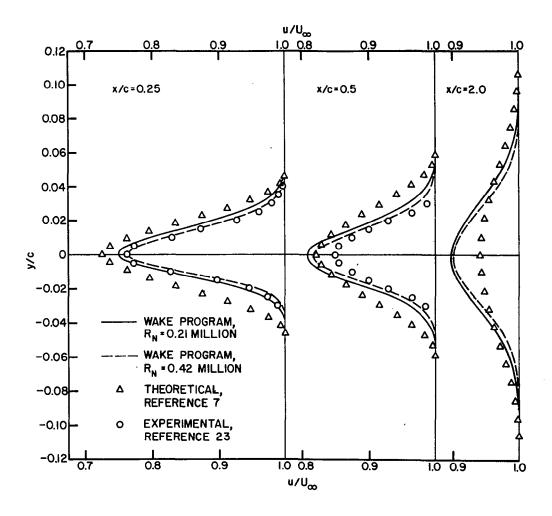


Figure 32. Comparison of velocity profiles with experiment (Ref. 26) for the Joukowski airfoil at $\alpha = 6^{\circ}$.

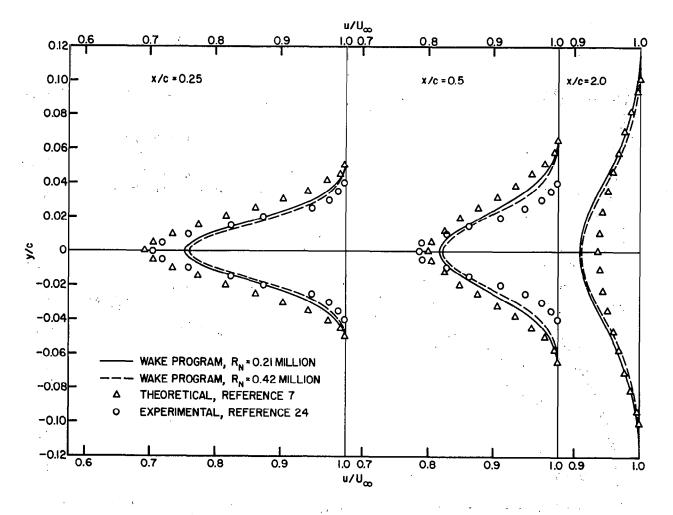


Figure 33. Comparison of velocity profiles with experiment (Ref. 27) for the Piercy airfoil at α = 0°.

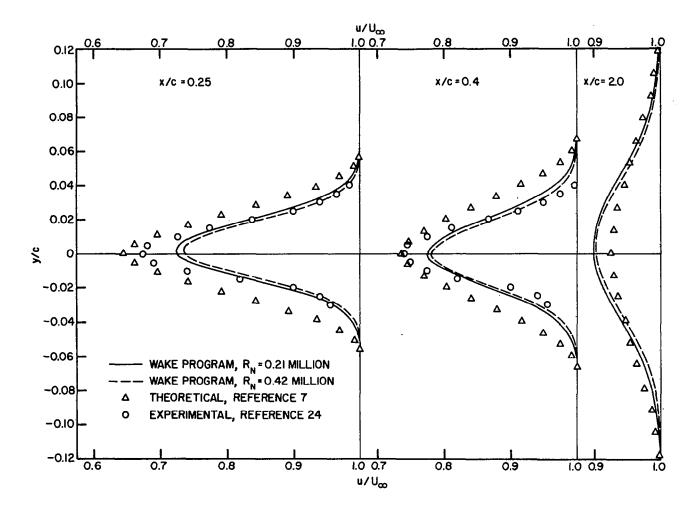


Figure 34. Comparison of velocity profiles with experiment (Ref. 27) for the Piercy airfoil at $\alpha = 6^{\circ}$.

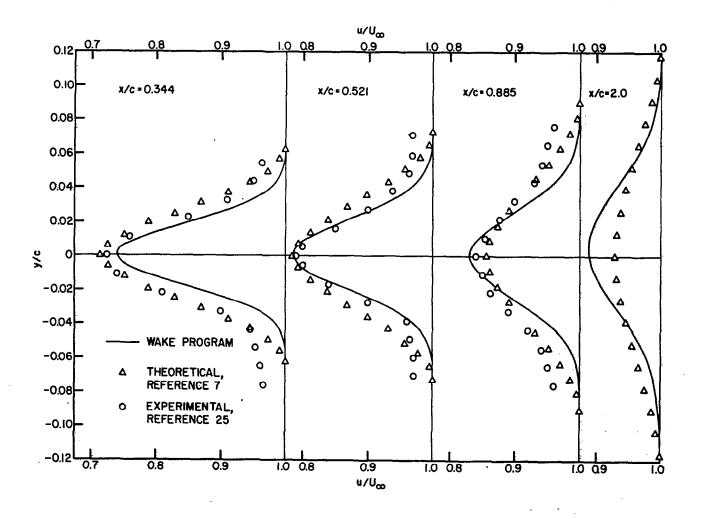


Figure 35. Comparison of velocity profiles with experiment (Ref. 28) for a modified 0015 airfoil at α = 8°.

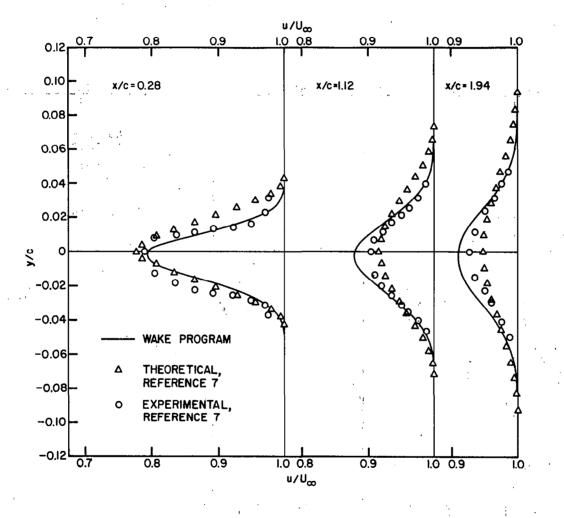


Figure 36. Comparison of velocity profiles with experiment (Ref. 7) for the USA 45 airfoil at α = -5.3°.

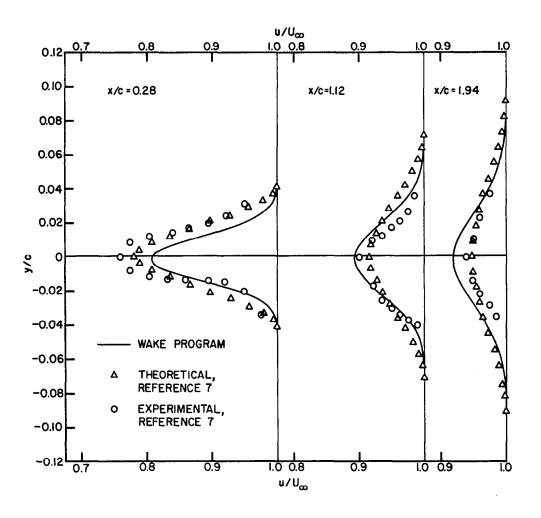


Figure 37. Comparison of velocity profiles with experiment (Ref. 7) for the USA 45 airfoil at α = 1.6°.

APPLICATION TO THE CALCULATION OF HORIZONTAL TAIL ONSET FLOW

In the preceding, the programs for determining the wake sheet location and the velocity profile in the wake have been discussed independently; consideration will now be given to combining them so as to compute the onset flow field at an aircraft's horizontal tail. The trailing vortex streamline locations are calculated using WASH. Naturally velocity profile solutions need be computed only along those streamlines which pass near the horizontal Given the section drag coefficient of the wing at the spanwise origin of each streamline used in the computation and the total streamline length to the x-station of interest, WAKE determines the velocity profile centered about the z-location of the wake sheet. The total distance traced by a streamline in going from the y-axis to some downstream x-station is given in the WASH program output in the section specifying the coordinates of the trailing vortex sheet. An example of how these are properly combined is presented in Figure 38 for the ATLIT wing at three stations downstream of the wing trailing edge in the wing plane of symmetry. The profile at the horizontal tail is therefore computed as the profile at the station x/c = 2.0 of Figure 38. Similar profiles may be calculated at other spanwise stations in order to show the spanwise variation of the profiles.

In the strictest sense profiles should be calculated along the 4 or 5 most inboard vortices to describe the spanwise variation of the onset flow at the horizontal tail. However, from a practical point of view unless the spanwise curvature of the wake is large there is, as may be seen in the wake sheet plots, little vertical variation in sheet location for y distance equal to normal tail semispan lengths. Also, a check of Figures 31 through 37 will indicate that at x/c = 2.0 the velocity profiles across the wake are very nearly the same for all airfoils tested, indicating that the effect of spanwise variations in section drag coefficient on the velocity profiles are small. As a result velocity profiles at different spanwise stations will usually have essentially the same velocity deficit. If the spanwise and downstream curvature is small for vortices which pass in the vicinity of the horizontal tail, it is therefore possible to execute only one case of each program and obtain the approximate wake position, flow angularity, and profile shape in the region of the horizontal tail (the most inboard vortex is used). This approximation can be improved if desired by applying the single WAKE program velocity profile to each of the desired spanwise vortex positions calculated in the WASH program. If a more rigorous analysis is desired, a boundary layer solution may be determined along each of the 4 or 5 most inboard streamlines noting the spanwise variation of section drag coefficient.

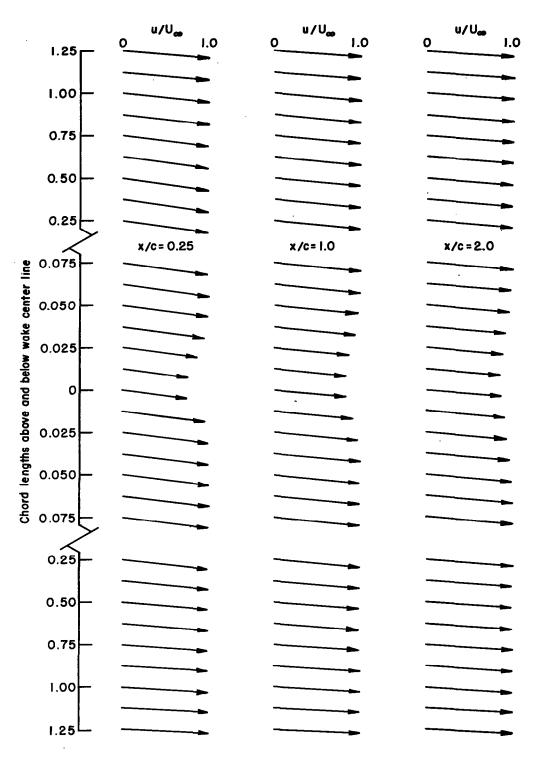


Figure 38. Velocity profiles with proper flow directions in the plane of symmetry behind the ATLIT wing.

With the profile shape in the tail region determined estimation of the forces on the tail plane due to the flow angularity and velocity variations can be undertaken. By executing the WASH program for a range of aircraft lift coefficients the wake position as a function of C_{\parallel} may be used to determine whether or not the tail ever passes through the wing wake.* If the tail always remains 10 to 20 percent of a wing chord length above or below the wake, the velocity deficit analysis may be neglected. Even if the tail is always out of the wake, the downwash computations are still important because the change in downwash at the tail with angle of attack must be known in order to predict tail trim angles and longitudinal stability. If the tail does pass through the wake, then the tail must be sized so that it produces the required control force even when the tail is located directly in the wake. The effect of spanwise variation in downwash may be accounted for by assuming it to be similar to a wing twist. While most light aircraft horizontal tails do not have twist, a twist variation can be assumed which will produce a spanwise angle of attack variation similar to that imposed by the downwash variation. This technique can be applied to the three-dimensional program given in Reference 4 when computing tail characteristics.

The determination of the proper flow velocity to use in calculating the aerodynamic characteristics of a section of the horizontal tail flying in a wake is complicated by the fact that the wake momentum defect is confined to a rather thin region which is on the order of the thickness of the airfoil for airfoils at low-to-moderate angles of attack. In this thin region the magnitude of the flow velocity may vary from 0.88 freestream to freestream. Since two-dimensional airfoil analysis has not yet progressed to the point of calculating aerodynamic coefficients in shear flow, it is necessary to find an average velocity squared over the thickness of the airfoil beginning at the point on the velocity profile intersected by a line parallel to the airfoil chord at t/2. This is best done graphically using plots of the $\frac{1}{2}\rho V^2$ distribution.

If the average $q=\frac{1}{2}\rho V^2$ varies significantly along the tailplane, its effects can be included in the three-dimensional aerodynamics calculation program (Ref. 4) in several ways: (1) artificially reduce the wing chord in proportion to $q_{|OCa|}/q_{\infty}$, (2) reduce only the local Reynolds number by the factor $V_{|OCa|}/V_{\infty}$ or some function thereof, and (3) multiply C_L and C_D by $q_{|OCa|}/q_{\infty}$. If these procedures result in significant changes in planform or aerodynamic properties, they cannot be accommodated readily within the framework of the 3-D characteristics program. However, if the changes are small enough to be capable of linear representation, then one of these procedures will serve nicely. Which procedure will yield the best result cannot be stated with certainty since time did not permit them to be investigated in detail. The author is inclined to favor the first as representing the least compromise with physical reality within the context of the two-dimensional airfoil analysis. Since the wake region is quite turbulent, it seems reasonable to insist that when the tailplane enters it, the analysis should consider the airfoil boundary layer fully turbulent from nose to trailing edge.

^{*} Although the analysis does not include the effects of the tail upwash on the wing downwash field, this distortion is not large. The wake position or magnitude is therefore not altered significantly.

CONCLUDING REMARKS

The present work provides two computer programs useful for predicting the flow magnitude and direction in the region where one would wish to locate an aircraft's horizontal tail (pitch trimming surface). The calculation of the contribution of this surface to the overall aircraft lift, drag, and moment is much enhanced if one has available more realistic values of the onset flow.

WASH ties together for the first time in a computer program a soundly-based inviscid method for determining the shape and location of the downwash wake sheet with a method previously used to determine the spanwise lift distribution for unswept moderate-to-high aspect ratio wings and wing bodies in incompressible flow. Excellent qualitative agreement is obtained with available experimental results. Quantitatively, the predicted flow directions at any point in the downwash field agree to within a degree or so of the measured values. Considering the experimental error present and the effects of boundary layers on the aft fuselage, this is about as good as one could expect. The results show there was little spanwise variation in wake position for normal horizontal tail semispans. Execution time for the program is 15-20 seconds on an IBM 370/165; it is thus a low cost means of mapping the downwash field during design analysis.

WAKE calculates the momentum defect downstream along the wake centerline. It uses as input section drag data developed analytically by the aforementioned spanwise lift distribution program. It provides velocities that are within 2 percent of the measured values at all stations for which data were available on two wings with different airfoil sections. Computation time for the flow along one streamline is 2 min 42 sec. The results indicate that the momentum defect due to wing drag is confined to a region no more than 0.43 m high for typical light aircraft in the cruise configuration. The region of noticeable defect (> 2 percent less than freestream) is only about 0.21 m high. There is little spanwise variation in wake velocity profile for typical light aircraft horizontal tail semispans. Thus, unless there is some compelling reason to locate the trim surface near the wake centerline, use of WAKE is not required.

The flight condition for which this type of information is of most interest is approach. In this configuration the wake is large and the momentum defect significant. While the inviscid downwash calculation as used here applies equally well, the viscous treatment suffers from the fact that the method used to determine the wing drag cannot accommodate separated flows. Further, flows with large separations can not be considered to possess constant eddy viscosities as was assumed here. It is apparent, therefore, that if horizontal onset flow is to be computed during approach the problems of the analytical determination of the correct aerodynamic characteristics of airfoils near stall and the characterization of turbulent flow eddy viscosity magnitude and decay rate in terms of the size of the initial separation must first be solved.

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APPENDICES

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APPENDIX A - WASH PROGRAM

User Instructions

The program is written in FORTRAN IV and is designed to run in double precision on an IBM 370-165 computer. This program evaluates (1) the location of the wake centerline by tracing the path of 18 vortices shed at the wing trailing edge, and (2) the total flow angle, sidewash angle, and downwash angle behind an unswept wing in any plane perpendicular to the wake centerline at a specified distance aft of the wing trailing edge or in the plane of symmetry of the wing. Downwash information in a single plane behind the wing using 15 downstream steps requires an average execution time of 20 to 25 seconds. The program requires the specification of the following input data:

<u>Card</u> Number	Variable Name	Variable Description
1	TITLE	The 80 character array which is used as a header to identify output. Termination of execution is achieved by following the last set of wing data to be analyzed by a title card having only the word END in the first three spaces.
2	NSTEP	The number of downstream steps to be taken aft of the wing trailing edge. The total distance the vortex system is traced downstream is given by NSTEP*DX. The maximum value of NSTEP is 18.
2	JPUNCH	The control variable giving the user the option of obtaining a punched plot data set which may be used to plot the vortex system using the PLOT program in Reference 4. JPUNCH=1 gives punched output while the default JPUNCH=0 gives none.
3 3 3 3 3	ALPHA B2 TR CR DX	The wing angle of attack in degrees. The wing semispan in feet. The wing taper ratio (tip chord/root chord). The wing root chord in feet. The step size in the streamwise direction specified as ratio of wing semispan.
4-5	Y	The 10 variable array specifying the Y-coordinates of the positive Y-axis (axis in the spanwise direction) at which the section lift coefficients are read. The order of specification is from positive wing tip to wing root as a ratio of wing semispan (from Y(1) at the tip to Y(10) at the root). All of the Y values <u>must be non-zero</u> .
6-7	CLS	The 10 variable array specifying the section lift coefficients corresponding to the Y-coordinates described above using the same ordering scheme.

<u>Card</u> Number	<u>Variable</u> <u>Name</u>	<u>Variable</u> <u>Description</u>
8	NXORY	The control variable used to specify the type of plane in which downwash calculations are made. NXORY=0 gives no downwash analysis in a plane. NXORY=1 gives downwash information in a Y-Z plane where X is the streamwise direction. The Y-Z plane is located at a value of X = STAT (see next variable). Downwash information is calculated for the 6 most inboard Y-stations at several Z locations. NXORY=2 gives downwash information in the X-Z plane at Y=0 for X values ranging from .25 to 1.75 semispans aft of the trailing edge. Z ranges from .5 semispans above and below a specified midpoint value of Z = STAT (see next variable). NXORY=3 gives downwash (or negative upwash) information in X-Z plane at Y=0 for negative values of X ranging from the. wing leading edge to5 semispans above to .25 semispans below the leading edge value of Z.
	STAT	Variable used with NXORY to specify in semispans the proper location of the plane of interest. If NXORY=1 then STAT specifies the X-station at which the Y-Z plane is to be located. This distance in semispans may be either positive or negative depending on whether downwash or upwash information is desired, but it must be measured from the wing trailing edge. If NXORY=2 then STAT specifies in semispans the midpoint of the Z-range for the downwash calculations in the X-Z plane. This Z-range is specified above (positive) or below (negative) the trailing edge in semispans. IF NXORY=3 the variable STAT is not used.
Last Ca	ird	Blank.

Cards 1 through 8 represent a complete data set for the WASH Program. Several data sets may be executed for a single program compile by placing subsequent data sets behind the first. More than one plane may be analyzed during a program execution by specifying new values for NXORY and STAT on other cards placed behind card eight and before the blank card.

The entire program execution is terminated when the END title card is encountered. The format specification for the above data is given in Figure A-1. A sample data set is given in Figure A-2, and the output of this data set is presented in Figure A-3.

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Figure A-1. Format specification of input data for the WASH program. \sim

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Y(1) Y(2) 987946 1987946 1987946 1987946 19885 19985 1	2811
Y(1) Y(2) 987946 - 1737577 - 1 กอการาคาธายาการการการการการการการการการการการการการ	2811 6 2 4 5 5 9 8 9 2 2 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
Y(1) Y(2)	2811 6 5 5 9 8 9 2 2 3 4 7 0 9 6 5 3 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6
Y(1) Y(2) 987946 17375271 101111111111111111111111111111111111	2811
Y(1) Y(2) 987946 17375271 101111111111111111111111111111111111	2811
Y(1) Y(2) 987946 - 1737577 - 1 กอการาคาธายาการการการการการการการการการการการการการ	2811

Figure A-2. Example data set for the WASH program.

Program Listing

•		200	_	0.18.51.18.17.1H1.18.8.110.18.4.110.1
•			•	(//
	EACH UP THE SMED WITHOUT SOURCES OF COUNTY OF	S	-	
				CARR SET UP 6 REDROTER TWE TO AND CLASS S
•		3	•	
•		2		#OBK!(!)AA(!)
•		I SP	•	35 #DF 2(1)=CLS())
		ĭ	•	00 40 1-1-10
•	_	ĭ	-	Y(1)=-#O#K1(1)
	THE COLT AT ALCONOMINED TO THE PROPERTY OF THE		=:	CI-1010880001010
	1746		·:	4
		į	: =	C.P(1010) 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
	DIMENSION WORKINGO, WORKER (2010-CLS (7010-CL20) - PO(3) - PI(1) - PI(1)	į	2	
	16 (20 to #583MT (4 - 13 1 - #98 (ATC 0 1 - 5 (4 - 20)		: :	
	DATA END/ANEND /	ï	-	90 45 111-10
	14640-1	ž	•	
	1 = 0.000 = 3	ž	•	C(114CRe(1.00+V(1)-V(1)eTR)
		E S	ę.	(11)=(11)
•		ĭ	~	GAM(1)=C(1)+CLS(1)/2.D0
- ;	S 46AD (IMEAD:10) (TITLE(1).1:1.20)	ž	25	•
Ĭ	TO STATE OF	I :	2	Coop BRINT CLS, CHERD, AND GAM , AREAT 10%
			::	##17E (1##17E,50) (1.711),CLS(1),C(1
	STORY OF THE STORY OF STREET		. :	SO FORMAT (//. SK. ZAMME DROEMED FULL - SPAN
	30 UNCH			TRADECTOR DRADECTOR DRADECTOR DRADECTOR OF A STATE OF A
				0.00 T. 100 T. 1
	AMAD CLEMAD NATION POST	ž		THE STATE OF SMITH STATE STATE SAID SAID
2			30	
•	ALPHAERING ANGLE OF ATTACK IN DEGREES	IS P		CANSAL DE GRACE - CANAL - CANA
•	ë	ž Ž	3.5	55 YGAMS(1)=(Y(1)+Y(1+1))/2.Do
•		Į,	11	COOD DRINT TRAILING VORTER GAMMA VALUES
•		I P	:	WAITE (IMPLIE, 60) (I.VGAMS(1), GAMS!!
•	CREENS BOOT CHORD LENGTH IN FRET	Ş	3	60 FIRMAT (//.IX. BPMLOCATIONS & STRFNS
	DESCRIPTIONS TO CALCULATE DOWNSTREAM VORTER LOCATIONS	ž	Ž ;	ITHE MEGATIVE V-ANSS./ZK, aSMCA MIRR
	CHROCHERS IN CRITICAL AND CONTROL OF THE CONTROL OF		<u>.</u>	LVE ANISTON OF THE PROPERTY OF THE PARTY OF
•	TOTAL STATEMENT OF THE			ISH.ZZHTIP VALUE (T-NEGATIVE),/,/(SX.
	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			1//301PA 100H01*NG*10*NG*10**10**10**
1	3 FORMAT (BF10.5)	ī	;	
•		HŞ.	•	C'LL SPLINE (NS.CAM.Y.AA)
	x4=-,7500eCxe0C0x(4L0)/62	ĭ	:	. write (tentil.65)
	/ Est. /500 0/700 05 1/4/4/ PJ/ ES	1	::	CANDO AD ALL BALLOSASSASSAS DA SOCIALISMOS DE CANDO DE CA
}	STATE CENTER AND ATTENDED TO SELECT OF SELECTION OF SELEC			
				10.1=2.00
~	A = .013.6.2%.7MDEGREFS./5%.9M62	E SH	:	VSPuvSP+.0500
	FT./5x.0Mfm = .015.6./5x.04Cm = .013.	2	÷	IF (YSP.GT.Y(1)) GO 10 70
	13.6.2x.emsemisPans./sx.enxs = .0	ĭ	ç	=
	013.c .2x, 945fml \$PAMS. /5x, 9445f		-	60 10 05
	TOTAL TRANSPORT OF THE PROPERTY OF THE PROPERT		25	70 IF (YSP.LT.V(20)) GO TO #5
•	AREA 2478 FROM +1 50 0 08 FROM POSITIVE RING TIP TO BING BOOT			
	#FAD (186AD-20) (V410-181-10)	ĭ		91 -1 -1 -0 00 54
•	_		•	
		45.	:	NO CONTINUE
	101.1		3.8	AS GAMMA-ICAGE, 110TSPOAMEZ, 1110VSPOAME
-	UES//.64.1M1.91 .MY[[].1]K.5MC	ĭ	ş	COOR PRINT SPLINED GAMMA WALUES FOR BOUND
	プログラン はいらん はっちゅう こうしゅう こう ゅう こうしゅう こうしゅう こうしゅう コープ さいかい こうしゅう こう こうしゅう こうしゅう こう こうしゅう こうしゅう こう	T S	3	WATTE TEMPTTE, 90) YSP. GAMMA

GENINO A SIN		1.013.4.5x.013.4.04.1M[./].5x.12.5x.013.4.51.013.4.5x.10+10.04	_
DENNER AND FE			250
2 PM WAY		TOTAL STREET STR	-
25 10 1.75			
		TO THE OWNER WINDS ON THE PROPERTY OF THE TOWNS	
A Sel A MGL P.S.		211111111111111111111111111111111111111	
CATON CHOSE		TO THE PERSON NAMED IN COLUMN	
F THE LEADING	o ISB	_	
	65 H 20	V(1)===000K1(1)	
		V1 (+10) 2 W GGR (+1+1)	NOM 71
(9), GAMI 20), GA		CLS(1) = #ORKP(1)	85H 72
V(31.21).XP(3	_		
	-		
31.102(3).1117		CONN. SET-UP CHORD VARIATION AS A FUNCTION OF BOOT CHORD C TAPER BATES	
	•	010111111111111111111111111111111111111	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
		(3)24(7)7	
	_	O - 67 - 13 - 13 - 13 - 13 - 13 - 13 - 13 - 1	
	W\$H 22		_
		Cook BRINT CLS. CHCRO. AND GAM ARRANION FOR SEMISPAN F.CM -1 TO 1	
		SPETE (1881TE.50) (1.v411.CL541).CL5411,CD0	
AILTHG EDGE		50 FORMAT (//.BE.ZewREGRDERED FULL-SPAN VALUES.//.SK.IMI.GK.aMVfII.I	120
		IN-OMCLECTIVE SHEAMCHING AND SHEAT S	į
		11. UE (Y-NEGATIVE)./.IRISH., 2.444K.DI 3.61.9K.IM ./1.5K.12.415K.DI 3.6	
DATA SET	E 2 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	-	
	•	CONTINUE GATE VALUES FOR THE VRAILING VORTICES C THE V STATIONS	
		TO A MARKET OF THE PARKET OF T	
05.00			
PROGRAMI		VALUE OF STATE OF STA	
44101	45H 34		
	85H 35	40 FIRMAT (//-IN- 674 OCATIONS C STRENGTHS OF THE 9 SHED VORTICES ON	
111045		ITME NEGATIVE V-ANIS-/	#\$H 46
		LVE ANIS) - / - 6x - 1 ME - 7x - 6MV GAMS(E) - 11x + 7MGAMS(1) - / 5x - 12 - 21 5x - 01 5x - 0x -	WSM 47
		194,22HTIP VALUE (V-NEGATIVE),/, P. (4x. 12.2.2 (5x, 013.6), 9x, 1H ,/).5x, 12	į
		-	
	_	CATALINE FIR FRE BECKNE VOMTER GARBAN	200
E .75 CHORD		CANADA CA	-
	84 m58	STATE CHESTING SAN	
	-	BS FORMAT 1//-1x-asmsPLINE FIT OF BOUND VOSTEX STRENGTHS VERSUS Y-//-	85H 104
		15K-IMV-15K SMCAMAD	
. 42.58.82.84.	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	STATE OF THE STATE	100
.BFF4./41.9462		-0.00 -0.00	
	_	TANK BELLACION OF THE TO	
	954 30		
PANS./SK. BM45T	-	_	=======================================
	-	PO IF (YSP-LT-V(20)) GO TO #5	45H 11.2
10 MIN. 8301	•	THE CASE OF A COURT AND A COURT OF THE COURT	
	,	De CLANCE DE LA CONTRACTOR DE LA CONTRAC	
	BSH SB		
MY111,111K,5MC	451 50		
	-		#5H 120

				181 HSA
8	1X.17.3.5X.115.6	121	72.42.74.74.74.74.74.74.74.74.74.74.74.74.74.	8SH 182
	THE TOWN THE FORM IN AT MADE VALUE OF THE TABLE AND TO BE A		60 10 138	
	FOGE VORTEX		120 P2(1)=P(KKH-1-LL)	_
	THE POSITIVE Y-AXIS THE NEGATIVE AXIS			-
:	SYMMETRY THE POSITIVE VALUES ARE ALSO		P2(3)=P(KKM-3-LL)	
:		WSH 127	60 TO 135	_
:	V(I, J,K)[#VORTEX INDEX(1-9) . J=COMPONENT [NDEX(1-3)(XYZ).			
***	_		Come SET LAST POINT AT X INFINITY	481 158
:	DEX(1-9) , Jacomponent Index(1-3)(XYZ),		P2(1)%100000±00	-
			02(2)=0K*2.L)	
:	STATION 1 IS AT THE GOUND VORTEX	251 132	72 (3. mg) - 1	
			44 - 44 - 44 - 44 - 44 - 44 - 44 - 44	
:	STATION 3 IS AT FIRST DUMMSTREAM STEP. ETC.			261 HSM
		1		961 HSR
			135 17 (4-67-9) 60 70 140	197 HSM
	0001110100			#SH 148
		984 139	GO TO 145	
001		041 HSM	140 GRE-GANS(KKR)	
		85H 141	Coos CALCULATE TRAILING VORTEX CONTRIBUTIONS	
	D(1.1.1) * XB		145 CALL BTRAIL(PI.P2.P0.GM.UU.VV.BW.B2)	202 HSB
	(NS(I)			207 150
	P(1.3.1)=28	Ser HSM		
	D([.1.23#d.0D0		おおとつ アンカルカー とうしょう とうしょう アンド・・・・・・・・・・・・・・・・・・・・・・・・・・・・・・・・・・・・	
	P([,2,2])#TGAMS([,			
2	P(I:35:2)=0:000			
			9 - 1 007 CC	#SH 209
	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		100 V(1.111-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1	WSH 210
	DELX=DX/2+00	161 HSM	Dysu1(2) 60x	
	DELY=V(I.2.J) ODELX		D2:41(3)+0X	4ST 212
	DELZ=V(1.3.J)+DELX		X(+(f*1*3)=b(f*1*3)+0)	
	IF (3,60.210EL 201AN(ALP)+00LX			#2H 21#
	PO(1)*P(1.1.1)+DELX		ZQ+(C+E+1)d#(FFF+E+1)d	
	P0(2)*P(1.2.J)+DELY			į
	P0(3)*P(1,3,1)+DELZ	121		
:	CALCULATE BOUND VORTEX CONTRIBUTION	121 121	100 CONTINUE	
	CALL #8(**0.00.******)	_	CONTINUE OF THE COORDINATES OF EACH VORTEX SHED FOR THE	MSH 220
				MSH 221
	AL(2)		MOD#NSTEP+1	WSH 222
•	LOOP OVER ALL 18 TRAILING VORTICES		DO 255 N=2.MDG	22 H 22 J
	00 155 Kal,18	WSH 164	Z-ERZEZ-	100 101
	X-61=X	101 HSM	TARESCEND GO TO 100	
	VORTEX CANNOT INDUCE VELOCITY ON ITSELF		TYS FORMAT (THIS TAN 95MCOGRDINATES FOR DOBNSTREAM SHED VORTICES ALONG	ISB
	1		I THE POSITIVE Y-AKIS (FROM MING ROOT TO MING TIP).//. 1X.87HS DE4OT	IS I
	17 T + 1	691 HS#		Z .
	IF (K.GY.9) GO TO 110		-	
	P1(1)*P(K*1,L)		061 01 05	152 HSA
	P1(2)=P(K,2,L)		130 MAITE (1881TE: 189) MAZ	222 128
	P1(3)*P(K+3+L)			454 PA
:		178	**************************************	
=	D(())#D(KKW.)*()			
	D1(2)=P(XXX:2+L)			
-	1F (L.EQ.J) GO TO 125			
	1F (K.GT.9) GD TO 120			
	P2(1)*P(K,1,LL)	WSH 180	60 TO 205	#2H 2+0

50			# C1 C2 (C-C3-Value) at	10E HSA
2	111111111111111111111111111111111111111		CONTRACTOR OF THE CONTRACTOR OF ANY	
200			CALL PLANE (STAT.MXDRY)	WSH 303
	ACCOUNTS OF THE PROPERTY OF TH	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	545	
2	1,1040,046,046,046			15H 30S
210	TO THE THE TAXABLE TO THE TOTAL TO THE TAXABLE TO T	#SH 246		306 HSI
	OLE FOREST AV LENGTH ON OTHER PROPERTY.	A W C H S H	-	70K HSM
:	GO TO 250	#SH 248	MI) =- YPL(MI)	MSH 308
220	MAITE (IMMITE, 225) (PPRINT(N).NH1.9)	84 249	DO 300 C*1;3	MSH 309
225	FORMAT (7X*1HY.9X.9(F9.6.3X))	WSH 250		
		WSH 251	KL=7-JL	MSH 311
230	WRITE (IMMITE.235) (PPRINT(N).N*1.9)	WSH 252		WSH 312
235	235 FORMAT (7X+1H2+9X+9(F9+6+3X))	WSH 253		ESH 383
	60 TO 250	WSH 254	KM)=DWASHX(KL+KM+L)	
240	240 BRITE (IBRITE,245) (PPRINT(N),N=1,9)	WSH 255	GD 10 330	WSH 315
245	FORMAT (TX=1HS:9X:9(F9:643X))	#SH 256	MPRINT(JL.KM)==DNASHX(KL.KM.L)	316
8	250 CONTINUE	MSH 257	CONTINUE	12 HSH
255	Ses Coarland	WSH 258	PRINT TOTAL FLOW ANGULAR DEVIATION, SIDEWASH, AND DOWNWASH FOR	MSH 316
946	BRITE (FURITE-250) (1111E-(1)-121-20) 240 EDBMAT (121-714, AZM ESTING OF BLOT DATA SET FOD SUFO VORTEY SYSTE		COSTS SPECIFICACIONES ALONG THE POSITIVE TOWN VAXISA ALIMONEM THE ME COSTS AND THE SECURITY VAXISA THE SECURITY OF THE SECURIT	120 HZW
3	IN. //. IX. 2014. //!	Ţ	THE BOXETIVE VARIANTED TO THE SECOND OF THE SECOND	MSH 421
	100//01/00/10/00/00 (D/O.1.1.1.180.200)	KSH 262	CO TO CARA, 464, 344, 1	12H 322
	TF (JPUNCH,NE-1) GO TO 275	WSH 263	[TLE: MML], MML=1,20),STAT	#SH 323
	WRITE (IPUNCH, 265) (TITLE(IP), IP=1,20)	WSH 264		MSH 324
265		WSH 285		828 HSA
***	PUNCH CONTROL INTEGERS FOR PLOT DATA SET	MSH 266		WSH 326
	MOGP=MD0-1	KSH 201	GO TO 365	#SH 327
		#SX 268	,	#SH 328
270		#SH 269	N FOR POSITIVE Y-AXIS AT THE X	926 HS#
	MATTER (FORCER, 500) (FORTH, 500) (FORTH, 500)	27.0	TATABLE OF TATABLE OF THE PROPERTY OF THE PROP	330
		1/2 1/2		100 000
613		WSH 273	H INFORMATION FOR POSITIVE Y-AXIS AT THE X	MSH 333
	MORKE (1) HD (0,3,1)	WSH 274		MSH 334
	DO 280 M#2,10	WSH 275		SH 335
		WSH 276	1H2.6X.5HANGLE.9X))	WSH 336
	#OFK1(N) H-P(NM.2.)	WSH 277	(11.1*4.(4).1*1.(6.1)	
280	#ORK2(W)=P(MM.3.J)	WSH 278	11(6(3x,F7.4,2x,F6,2,3x),/))	NSH 338
	DO 285 Mailtel8	WSH 279		MSH 339
	O-T027	WSH 280		WSH 340
;	FORK (A) H - F (RX - Z - Z - Z - Z - Z - Z - Z - Z - Z -	#SH 281		WSH 341
G B N		WSH 263	SECTIONARY CHRIVELY AND BENEFIT OF THE TOTAL CANDED AND THE PROPERTY OF A LAKES AND A TAME DEFENDED AND A VEG. /// "TX. 2019. ///)	245 H2W
	WORK2(19) #P(9,3,J)	MSH 284		WSH 344
	WRITE (IMMITE, 290)	WSH 285	12:12	
230	FORMAT (10x)	4SH 286		
	##	107 151	MANITURE CLARITOR CONTRACTOR OF THE CONTRACTOR O	
,	BRITE (188110.295) (BORRZILM:19)	007 158	SASS PLEMBAL CONTINUES AND A TOTO CARACTOS AND ANTICOMES AND AND ANTICOMES AND ANTICOM	200
2	TOTAL	1SH 290		
		162 HSA	WRITE (IMRITE, 405)	MSH 351
	WRITE (IPUNCH.300) (WORK2(LM),LM=1,19)	262 HSM	405 FORMAT (//)	WSH 352
300	FORMAT (10F7.4)			NSH 353
305		#5H 294		400 HS
	READ CONTROL VARIABLE SPECIFYING DOWNWASH PLANE INFORMATION	262 HSM		250 HSB
	DESIRED, WADRYS! VIELDS INFORMATION IN THE PLANE XESTAL.	200 HSH	_	OCC TOP
	NXONYES TIELDS INTOXAMILIA IN THE THE PLANE BENIED THE MINE. NXONYES TIELDS INTOXAMILE IN THE YEAR PLANE AHEAD OF THE MINE.		#XILE (!#X!IL*#ZC) (ZPELLC)*(D#XSULC)*(!#ZD*51)*(!#ZD*C)*(**********************************	NSH 158
310	310 READ (IREAD, 315) NXCRY, STAT	WSH 299	GO TO 310	620
315	315 FORMAT (110.F10.5)	WSH 300	425 MRITE (IWRITE, 430) (TITLE(MML).MML=1.20)	09E HSA

	DN AA(4,20),H(20),G(20),U(20),X(20),Y(20)	• • • • • • • • • • • • • • • • • • • •	AA(2.1)=0.5000(XPauu-Xxaup)/HH	SPL 78	
	TAN THE TANK	2 6	Apr. do	7.6	
٠	**************************************		**************************************		
•	M(1)#4(1+1)-4(1)				
	END CONDITION THAT ALEVIATES THE NEED				
*	RIVATIVE OF Y AT POINT 1	53			
	1.000/32.000	40	20 YY#YP		
	HI=H(1) SPL		RETURN	Se 148	
	H2=H(2) SPL		GND	SPL 86	
		27			
	U(1)#(1)#(32*0D0#N +42*0D0#HZ421*0D0#H3)/(H1+H2)/(H1+H2+H3)-4(5)# SbC				
	0° 17 • 18 • 000 ° 11) • 18 • 6° 1 Å• 28 / 48 88) / 68 88 80 ° 12 • 21				
	.{H}+HZ /HZ/HJ-A{4}#H *{ opd*H +Z .opo*HZ}/{HZ+H3}/(H	R ;	SUBROUTINE PLANE STAT. NXGRY)	٠. ا ۲	
	Take the second			,	
	TIP BY ALGENITHEN GIVEN BY AMERICA	ž :			
		77	DICTERED ANGELTO TON ACCALLYO THANKS AT ANY DEBASTAN AND TO THE STATES OF THE STATES O		
		, #			
		36	L		
	23.481	37	MOST INDOARD V-CODDOTNATES OF THE SHED VODICES, THE	4 0	
		36	4.25 Tn		
		39 Cess	Ä	-	
	(AH+HH)/(HH-(AA-AA)/HH/(AA-AA)	***	FOR THE SPECIFIED X=STAT PLANE. NXOPY±2 CALCULATES DOWNASH ANGLES	11	
	C=0"2D00+HH/(HH+HH) ShL	7	ON THE POSITIVE X-AXIS FROM X=.25 TO X=1.75 SEMISPANS IN THE Y=0	PLA 12	
		42	PLANE. Z RANGES FROM STAT+.5 TO STAT5 IN STEPS OF .05 WHERE		
	000-1-0	5	STAT IS SPECIFIED AS THE MIDPOINT OF THE 2-RANGE DESIRED.		
		:	NXGRY=3 CALCULATES THE UPWASH (NEGATIVE DOWNWASH) ANGLES ON THE		
	(D-AtU(I-1)1/p	£ ;	NEGATIVE X-AXIS FROM X=X-LEADING EDGE TO X=.5 SEMISPANS AMEAD OF		
		94	THE LEADING EDGE IN THE YES PLANE, Z RANGES FROM . 25 SEMISPANS		
	110	::	ADDRESS OF THE STATE OF THE PROPERTY OF THE PR		
2	CARA				
	MODIFIED RIGHT HAND END CONDITION THAT ALEVIATES THE NEED		CURTON ALPOCLOCUSES:TROCROXBOLDSANGESCOS,V(20).VGAMS(9).GAM(20).GA	P	
,	TO SPECIFF THE A-DERIVED OF A POINT A		11 1 × VPL(61 2 VPL(6 11 1 2 VPL) 12 13 10 VPL V NSTEP		
		-	DIMENSION PO(3), P2(3)		
	Tas Caragraph	53	CRAD=57-29577951b0		
	=	ă.	IF (NXORY.E0.2) GO TO 70		
	TAS INTERNATIONAL PROPERTY OF THE PROPERTY OF	55	JF (NXORY.EQ.3) GO TO 105		
		26	CALCULATE INFORMATION FOR PLANE AT X=CONSTANT FOR THE 6 MOST		
			INBOARD SHED VORTICES (1=4.9)		
	H2)/H2/H3-V(NH1-2)+H1+(11.000+H1+21.000+H2)/(H2		NX={STAT+.0001D0}/Dx+2		
	1+H3)/(H1+H2+H3)/H3		IF (SYAT-LT.0.00)NX=1		
		99	1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		
į	TAGE TO A THE TENT OF THE TENT OF THE TENT OF THE TOTAL THE TENT OF THE TENT O		(AN'E') OH(G'F) OL	7 Y	
	MICH TO ECEN AND ATCHES IN THE UCEN.	-	00 5 KI=1.5		
	DO 15 Jan 18 18		ZPL(M.6+K!)=ZPL(M.6+K!-1)0500		
		65	5 ZPL(4.6-XI)=ZPL(4.6-XI+1)+.0500		
5	(I) =0(I) +0(I+2) +n(I)	99			
	FORM THE AA(J. 1) COEFFICIENTS FOR THE CONVENTIONAL FORM OF		P0(1)*P(1,1,NX)	PLA 38	
	A CUBIC POLYNOMIAL FROM THE U(1)		IF (STAT.LT.0.D0)P0(1)=STAT		
			YPL(M) =P([.2.NX]	PLA 40	
		2;	PO(2)=YAL(A)		
	JdS (1)		00 (3) = ZD (W, J)		
		7.5	CALL MEGINO.MANNIC.MANNIC.MANNIC.		
	114120100	•			
			IF (1,60 ×) GD TD 55		
	ToS (2) Market	7.6			
	-(UP-UU)/HH/6.0D0		נובריו	7.	

0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	4	CASS OF STATE STATE AND AND STATE OF STATE	
(7) (2) (1) (1)		DO 45 L*1. NS (EP	
			4
		1(1)=0(K-10-1)	
		PI (2)=P(x, 2, L)	
		1	
		FF (Ledanstep) GO TO 85	
15 IT (L'EGUNSTER) GO TO 25		52(1) 20(K-1) (T)	
			1 4 1 d
P2(2) #P(K-2-11)		06 04 09	
D2(3) 40(5)		Bay 0.20000111000001001	
60 10 35			PLA 122
20 P2(1)=P(KM1,1,LL)		P2(3) HP(K, 3, L)	PLA 123
P2(2)=-P(KMI+2+LL)	PLA 64	90 GM=GAMS(K)	
. P2(3)=P(KM1,3,LL)			
GO TO 35			PLA 126
25 JF (K.67.9) GO TO 30			PLA 127
P2(1)=1000000*D0	P. 68	100 DEASHY (1.1) = -DATAN(EASHE)*CRAD	PLA 126
(100 ex) 101 (100 c)		RETORNA	A 10
		CARLOLLAND TO THE TANK THE MENTINE ALAND TO THE TANK THE	
30 p24 = 100000 = 00			
		00 110 1=2.11	PLA 133
P2(3)=P(KM1,3,L)		XPL(1)=XPL(1-1)=.05D0	PLA 134
35 IF (K.GT.9) GD TD 40		110 2PLL(1)*ZPLL([-1)05D0	
GM=GAMS(K)		PO(2)=0.D0	P. A 136
60 70 45		DG 130 [m1,1]	
			PLA 138
		11.411.00	
ベスキカよりを担じています。		CELORE CANADA CONTRACTOR CONTRACT	PLA 141
		00 125 K*1.9	PLA 142
50 CONTINUE		00 125 L*1.NSTEP	PLA 143
55 CONTINUE		LL=L+1	PLA 144
		ם (ו) = (אין יך)	PLA 145
		P1(2) #P(K,2,L)	
IN THE PLANE XMCONSTANT	P. A 97		PLA 147
Coest Darkota (March Landers Anders Anders and Company)		Carled Andreas	* ·
DESCRIPTION OF THE PROPERTY OF		741-1411/5	
DESCRIPTION OF THE PROPERTY OF		P2(U) mp(K) mp(K)	PLA 151
DEPORT (F. J. U) I - DATAN(BASIX) SCHOOL		60 10 120	PLA 152
60 CONTINUE		115 P2(1)=100000,D0	
AS CONTINUE		D2(2)#P(K.2.L)	
	4,6		PLA 195
Come CALCULATE INFORMATION FOR THE POSITIVE X-AXIS IN THE YEA PLANE		I SO GHEGANSKY	
0002-11-12-01-01-01-01-01-01-01-01-01-01-01-01-01-			4 10
TO TO TAKE A TOTAL OF THE		######################################	
	_		PLA 160
00 00 [±2,2]		_	PLA 161
60 ZPLL(1)=ZPLL(1-1)05D0	-	RETURN	PLA 162
p0(2}=0.00		G.A.O.	PLA 163
DO 100 (=1,31			
	PLA 105		
001 100 001 00			
・ 第二)とするトニンとは、カース・ロンド・コンド・コンド・コンド・コンド・コンド・コンド・コンド・コンド・コンド・コ			

Sample Output

```
THPUT SENT-SPAN VALUES
                                                                                                     CLSII)
0.4888700 80
0.4103800 60
0.103800 01
0.1208400 01
0.1208400 01
0.130800 01
0.130800 01
0.130800 01
                                                                                                                                                               TEP VALUE (Y-POSITIVE)
                                                                                                                                                                 ROOT VALUE
      REGROERED FULL-SPAN VALUES
                                                                                                                                                                  C(11)
0.261400 01
0.2707280 01
0.2707280 01
0.2750950 01
0.3953610 01
0.3953610 01
0.3953620 01
0.4960220 01
0.4960220 01
0.4960230 01
0.4960230 01
0.4960230 01
0.4960300 01
0.4960300 01
0.3953620 01
0.3953620 01
0.3953620 01
0.3953620 01
0.3953620 01
0.3953620 01
0.3953620 01
0.3953620 01
0.3953620 01
0.3953620 01
0.3953620 01
LOCATIONS & STRENGTRS OF THE 9 SHED VORTICES ON THE HEGATIVE Y-AXIS
(A MIRROR IMAGE IS ASSUMED FOR POSITIVE AXIS)
                                    (A MIRROR HAGE
YGAMS[]
-0.970170 00
-0.9227350 00
-0.7533850 00
-0.753850 00
-0.753850 00
-0.538900 00
-0.538900 00
-0.4032850 00
-0.2685520 00
-0.1471070 00
                                                                                                  GAMS(1)
-0.4629740 00
-0.7449120 00
-0.2751500 00
-0.2751140 00
-0.2751940 00
-0.2751940 00
-0.3133190 00
-0.3133190 00
                                                                                                                                                                  TIP VALUE (Y-NEGATIVE)
                                                                                                                                                                 ROOF VALUE
SPLINE FLT OF ROUND VORTEX STRENGTHS VERSUS Y
```

Figure A-3. Sample output of WASH program.

COMPUTATES FOR DOWNSTREAM SHED VORTICES ALONG THE POSITIVE Y-AXIS (FROM WING ROOT TO WING TIP)

TRAILING SDOF	0.7	3.3	0.0	2.0	0.0	0.0	0.0	0.0	0.0
į.	0.147367	0.258552	0.403245	0.534944	0.656672	0.763535	0.953186	0.922736	0.970017
7	0.7	0.0	0.0	0.0	0.0	2.0	0.0	3.7	3.0
5	0.0	0.0	2.9	0.0	0.0	0.0	0.0	0.0	0.0
STEP 1									
*	0.200000	0.200000	0.200000	0.200000	0.658315	0.200000	0.200330	0.200000	0.200000
;	-2.127234	-1.023312	-0.019655	-7.017309 0.200751	-0.015431	-0.013981	-9.312585 0.200426	-3.303525	7.312445
•	0.202126	0.201356	0.200969	0.200751	-0.015431 0.200599	0.200499	0.200426	-3.303525 0.201291	7.312445 0.200433
STEP ?									
1111	C. 4 00 00 0	0.400900	0.400900	0-400000	0.400000	0.400000	0.400300	0.400000	0.400000
*	0.144616	0.269947	0.404709	0.536662	0.655742	7.767101 -7.024376	0.859515	0.916950	0.967587
,	-7.957379	-0.040498	-0.034114	-0.029554	-0.026691 0.400917	0.400772	-3.322171	-7.718187	0.00001
STEP 1	0.00000	2.500000	0.400000	0.600000	0.500000	0.600000	0.600202	0.501020	0.600000
÷	0.149547	0.270422	0.405113	0.5371 03	0.659492	3.769569	2.557132	0.949679	3.955749
,	-0.073179	-0.256727	-0.046414	0.040490	-0.016129	-0.013330	-3.329397	-^.2(1197	7.235423
5	0.404541	0.602715	0.401867	0.601429	0.631141	7.400963	0.500140	0.400858	n.601561
STED 4									
×	0.15073)	0.900000	0.800000	0.800000	0.800000	3.800000 0.770\$55	0.900000	0.900000	0.800000
;	-0.792735	-2.270399	-0.057618	-0.050066	-0.044579	-2.040559	-2.035346	-0.007092	\$-94999
5	0.805500	0.903217	0.802141	0-801655	0.801322	9.601115	0.800797	0.401436	0.802145
STEP 5									
×	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000	1.903300	1.000000
7	0.152177	0.271375	0.405905	0.539268	0.661466	0.777950	3.975???	0.771991	0.977673
ś	1.006385	1.073572	1.002460	1-001959	1.001477	1.001245	1.731151	1.002170	1.002622
STEP A	1.200000	1.200000	1.200000	1.200000	1.200000	1.200000	1.200000	1.202000	1.200000
÷	7.(53593	0.271851	2.406126	0.538974	0.652759	0.775335	3.397521	0.975252	0.915999
7	-9.129744	-0.795924	-0.078292	-0.067541	-0.059753	-0.053533	-3.34?199	7.728519	7.039746
s	1.207221	1.204097	1.202716	1+202042	1.201617	1.201161	1.201146	1.202972	1.207973
STEP 7									
×	1.407000	1.400000	1.40000	1.400000	1.400000	1.400000	1.400700	1.497000	1.400000
,	0.155847 -0.147544	0.272409	0.406769	0.519768 -0.075763	0.664262	0.779407	0.977775 -0.043146	0.077455	0.905395
į.	1.408022	1.404502	1.402955	1.402212	1.401746	1.401475	1.401505	1.493753	1.403226
STEP 4									
\$1 P.D. 4	1.500000	1.600000	1.600000	1.600000	1.600000	1.600000	1.600000	1.600000	1.600000
*	C-1580A3	0.272956	0.407232	0 - 5 4 0 5 4 7	0.665976	0.791597	0.775551	0.965129 0.757812	0.878281
,	-0.164983	-0.172131	1.601109	-0.083746 1.602374	-0.073495 1.671966	-9.064525 1.631589	-0.041755 1.601762	1.504504	1.603425
,	11.00.101	1.50.4542	1.001109	1402174	1.071.100	1.031309	14401402	14404544	1.00,473
STEP 9		1.400000				1.500000		1.502020	1.800000
*	1.400000	0.273527	0.407714	1.800007	1.400000	2.799107	1.800000	0.954674	1.800000
,	-0.182398	-0.134426	-0.177122	-0.091530	-0.079966	-3.059197	-0-017164	3.771131	3.028975
5	1.809539	1.905271	1.903410	1.402527	1.801950	1.801707	1.902414	1.505223	1.907559
STEP 19									
×	2.000000	5.000000	2.000000	5.000000	2.000000	2.000000	5-000000	2.000000	2.000000
7	0.163236	0.274112	0.405216	9.542563	0.670026	0.793921 -3.073870	0.313721	0.941952	0.445498
•	2.010263	2.005640	2.003025	2.002675	2.002044	2.001977	2.007756	2.101913	7.003725
5TCP 11	2.200000	2.200000	2.200000	2.200000	2.200710	2.200000	2.200300	2.200000	2.200000
*	0.1 ^^ 45	3.274713	0.405736	0.541799	9.672364	0,400197	3.741?73	910156.6	0.841267
,	-0.215441 2.210266	-7.159563 2.206900	-9.125513 2.203834	-0.106597 2.202817	-0.092216	-0.077959	-0.017997	0.099572	2.01974B
-	2421038h	×.2.10000	2.20 10.34	21202417	217.72145	********	2.203559	217.0374	×+ ×11 15 40
STED 12			2.400000			2.400000			2.400000
ž.	2.400000 0.169370	2.400000	0.409271	2.400000 0.545917	2.40030n 0.674994	0.437259	2.400700	0.91?428 2.400000	2.878704
7	-7.2316AR	-0.170441	-9.134527	-0.113912	-0.094530	-1.041568	-0.001930	0.095047	0.013907
•	2.411650	2.496353	2.404035	2.402954	2.402293	2.492132	2.404197	2.437224	>.4039>3
STED 13									
×	2.600000	5.600000	2.600000	2.600000	2.600000	2.600000	5.600330	2.500000	5.600000
,	7.172749 -7.247659	7.775945 -7.192296	9.409827	0.546115 -0.121097	0.677536	0.815167 -0.094974	0.952720	0.495751	0.978423 0.99412
5	2.612316	2.606700	2.604277	2-603097	\$-605340	2.632715	2,534935	2.107955	2.603971
4150 14 X	2,900000	2.900000	8+600000	2.800000	2.600000	7.800000	2.400300	2.412200	7.900000
Y	0.175437	2.276567	0.410395	0.547689	0.680549	7. 423449	0.9531 99	2.991215	3.477564
7	-r.267755 2.417964	-0.193964	-9.152239 2.504432	-0.128144	-2.109362	-9.087909 2.832525	0.02775#	9.197719 2.135477	0.006066 7.904003
•	20-12484	2.897041	5. 00ee 35	2.803216	2.802485	7, 777525	2.935179	2,131471	2.504002
515P 15									
ž	3.000000	7.2277197	3.007700	7-000000	3.007000 0.663636	3.700500 0.411185	0.000700	3.777777	7.000000 7.991755
,	-0.274775	-0.205426	-0-100948	-0+135066	-0.114205	-2.090761	0.043554	0-095233	0.004191
8	3-013595	3.007375	3.004622	1-003341	3.002577	3.722764	3. 2251 24	1.000079	1.994025
5T=P 16									
11-5 10	7.700000	3.200000	3.200000	3-200000	1-200000	1-200000	3.203100	1,200000	1.200000
Y	7.184417	0,277900	2-411571	3.200000	0.665896	0.843560	0.944177	0.451222	0.465150
,	-0.293916 3.214209	-0.216490 3.207705	-0.169565 1,704809	-0.141550 3.201453	-0.119253 1.202655	-0-091588	0.059554	n. 027408	9.003954 1.204751
	34.14604	102377113		20 1451	********	31-33724	30033111	********	
5TEP 17									
Ť	7-400000	7.400000 2.275195	3.400000	3.400000 0.552266	3.400000 C.690335	1.477700 0.454275	3.423333	3.403300 0.437575	1.400000 0.885824
,	-7.308777	-0.224252	0.412179 -0.179090	-0.148527	-0.124010	-0.092237	3.372262	7.043479	2.005416
4	1.414508	1.479029	1.404991	1.403530	3.402751	1.473315	3-407431	1.417241	1.494093
\$750 14									
×	1.500012	3.600000	1.00000	3.600000	3.600000	1.620200	3.600000	3.600000	3.677207
ž	0.191302 -0.323354	7.779977 -0.239546	2.4(2902 -0.186529	0 • 55 395 1 -0 • 155070	-0.128533	0.805350 -0.091557	0.924412	0.425500	0.008557
Ś	3.015390	3.408347	1.005170	3.603694	1.602835	3.623673	3.50AL 21	3.513785	1.604148

Figure A-3. Continued.

	FOIL CL#1.	221. 372-	19.45 DA1	A FOR ATLE	•				
0.0 2.0000	0.2000	0.4000 2.4000	0.6000	0.8090 2.8000	1.0000 3.0000	1.2000	1.4000	1.6000	1.0000
0.0	0.1474	0.2686	0.4032	0.5349	0.6566	0.7636	0.8534	0.9227	0.9700
0.9227	0.6534	0.7638	0.6566	0.5349	0.4032	0.2686	0.1474	0.0	3.6
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
0.0	0.1479	0.2694	0.4042	0.5360	0.6560	0.7659	0.8569	0.9293	3.9743
0.9293	0.8569	0.7659	0.6580	0.5360	0.4042 -0.0154	0.2694	0.1479 -0.0126	0.0 -0.7085	3.0124
0.0292	-0.0292 -0.0126	-0.0233 -0.0140	-0.0197 -0.0154	-0.0173	-0.0197	-0.0233	-0.0292	-0.0545	
0.0	0.1486	0.2699	0.4047	0.5366	0.6587	0.7671	0.8596	0.9369	3.9576
0.9769	0.6596	0.7671	0.6567	0.5366	0.4047	0.2699	0.1456	-0.0141	2.0252
0.0524	-0.0524	-0.0409	-0.0341	-0.0399	-0.0267 -0.0341	-0.0244	-0.0524	-3.0524	3.0232
	0-1495	0.2704	0.4051	0.5371	0.6595	0.7686	0.8634	0.9487	2.9557
0.9457	0.1495	0.7686	0.6595	0.5371	.4051	0.2704	0.1495	0.0	
0.0732	-0.0732	-0.0562	-9.0464 -9.0361	-0.0405	-0361	-0.0330 -0.0562	-0.0296	-0.0142 -0.0732	3.0354
0.9621	0.1507	0.2709	0.4055	0.5376	0.4055	0.7705	9.8656 9.1507	0.9621	2.9415
-0.0927	-0.0927	-0.0704	-0-0576	-0.0501	-0.0446	-0.0406	.0.0353	-0.5071	3,3437
-0.0071	-0.0353	-0.0405	-0.0446	-0.0501	-0.0576	-0.0704	-0.0927	-0.0927	
0.0	0.1522	0.2714	0.4059	0.5383	0.6615	0.7729	0.9752	0.9720	3.9277
0.0770	0.8752	0.7729 -0.0839	-0.0662	0.5383	-0.0524	0.2714 -0.0473	0.1522	0.0	3.0417
0.0071	-0.0395	-0.0473	-0.0524	-0.0590	-0.0652	-0.0839	-0.1115	-0.1115	
0.0	2.1539	0.2719	0.4063	0.5390	0.6628	0.7750	0.8836	0,9753	3.9163
0.9751	0.8836	0.7758	0.0028	0.5390	-0.0598	-0.0535	0.1539	0.0246	2.0398
0.1297	-0.1297 -0.0422	-0.0967 -0.0535	-0.0783 -0.0598	-0.0675 -0.0675	-0.0598 -0.0783	-0.0959	-3.1297	-0.1297	3.0340
					0.6643	0.7794	0.6938	0.9725	0.9064
0.0	0.1558	0.2724	0.4068	0.5398	0.4068	0.2724	0.1758	0.0	
0.1475	-0.1475 -0.0431	-0.1096	-0-0881 -0-068	-0.0758	-0.0668	-0.0592 -0.1096	-9.0431 -0.1475	0.0421	0.0365
9.0421	-0.0431	-0.11542			•••••				
0.0 0.9651	0.1581	0.2730	0.4072	0.5406	0-6660	0.7836	0.9057	0.9551	1.6983
-0.1650	-9.1650	-0.1221	-0.0977	-0.0837	-0.0735	-0.0645	-0.0418	0.9578	0.0330
0.0575	-0.0418	-0.0645	-0.0735	-0.0837	-0.0977	-0.1221	-0.1650	-0.1550	
0.0	0.1605	0.2735	0.4077	0.5416	0.6679	0.7884	0.9184	0.9546	0.8913
0.9546 -0.1921	0.9184	3.7854 -0.1364	-0-6679	0.5416 -0.0915	-0.4077	-0.0594	0.1605 -0.0374	0.0711	7.0289
0.0711	-0.0374	-0.0694	-0.0800	-0.0915	-0.1071	-0.1344	-0.1821	-0.1881	
	0-1672	0.2741	0.4082	0.5427	0.6780	0.7919	0.9307	0.9419	2.0055
9-9419	0.9307	0.7939	0.6700	0.5427	28804.0	0.2741 -0.0739	0.1632 -0.0293	0.0	3.0242
0.1989	-0.1969 -0.0293	-0.1466	-0.1164	-0.0991	-0.0862	-0.1466	-0.1989	-0.1989	3.0545
			0.4087	0.5438	0.6724	0.8002	0.9412	0.9276	3.0013
0.0	0.1662	0.2747	0.6724	0.5438	0.4087	0.2747	0.1662	0.0	
0.2154	-0.2154	-0.1586	-0.1255	-0.1066	-0.0922	-0.0780	-0.0179	2.0979	>.01+>
0.0046									
0.0	0.1694	0.2753	0.4093	0.5450	0.6749	0.8073	0.9487	0.9124	3.6769
-0.2317	-0.2317	-0-1704	-0.1345	-0.1139	-0.0980	-0.0817	-0.0036	0.0951	3.0139
0.0951	-0.0036	-0.0817	-0.0980	-0.1139	-0.1345	-0.1704	-0.2317	-0.2317	
0.0	0.1728	0.2759	0.4098	0.5463	0.6776	0.8152	0.9527	0.8968	0.8784
0.9968	0.9527	0.8152	-0.1434	-0.5463	-0.1036	0.2759	0.1728	0.0 0.0977	3.0394
0.0977	0.0117	-0.0850	-0.1036	-0.1211	-0.1434	-0.1822	-0.2477	-0.2477	
0.0	0.1764	D.2765	0.4104	0.5477	0.6605	0.0239	0.9532	0.6810	3.8796
0.8810	0.9532	0.8239	0.6803	0.5477 -0.1281	-0.1091	-0.0878	0.1764	0.0	3.0061
0.0977	-9+2634 9+9278	-0.1939 -0.0879	-0.1522	-0-1281	~0.1522	-0.1939	-0.2434	-0.2634	,,,,,,,
		0.2772	0.4110	0.5491	0.6836	0.0334	0.9504	0.8556	>.0922
0.8636	0.1803	0.9334	0.6836	0.5491	0.4110	0.2772	0.1803	0.0	-
0.2788	-0.2788	-0.2054	-0.1609	-0.1351 -0.1351	-0.1143 -0.1609	-0.0901 -0.2054	0.0436	0.0352	0.0042
0.0	0.1844	0.2778	0.4116	0.5507	0.6869	0.8436 0.2778	0.9444 D.1644	0.8510	7.0951
-0.2030	-0.2939	-0.2169	-0.1696	-0.1419	-0.1193	-0.0916	0.0586	-0.2939	0.0040
0.0904	0.0586	-0.0916	-0.1193	-0.1419	-0.1695	-0.2169	-0.2939	-0.2939	
0.0	0.1867	0.2784	0.4172	0.5523	0.8903	0.8543	0.9357	0.8376	>.0686
0.5376	0.9357	0.8543	0.6903 -0.1781	0.5523	0.4122 -0.1240	0.2784	0.1887 0.0723	0.0	3.0050
0.0875	9.0723	-0.0922	-0.1781	-0.1485	-0.1751	-0.2283	-0.3088	0.0835	
0.0	0.1931	0.2790	0.4178	0.5540	0.6940	0.6654	0.9244	0.8257	2.8925
0.8257	0.9244	0.5654	0.6940	0.5540	0.4125	0.2790	0.1933	0.0	0.006
-0.1234									

Figure A-3. Continued.

TOTAL FLOW	ANGULAR	DEVSATION I	NF OR MAY 10	H FOR POSIT	YE Y-AX	AT THE X ST	ATTOM OF	0.6008 SE	HE-SPANS		
	.1495		0.2704	v -	0.4051	v =	0.5371	٧.	- 0.4595	Y = 0.	7606
Z	ANGLE	ž	ANGLE	z	ANGLE	,	ANGLE	Z	ANGLE	z	ANGLE
0.1769	2.78 3.00	Z 0.1936 0.1439	2,89	0.203	3.08	0.2095	3.38 3.55	0.21		0.2170	4.22
0.1248	3.00 3.14	0.1439	3,04	0.153	3.22	0.1595	3.67	0.11	39 4-24	0.1170	4.96
0.0268	3.09	0.0436	3.08	0.053	6 3.28 6 3.09	0-0593	3.40	9.06	39 4.48	0.0478	5.30 5.73
-0.0232	2.70	-0.0062		-0.003	6 3.09 4 2.87	-0.0405	3, 54	-0.03	39 4.40 61 4.21	0.9178	5.73 5.77
-0.0732 -0.1232	2.62	-0.0562	2.67	-0.000	2.91	-0.0903	3.32	-0.08	51 4.29	-0.0830	5.42
-0.1732	2.83	-0.1562	2.85	-0.146	3.03	-0.1407	3.37	-0-13	4.03	-0.1339	4.93
-0.2232	2.75	-0.2062	2,85	-0.196	3.03 4 2.93	-0.1905 -0.2465	3.36	-0.18	61 3.69 61 3.67	-0.2333	4.47
-0.2732	2.57	-0.2562	2.73	-0.296	2.78	-0.2903	3.07	-0.28	61 3.42	-0.5030	3.00

SIDEWASH I	NFORMATIC	N FOR POSIT	IVE Y-AXI			0.6000 SE					
	.1495	Y -	0.2704	y -	0.4051	ÿ.•	0.5371 AMGLE		- 0.6595 ANGLE	¥ = 0.	75 06 ANGLE
2 0.1768	-2.32	0.1939	ANGLE	0.203	ANGLE 6 ~1.76	0.2095	-1.45	0.21	39 -1.01	0.2173	-3.96
0.1268	-2.45	0.1439	-2.10	0.153	6 -1.81	0.1595	-1.52	0.16	39 -1.09	0.1670	-0.61 -0.64
0.0768	-2.44	0.0935 0.0438	-2.06	0.103	6 -1.70 6 -1.56	0.1095	-1.57 -1.36	0.06	39 -1.12	0.1170 2.0570	-2.55
-0.0232	-1.26	-0.0062	-1.14	0.003	6 -0.98	0.0595	-1.36 -0.88	0.06	39 -1.04 39 -0.69	0.0170	-9.56 -0.26
-0.0732	0.39	~8.0567	0.13	-0.046	0.05	-0.0405	0.01	-2-23		-0.0330 -0.0630	0.25
-0.1232 -0,1732	2.43	-0.1067	1.37	-0.096 -0.146	4 1.08 4 1.64	-0.1409	1.42	-0.13	1.16	-0.1330	0.77
-0.2232	2.46	-0.2062	2.14	-0.196	4 1.84	-0-1905	1.59	~7.18	61 1.23	-0.1933	0.69
-0.2732	5.35	-0.2562	2.11	-0.246 -0.296	4 t.85	-9.2405 -0.2905	1.58	-0.23	61 1.16	-0.2330	0.61
-0.3232	2.13	-0.3062	1.44	-0.246		-0,2903		-5126		-011030	****
DOWNWASH I	NFORMATIC	N FOR POSIT	IVE Y-AXI	S AT THE X	STATEON OF	0.6000 SE	I-SPANS				
¥ = 0	.1495	v =	0.2704	¥ =	0.4051	٧.	0.5371	¥ .	0.6595	Y = 0.	7686
,	ANGLE	z	ANGLE	0.203	ANGLE	0.2095	ANGLE 3.06	0 · 21	AMGLE 34 3.64	7 0.2170	ANG. E 4.18
0.1768	1.53	0.1935	2.05	0.203	6 2.67	0.1595	3.21	0.16	39 3.87	0.1670	4.53
0.0768	1.97	0.0939	2.35	0.103	6 2.79	0.1095	3.34	0,11	39 4.09	0.1170	4.92
0.0200	2.52	0.0431	2.40	0.003	6 2.8A 6 2.93	0.0595	3.43	0.04		0.0570	5.35 5.73
-0.0232 -0.0732	2.38 2.26	-0.0062	2.53	-0.046	2.93	-0.0405	3,35	-0.030	61 4-21	-0.0330	5.76
-0-1232	1.82	-0.1062	2.29	-0.096	2.70	-0.0995	3.19	-0,050	61 4.51	-0.0830	5.38
-0-1732	1.45	-0.1562	2.06	-0-146	4 2.54	-0.1405 -0.1905	3.08 2.96	-0.13	61 3.66 61 3.69	-0.1330 -0.1830	4.47
-0.2732	1.23	-0.2562	1.73	~0.246	4 2.28	-0-2405	2.83	-0.23	61 3.40	-2.2332	4.Dt
-0.3212	1.02	-0.3062	1.61	-0.296	4 2.15	-0.2907	2.69	-0.28	61 3.25	-0.2830	3,65
				-AKIS AT THI		SYMMETRY, T	-0				
WHITCHMA	JAFOIL CL	=1.2217 B/	2=19.85 x = 0.35	DATA FOR ATI	LIT	x = 0.50 'x	- 2.55 4	: = 0460 × Awsle	- 2.65 ×	T 0.70 K - 0. Mgle amsle	73 × = 0.80 Angle
WHITCHMA	# = 0.25 4 NGLF	x = 0.30 ANGLE 3.93	2=19.85 x = 0.35 ANGLE	X T 0.40 :	LIT K = 0.45 Angle	X = 0.50 X ANGLE A	- 2.55 4 NGLE 3.45	145LE /	146_E A	NGL5 ANGLE	ANGLE 3.15
#HITCHMM A 7 0+320 0+250	# = 0.25 ANGLE 4.05	x = 0.30 ANGLE 3.93 4.31	2=19.85 x = 0.35 ANGLE 3.52 4.17	X T U.40 : ANGLE 3-72 4-04	LIT * P 0.45 ANGLE 3.62 3.92	x = 0.50 x ANGLE A 3.53	- 2.55 4 NGLE 3.45 3.72	3.39 3.64	3.31 3.36	NGL5 ANGLE	3.15 3.35
#HITCHMM A 2 0+300 0+250 0+210	# = 0.25 ANGLE 4.05 4.48 4.91	x = 0.30 ANGLF 3.93 4.31 4.70 5.06	2=19-85 X = 0.35 ANGLE 3.52 4.17 4.51 4.74	X T 0.40 : ANGLE 3.72 4.04 4.36 4.56	NGLE 3.62 3.92 4.22	x = 0.50 x ANGLE A 3.53 3.91 4.10	- 0.55 4 NGLE 3.45 3.72 3.79	3.39 3.64 3.90	NG_E A 3.31 3.56 3.91 4.27	MGL5 AMSLE 3.25 3.20 3.49 3.43 3.74 3.67 3.99 3.92	ANGLE 3.15 3.38 3.61 3.86
2 0.300 0.250 0.210 0.150 0.100	x = 0.75 ANGLE 4.05 4.40 4.91 5.32 5.07	x = 0.30 ANGLF 3.93 4.31 4.70 5.05 5.37	2=19.85 X = 0.35 ANGLE 3.52 4.17 4.51 4.74 5-13	X T 0.40 : ANGLE 3-72 4.04 4.36 4.06 4.94	X P 0.45 ANGLE 3.62 3.92 4.22 4.51 4.77	x = 0.50 x ANGLE A 3.53 3.91 4.10	- 0.55 4 NGLE 3.45 3.72 3.79	3.39 3.64 3.90	NG_E A 3.31 3.56 3.91 4.27	MGL5 AMSLE 3.25 3.20 3.49 3.43 3.74 3.67 3.99 3.92	ANGLE 3-15 3-36 3-61 3-86 8-09
7 0.300 0.250 0.210 0.150 0.100	x = 0.25 ANGLE 4.05 4.40 5.32 5.07	x = 0.30 ANGLE 3.93 4.31 4.70 5.05 5.37 5.60	X = 0.35 ANGLE 3.52 4.17 4.51 4.74 5-13	X T 0.40 : ANGLE 3.72 4.04 4.36 4.66 4.94 5.15	ANGLE 3.62 3.92 4.22 4.51 4.77 4.98	x = 0.50 x ANGLE A 3.53 3.81 4.10 4.37 4.63 4.84	- 3.55 4 NGLE 3.45 3.72 3.99 4.26 4.51	AMSLE 3-39 3-64 3-90 4-16 4-61	A4G_E A 3.31 3.36 3.91 4.77 4.31 4.52	MGLE AMSLE 3.25 3.20 3.49 3.43 3.74 3.67 3.99 3.92 4.23 4.16 4.44 4.37	ANGLE 3.15 3.35 3.61 3.86 4.09
7 0.329 0.250 0.250 0.150 0.150 0.150	# = 0.25 ANGLE 4.05 4.48 4.91 5.32 5.67 5.90	X = 0.30 ANGLE 3.93 4.31 4.70 5.05 5.37 5.60	2=19.65 X = 0.35 ANGLE 3.52 4.17 4.51 4.54 5.13 5.46 6.55 6.5	X Y 0.40 : ANGLE 3.72 4.04 4.36 4.94 5.15 5.27	X P 0.45 ANGLE 3.62 3.92 4.22 4.51 4.77 4.98 5.10	x = 0.50 x ANGLE A 3.53 7.81 4.10 4.37 4.63 4.84 4.97 4.98	- 2.55 4 NGLE 3.45 3.72 3.99 4.26 4.51 4.72 4.85	AWGLE 3 3.39 3.64 3.90 4.16 4.41 4.61 4.75 6.79	AG_E A 3.31 3.36 3.91 4.77 4.31 4.52 4.57 4.71	MGLE AMGLE 3.20 3.43 3.43 3.43 3.43 3.43 3.43 3.43 4.16 4.37 4.59 4.50 4.50	ANGLE 3.15 3.35 3.61 3.86 4.09 4.40 4.53
7 0.300 0.25n 0.25n 0.15n 0.15n 0.15n -0.000 -0.000	x = 0.25 ANGLE 4.05 4.491 5.32 5.47 5.40 5.47 5.40 5.47	X = 0.30 ANGLE 3.93 4.31 4.70 5.06 5.37 5.69 5.63 5.42	2=19-85 X = 0.35 ANGLE 3-82 4-17 4-51 4-94 5-13 5-46 5-42 5-25	X V 0.40 :: ANGLE 3.72 4.04 4.36 4.06 4.04 5.15 5.27 5.25 5.10	X P 0.45 ANGLE 3.62 3.92 4.22 4.21 4.77 4.98 5.10 5.11	X = 0.50 x ANGLE A 3.53 3.71 4.10 4.37 4.63 4.84 4.97 4.98	- 3.55 4 NGLE 3.45 3.72 3.99 4.26 4.51 4.51 4.52 4.65	AMSLE 3-39 3-54 3-90 4-16 4-41 4-75 4-75 4-79	AMG_E A 3.31 3.56 3.91 4.77 4.31 4.52 4.57 6.71 4.56	MGLE ANSLE 3.25 3.20 3.49 3.43 3.74 3.67 3.99 3.92 4.25 4.16 4.37 4.59 4.52 4.64 4.37 4.59 4.59	ANGLE 3-15 3-35 3-61 3-86 4-09 4-30 4-46 4-53 4-48
7 0.329 0.239 0.239 0.299 0.199 0.199 0.199 -0.050 -0.170 -0.150	x = 0.25 ANGLE 4.05 4.491 5.32 5.47 5.40 5.47 5.40 5.47	x = 0.30 ANGLE 3.93 4.31 4.70 5.05 5.69 5.69 5.69 5.63 5.42	X = 0.35 ANGLE 3.52 4.17 4.51 4.51 5.13 5.40 5.42 5.25	x v 0.40 :: ANGLE 3-72 4.04 4.36 4.36 4.36 5.13 5.27 5.25 5.10 4.34	X P 0.45 ANGLE J.62 J.62 4.22 4.51 4.77 4.98 5.10 5.11 4.98 4.74	x = 0.50 x ANGLE A 3.53 3.91 4.10 4.37 4.63 4.64 4.97 4.98 4.87	- 3.55 4 NGLE 3.45 3.72 3.99 4.26 4.56 4.56 4.72 4.85 4.86 4.88	A WSLE 3-39 3-54 3-50 4-16 4-61 4-61 4-75 4-79 4-71	AMG_E A 3-31 3-36 3-91 4-77 4-77 4-52 4-57 6-71 4-66	MGLE MALE 3.25 3.26 3.49 3.49 3.49 3.49 3.49 3.49 3.49 3.49	ANGLE 3-15 3-36 3-61 3-86 4-09 4-46 4-53 4-46
7 0.300 0.25n 0.25n 0.15n 0.15n 0.15n -0.000 -0.000	x = 0.25 ANGLE 4.05 4.491 5.32 5.47 5.40 5.47 5.40 5.47	x = 0.30 ANGLE 3.93 4.70 5.05 5.05 5.69 5.63 5.42 5.10 4.71 4.30	2=19-85 X = 0.35 ANGLE 3-92 4-17 4-51 4-94 5-17 5-35 5-40 5-42 5-25 4-96 4-61 4-23	X V 0.40 : ANGLE 3-72 4-04 4-36 4-36 4-36 5-15 5-27 5-25 5-10 4-84 4-52 4-17	NGLE 3-62 3-62 3-62 3-92 4-27 4-98 5-11 4-98 4-74 4-44 4-11	x = 0.50 x ANGLE A 3.33 3.71 4.17 4.37 4.63 4.84 4.97 4.98 4.87 4.66 4.37 4.66 4.37	- 3.55 4 NGLE 3.45 3.72 3.99 4.26 4.56 4.56 4.72 4.85 4.86 4.88	A WALE 3 - 34	AMG_E A 3.31 3.56 3.91 4.77 4.71 4.52 4.57 4.76 4.76 4.66 4.21 3.23	MGLE AMGLE 3.29 3.43 3.74 3.67 3.79 3.92 4.23 4.14 4.59 4.52 4.64 4.37 4.61 4.37 4.17 4.14 4.17 4.14	ANGLE 3-15 3-35 3-61 3-86 4-09 4-30 4-46 4-53 4-48 6-33 4-11 3-84
WHITCHMM A 7 0.320 0.250 0.250 0.150 0.150 -0.020 -0.150 -0.120 -0.150 -0.250 -0.250	19F01L CL # = 0.25 ANGLE 4.05 4.40 5.32 5.47 5.47 5.40 5.64 5.25 4.30 4.30 3.92	X = 0.30 ANGLE 3.93 4.70 5.05 5.37 5.69 5.63 5.42 5.10 4.71 4.30 3.90	2=19.85 x = 0.35 ANGL & 3.92 4.17 4.51 4.54 5-13 5-35 5-40 5-42 5-25 4.91 4.23 3.86	A T 0.40 : ANGLE 3-72 4-04 4-36 4-06 4-06 5-15 5-27 5-25 5-10 4-84 4-52 4-17 3-82	X P 095 ANGLE 362 392 451 477 478 511 4.98 4.74 4.94 4.11 3.78	x = 0.50 x ANGLE A 3.53 3.91 4.10 4.37 4.64 4.97 4.08 4.87 4.66 4.37 4.06 4.37	- 3.55 4 NGLE 3.45 3.72 3.70 4.26 4.51 4.68 4.78 4.68 4.78 4.78	AMSLE 3 3.34 3.54 3.54 3.50 4.16 4.41 4.41 4.75 6.79 4.71 4.52 6.26 7.97	AMG_Z 3-31 3-56 3-91 4-77 4-57 4-57 4-57 4-57 4-58 4-58 4-51 3-93 1-51	MGLE AMSLE 3.20 3.20 3.20 3.20 3.20 3.20 3.43 3.74 3.67 3.42 4.23 4.14 4.37 4.50 4.50 4.51 4.17 3.00 3.86 4.17 3.00 3.86	ANGLE 3-15 3-35 3-61 3-66 4-30 4-40 4-33 4-46 4-53 4-48 4-33 4-11 3-84 3-56
7 0.300 0.25n 0.70n 0.15n 0.15n 0.15n 0.000 -0.15n -0.000 -0.15n -0.000 -0.15n -0.300 -0.300 -0.350	X = 0.25 ANGLE 4.05 4.05 4.05 4.91 5.32 5.07 5.00 5.00 5.00 4.00 5.00 5.00 5.00 4.00 5.00 6	X = 0.30 ANGLE 3.93 4.31 4.70 5.06 5.37 5.69 5.63 5.42 5.10 4.71 4.70 3.90 3.90 3.90	2=19.85 X = 0.35 ANGLE 3.52 4.17 4.51 4.14 5.15 5.46 5.42 5.25 4.01 4.23 3.86 3.50 1.50	X V 0.40 : ANGLE 3-72 4-04 4-36 4-36 4-36 5-15 5-27 5-25 5-10 4-84 4-52 4-17 3-82 3-86	NO.45 ANGLE 3-62 3-92 4-27 4-77 4-98 5-10 5-11 4-98 4-74 4-44 4-11 3-78	X = 0.50 X ANGLE A 3.53 3.91 4.10 4.21 4.03 4.04 4.07 4.06 4.07 4.06 4.07 4.07 4.00 4.07 4.00 4.07 4.00 4.07 4.00 4.07 4.00 4.07 4.00 4.00	- 0.09 4 3.45 3.72 3.79 4.72 4.85 4.85 4.85 4.86 4.81 4.81	AMGLE 3 3-39 3-64 3-90 4-16 4-61 4-61 4-79 4-79 4-79 4-52 6-26 7-97 7-67 3-37	NG_5 A 3.31 3.31 3.56 3.91 4.77 4.52 4.57 4.57 4.66 6.66 6.21 3.93 3.93	NGLE ANGLE 3.29 3.20 3.49 3.43 3.74 3.67 3.99 3.92 4.23 4.18 4.44 4.37 4.59 4.52 4.51 4.17 4.17 4.14 3.89 3.86 3.61 3.58 3.53 3.33	ANGLE 3-15 3-38 3-61 3-86 4-09 4-30 4-46 4-53 4-48 4-33 4-11 3-84 3-56 3-29
VMITCHM9 A 7 0.370 0.250 0.270 0.150 0.150 0.050 -0.170 -0.150 0.270 -0.150 -0.270 -0.150 -0.270 -0.150 -0.270 -0.150 -0.270 -0.270 -0.270 -0.270 -0.350	x = 0.25 ANGLF 4.05 4.86 4.80 5.32 5.07 5.97 5.90 5.90 5.90 5.92 5.92 5.93 5.94 5.92 4.95 4.36 5.92 7.55 7.75 7.75 7.75 7.75 7.75 7.75 7.7	X = 0.30 ANGLE 3.93 4.70 5.05 5.37 5.69 5.63 5.42 5.10 4.71 4.30 3.90	2=19.65 X = 0.35 ANGL E 3.82 4.17 4.74 5.17 5.25 5.40 5.25 4.96 4.01 4.23 3.86 1.50 3.17 2.67	X V 0.40 SANGE 3.72 A.00 A.00 A.00 A.00 A.00 A.00 A.00 A.0	X W 0.45 ANGLE 3-62 7-92 4-51 4-76 5-10 5-11 4-98 4-74 4-44 4-11 3-45 3-15 2-87	X = 0.50 X ANGLE A 3.33 3.91 4.10 4.17 4.63 4.64 4.97 4.97 4.97 4.97 4.97 4.97 4.97 4.9	- 3.55 4 NGLE 3.45 3.42 3.99 4.26 4.75 4.85 4.86 4.55 4.86 4.55 3.70 3.70 3.70	ANGLE // 3.39 3.84 3.90 4.16 4.16 4.41 4.75 4.77 4.52 4.71 4.52 4.26 7.07 7.67 7.67 7.67	NG_5 A 3.31 3.36 3.31 3.36 3.91 4.37 4.31 4.52 4.57 6.71 6.71 6.66 6.66 6.21 3.93 3.93 3.93 3.93	MGLE AMSLE 3.20 3.20 3.20 3.20 3.20 3.20 3.20 3.74 3.67 3.67 3.90 3.92 4.53 4.54 4.37 4.54 4.54 4.57 4.17 4.14 4.17 4.18 3.60 3.60 3.60 3.60 3.60 3.60 3.60 3.60	ANGLE 3-15 3-36 3-66 4-09 4-30 4-46 4-53 4-46 4-53 4-11 3-84 3-56 3-29 3-03 2-79
WHITCHMM A 7 0.370 0.250 0.270 0.150 0.150 0.050 -0.170 -0.150 -0.270 -0.150 -0.270 -0.150 -0.270 -0.150 -0.270 -0.270 -0.270 -0.270 -0.270 -0.270 -0.350	x = 0.25 ANGLF 4.05 4.86 4.80 5.32 5.07 5.97 5.90 5.90 5.90 5.92 5.92 5.93 5.94 5.92 4.95 4.36 5.92 7.55 7.75 7.75 7.75 7.75 7.75 7.75 7.7	x = 0.30 ANGLE 3.03 4.31 4.70 5.05 5.05 5.60 5.63 5.69 5.63 5.42 5.10 4.71 4.30 3.51 7.31 7.31 7.31 7.31 7.31 7.31 7.31 7.3	2=19.85 X = 0.35 ANGLE 3.82 4.17 4.51 4.74 5.15 5.40 5.12 5.40 6.61 6.25 6.06 6.25 6.06 6.26 7.25 6.06 7.2	X V 0.40 SANGE 3.72 A.00 A.00 A.00 A.00 A.00 A.00 A.00 A.0	X = 0.45 ANGLE 3.62 3.62 4.22 4.51 4.71 4.98 4.71 4.98 4.74 4.44 4.11 3.47 3.45 3.45 3.45 3.45	X = 0.50 X ANGLE A 3.53 3.61 4.10 4.37 4.63 4.97 4.68 4.97 4.66 6.37 4.66 6.37 3.76 3.76 3.43 3.11	- 3.55 4 NGLE 3.45 3.42 3.99 4.26 4.75 4.85 4.86 4.55 4.86 4.55 3.70 3.70 3.70	ANGLE // 3.39 3.84 3.90 4.16 4.16 4.41 4.75 4.77 4.52 4.71 4.52 4.26 7.07 7.67 7.67 7.67	NG_5 A 3.31 3.36 3.31 3.36 3.91 4.37 4.31 4.52 4.57 6.71 6.71 6.66 6.66 6.21 3.93 3.93 3.93 3.93	MGLE AMSLE 3.20 3.20 3.20 3.20 3.20 3.20 3.20 3.74 3.67 3.67 3.90 3.92 4.53 4.54 4.37 4.54 4.54 4.57 4.17 4.14 4.17 4.18 3.60 3.60 3.60 3.60 3.60 3.60 3.60 3.60	ANGLE 3-15 3-36 3-61 3-86 4-30 4-46 4-33 4-11 3-84 3-56 3-29 3-03 2-70
7 0.300 0.250 0.270 0.170 0.170 0.170 0.170 0.170 0.000 0.170 0.250 0.170 0.250 0.470 0.450 0.450	x = 0.25 ANGLF 4.05 4.86 4.80 5.32 5.07 5.97 5.90 5.90 5.90 5.92 5.92 5.93 5.94 5.92 4.95 4.36 5.92 7.55 7.75 7.75 7.75 7.75 7.75 7.75 7.7	X = 0.30 ANGLE 3.93 4.31 5.05 5.05 5.05 5.09 5.09 5.03 5.02 5.00 5.03 5.03 5.03 5.03 5.03 5.03 5.03	2=19.65 X = 0.35 ANGLE 3.52 4.17 4.51 5.55 5.42 5.25 4.96 4.61 A.27 3.86 3.17 2.97 2.99 2.34	X T 0.40 ATI X T 0.40 ANGLE 3-72 4-04 4-36 4-06 4-05 5-15 5-25 5-25 5-25 4-82 4-17 3-46 3-46 2-61	X = 0-45 ANGLE 3-02 4-22 4-25 4-51 4-78 5-10 5-11 4-98 4-74 4-44 4-41 3-45 3-15 2-87 2-87 2-62	X = 0.50 X ANGLE A 3.53 3.61 4.10 4.37 4.63 4.97 4.68 4.97 4.66 6.37 4.66 6.37 3.76 3.76 3.43 3.11	- 0.55 4 NGLE 3.45 3.45 3.72 3.90 4.26 4.55 4.65 4.65 4.65 4.61 3.70 3.12 2.86 2.61	AUGLE J 3.39 3.64 5.90 4.16 4.41 4.47 4.47 4.51 4.79 4.72 4.52 4.26 7.07 7.67 3.10 7.87 3.10 7.88	NG_5 A 3.31 3.36 3.31 4.37 4.37 4.37 4.52 4.57 4.51 4.64 4.21 3.23 3.33 3.33 3.33 3.33 3.33 3.33 2.13 2.1	NGLE AMALE 3.25 3.20 3.49 3.43 3.74 3.67 3.90 3.42 4.61 4.37 4.59 4.52 4.17 4.14 4.17 4.14 3.61 3.50 3.61 3.50 3.61 3.50 3.61 3.50 3.61 3.50 3.61 3.50	ANGLE 3-15 3-36 3-66 4-30 4-46 4-33 4-46 4-33 4-11 3-86 3-56 3-27 3-03 2-70 2-37
WHITCHM9 A 0.370 0.250 0.250 0.270 0.150 0.150 0.050 0.150 0.270 0.150 0.270 0.150 0.270 0.250 0.250 0.250 0.250 0.250 0.250	x = 0.25 ANGLE 4.05 4.60 4.60 4.91 5.12 5.07 5.04 5.22 5.7 5.04 5.22 4.7 4.7 4.15 2.2 3.15 2.3 3.15 2.3 3.15 2.3 3.15 2.3 3.15 2.3 3.15 2.3 3.15	X # 0.30 AMGLE 3.93 4.70 5.00 5.00 5.60 5.62 5.62 5.62 6.71 7.72 7.73 7.73 7.73 7.73 7.73 7.73 7.73	2=19.85 X = 0.35 ANGLE 3.82 4.17 4.51 4.55 5.45 5.45 4.55 4	DATA FOR AYI X	X W 0.45 AMGLE 3.62 7.92 4.51 4.77 4.78 4.77 4.78 4.77 4.90 4.10 5.10 4.90 4.11 3.45 3.45 3.45 3.45 3.45 3.45 3.45	AMGLE A 3-53 7-91 4-10 4-37 4-63 4-66 4-66 4-37 4-00 3-74 3-63 3-74 3-63 2-67 2-67 2-67 2-74 2-75 2-75 2-75 2-75 2-75 2-75 2-75 2-75	- 0.00 4 NGLE 3.45 3.72 4.72 4.86 4.72 4.86 4.73 4.50 4.73 4.50 3.70 3.70 3.140 3.140 3.140 3.12 2.86 2.01 2.210	AUGLE J 3.39 3.64 5.90 4.16 4.41 4.41 4.75 6.79 4.75 6.79 4.71 7.67 7.67 7.67 7.67 7.67 7.61 7.87 7.10 7.87 7.87 7.87 7.87 7.87	NG_5 A 3.31 3.36 3.31 4.37 4.37 4.37 4.52 4.57 4.51 4.64 4.21 3.23 3.33 3.33 3.33 3.33 3.33 3.33 2.13 2.1	NGLE AMALE 3.25 3.20 3.49 3.43 3.74 3.67 3.90 3.42 4.61 4.37 4.59 4.52 4.17 4.14 4.17 4.14 3.61 3.50 3.61 3.50 3.61 3.50 3.61 3.50 3.61 3.50 3.61 3.50	ANGLE 3-15 3-36 3-66 3-66 4-30 4-46 4-33 4-46 3-33 4-11 3-86 3-29 2-29 2-79 2-19 2-19 2-19 2-19 2-19
7 0.300 0.250 0.270 0.170 0.170 0.170 0.170 0.170 0.000 0.170 0.250 0.170 0.250 0.470 0.450 0.450	# = 0.25 ANGLE 4.05 4.05 4.07 5.12 5.07 5.00 5.07 5.04 5.29 4.10 7.00 7.00 7.00 7.00 7.00 7.00 7.00 7	X = 0.30 ANGLE 3.93 4.70 5.06 5.06 5.69 5.69 5.63 5.42 5.10 4.71 4.70 3.90 3.91 7.265 7.265 7.265 7.265	2=19.85 X = 0.35 ANGLE 3.92 4.17 4.51 4.51 5.15 5.16 5.42 5.25 4.96 4.51 4.51 4.51 7.25 7	X T 0.40 AYI X T 0.40 AYI ANGLE 3.72 4.36 4.36 4.36 4.36 4.36 4.37 4.17 3.48 4.52 4.17 3.48 3.16 3.16 2.27 2.15	X F 0.45 ANGLE 3.62 7.92 4.51 4.77 4.98 5.10 5.10 5.11 4.74 4.44 4.11 3.45 3.45 2.67 2.67 2.62 2.38	AMGLE A 3-53 7-91 4-10 4-37 4-63 4-66 4-66 4-37 4-00 3-74 3-63 3-74 3-63 2-67 2-67 2-67 2-74 2-75 2-75 2-75 2-75 2-75 2-75 2-75 2-75	- 0.55 4 NGLE 3.45 3.472 3.479 4.72 4.85 4.72 4.85 4.73 4.53 4.70 3.40 3.40 3.40 2.86 2.261 2.39	AMSLE J 3.39 3.64 3.90 4.16 4.41 4.75 4.70 4.71 4.52 4.26 3.26 3.10 7.67 3.37 7.67 3.37 7.67	NG_5 A 3.31 3.36 3.31 4.37 4.37 4.37 4.52 4.57 4.51 4.64 4.21 3.23 3.33 3.33 3.33 3.33 3.33 3.33 2.13 2.1	NGLE AMALE 3.25 3.49 3.49 3.40 3.40 3.40 3.40 3.40 4.50 4.50 4.50 4.50 4.50 4.51 4.17 4.17 4.17 4.17 4.17 4.17 4.17 4.1	ANGLE 3-15 3-35 3-61 3-66 4-09 4-30 4-46 4-53 4-49 4-73 4-11 3-84 3-56 3-29 3-03 2-70 2-57 2-37
WHITCHMM A 7 0.379 0.379 0.170 0.150 0.150 0.150 0.150 0.150 0.150 0.050 0.050 0.050 0.050 0.050 0.050 0.050 0.050 0.050	# # 0.45	x x 0,30 x x 0,30 AMGLE 3,03 4,01 4,00 5,00 5,00 5,00 5,00 6,10 4,10 4,10 4,10 4,10 4,10 4,10 4,10 4	2=19.65 X = 0.32 3.92 4.17 4.51 4.74 5.15 5.40 5.40 6.27 3.80 7.20 7.20 7.20 7.20 7.20 7.20 7.20 7.2	DATA FOR ATI 2 Y 0.40 ANGLE 3-72 4-06 4-06 4-06 5-17 5-27 5-27 5-27 5-28 4-52	x = 0.405 AndLE 3.62 3.92 4.22 4.51 4.71 3.93 4.73 3.93 3.70 3.70 3.70 3.70 3.70 3.70 3.70 3.7	X = 0.30 ANGLE A 3.33 3.31 4.37 4.63 4.63 4.60 4.37 4.60 4.37 4.60 4.37 4.60 4.37 4.60 4.37 2.62 2.39 2.10	- 0.05 4 NGLE NGLE 3.45 3.72 4.26 4.26 4.26 4.31 4.05 4.31 4.01 4.	AVSLE J 3.39 3.60 3.60 4.16 4.17 4.21 4.2	NGC.E A 3.31 3.35 3.36 4.27 4.27 4.71 4.72 4.71 4.72 4.71 4.72 4.71 4.72 4.71 4.72 4.71 4.72 4.71 4.72 4.72 4.72 4.72 4.72 4.72 4.72 4.72	MGLE ANGLE 3.43 3.45 3.45 3.46 3.47 3.47 4.79 4.52 4.53 4.54 4.57 4.59 4.53 4.77 3.69 3.60 3.70 3.60 3.70 3.60 3.70 3.60 3.70 3.70 3.70 3.70 3.70 3.70 3.70 3.7	AMGLE 3-135 3-35 3-36 3-06 4-30 4-46 4-30 4-46 4-33 4-11 3-86 3-26 3-27 2-37 2-17 2-17 2-17 2-19 2-02 1-96
VHITCHM A 7 0. 170 0. 25e 0. 27n 0. 15n 0.	X = 0.25 ANGLE 4.05 4.05 6.01 5.12 5.02 5.07 5.04 5.02 5.07 5.04 5.02 7.02 7.02 7.15 7	x = 0.30 AMGLE 3.93 4.31 4.70 5.60 5.61 5.62 5.62 5.63 5.62 5.61 5.92 4.10 1.90 3.91 1.72 2.85 2.97 2.10 2.86 2.97 2.87 2.87 2.87 2.87 2.87 2.87 2.87 2.8	2=19.85 X = 0.35 ANGLE 3.92 4.17 5.16 5.40 5.40 5.40 5.40 4.25 4.01 4.27 3.86 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25	DATA FOR ATI X Y G.40 ANGLE 3-72 4-72 4-72 4-72 4-72 5-15 5-27 5-25 5-27 5-25 5-27 5-25 1-96 1-79 X = 1-00 X	ANGLE 302 192 421 421 421 421 477 498 5.10 5.10 5.10 5.10 5.10 5.10 5.10 5.10	X = 0.30 A ANGLE A 3.33 3.71 4.137 4.637 4.64 4.97 4.66 4.97 4.67 4.67 4.67 4.67 4.67 4.67 4.67 4.6	- 2.55 4 NGLE 3.45 3.45 3.47 3.47 3.47 4.26 4.51 4.65 4.72 4.65 3.40 3.40 3.40 3.40 3.40 3.40 3.40 3.40	AVSLE J 3.39 3.60 3.60 4.16 4.17 4.21 4.2	NGC.E A 3.31 3.35 3.36 4.27 4.27 4.71 4.72 4.71 4.72 4.71 4.72 4.71 4.72 4.71 4.72 4.71 4.72 4.71 4.72 4.72 4.72 4.72 4.72 4.72 4.72 4.72	MGLE ANGLE 3.43 3.45 3.45 3.46 3.47 3.47 4.79 4.52 4.53 4.54 4.57 4.59 4.53 4.77 3.69 3.60 3.70 3.60 3.70 3.60 3.70 3.60 3.70 3.70 3.70 3.70 3.70 3.70 3.70 3.7	ANGLE 3-135 3-38 3-06 4-3-30 4-46 4-33 4-46 4-33 4-45 3-86 3-26 3-27 2-19 2-19 2-19 2-19 2-19 2-19 2-19 2-19
VHITCHM A 7 0.170 0.25c 0.27c 0.170 0.050 -0.150	# = 0.25 # = 0.25 # 4.05 # 4.05 # 4.05 # 6.01 5.12 5.00 5.	x = 0.30 AMGLE 3.03 4.31 4.70 5.00 5.00 5.00 5.01 5.02 4.10 4.10 4.10 1.00 1.	2=19.85 X = 0.35 ANGLE 3.92 4.17 5.16 5.40 5.40 5.40 5.40 4.25 4.01 4.27 3.86 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25 4.27 7.25	DATA FOR ATI X Y G.40 ANGLE 3-72 4-72 4-72 4-72 4-72 5-15 5-27 5-25 5-27 5-25 5-27 5-25 1-96 1-79 X = 1-00 X	ANGLE 302 192 421 421 421 421 477 498 5.10 5.10 5.10 5.10 5.10 5.10 5.10 5.10	X = 0.30 A ANGLE A 3.33 3.71 4.137 4.637 4.64 4.97 4.66 4.97 4.67 4.67 4.67 4.67 4.67 4.67 4.67 4.6	- 0.093 4 NGLE 3.45 3.47 3.476 4.76 4.76 4.75 4.65 4.65 4.60 4.55 4.10 3.12 2.66 2.61 2.10 2.10 2.10 2.10 2.10 2.10 2.10 2.1	AVGLE J 3.34 3.43 3.44 4.41 4.41 4.41 4.41 4.41	NGCE A 3.31 3.56 4.77 4.57 4.57 4.57 4.50 4.57 4.50 3.73 3.73 3.73 3.73 3.73 3.73 3.73 3.7	MGLE ANGLE 3.25 3.25 3.25 3.25 3.25 3.25 3.25 3.20 3.20 3.20 3.20 3.20 3.20 3.20 3.20	ANGLE 3-15 3-35 3-36 3-66 4-30 4-40 4-30 4-40 3-56 3-29 3-56 3-29 3-69 2-19 2-19 2-19 2-19 2-19 2-19 2-19 2-1
VMITCOMM A 7 0. 370 0. 225 0. 275 0. 170 0	X = 0.25 ANGLE 4.05 4.05 4.05 5.07 5	x = 0.30 x = 0.30 AMGLE 3.03 4.31 6.70 5.60 5.61 5.62 5.61 5.62 5.61 7.72 7.73 7.73 7.74 7.75 7.75 7.75 7.75 7.75 7.75 7.75	2=19.85 X = 0.35 ANGLE 3.92 4.17 4.51 5.15 5.40 5.42 7.19 5.10 5.42 7.25 7.25 7.25 7.27 7.380 7.19 7.390 7.19 7.390 7.300 7.300 7.300 7.300 7.300 7.300 7.300 7.300 7.300 7.300 7.	X Y G.+0 ATI X Y G.+0 ATI X Y G.+0 ATI X ANGLE 3.72 A.04 A.34 A.04 A.04 A.04 A.04 A.04 A.04 A.04 A.0	ANGLE 3.62 3.62 3.79 4.77 4.98 5.10 5.11 5.10 5.11 3.78 3.15 3.45 3.45 3.16 1.98 1.98	X = 0.30 X ANGLE A 3.33 7.71 4.107 4.62 4.63 4.64 4.97 4.06 4.07 4.06 3.74 3.14 2.07 2.010 2.07 2.010 2.07 2.010 2.07 2.010 2.07 2.010 2.07 2.010 2.07 2.010 2.07 2.010 2.07 2.010 2.07 2.010 2.07 2.07 2.07 2.07 2.07 2.07 2.07 2.0	- 2.53 4 NGLE 3.45 3.472 3.406 4.51 4.66 4.51 4.67 3.40 3.40 3.40 3.40 3.40 3.40 3.40 3.40	AVSLE J 3.39 3.04 4.05 4.05 4.05 4.05 4.07 4.71 4.72 4.72 4.71 4.72 4.71 4.71 4.72 4.73 4.73 4.73 4.73 4.73 4.73 4.73 4.73	NGC. A 3.31 3.56 3.31 3.56 4.61 4.61 4.61 4.62 4.57 4.66 4.61 4.66 4.21 3.76 3.76 3.76 2.19 2.19 2.10 2.10 2.10 2.10 2.10 2.10 2.10 2.10	MGLE ANGLE 3.45 1.25 1.25 1.25 1.25 1.25 1.25 1.25 1.2	ANGLE 3-15 3-35 3-36 3-36 3-36 3-36 3-36 3-36 4-39 4-46 4-53 4-49 3-53 4-11 3-86 3-36 3-29 3-20 2-70 2-57 2-19 2-02 1-90 ANGLE 2-77 2-19 2-02 1-90 3-80 3-80 3-80 3-80 3-80 3-80 3-80 3-8
VHITCOMM A 7 7 0.170 0.25c 0.2nc 0.15n	# = 0.25 4.05 4.05 4.05 4.05 5.12 5.72 5.70 7.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 4.00 5.20 6.	x = 0.30 x = 0.	2=19.65 X = 0.32 3.62 4.17 4.51 4.74 5.15 5.42 5.25 4.96 4.61 7.25 4.97 7.25 4.97 7.37 7.37 7.37 7.37 7.37 7.37 7.37 7.37 7.37 7.37	DATA FOR ATI X Y G.40 ANGLE 3-72 4-72 4-72 4-72 4-72 5-15 5-27 5-25 5-27 5-25 5-27 5-25 1-96 1-79 X = 1-00 X	ANGLE 3.62 3.62 3.792 4.72 4.73 4.70 5.10 5.11 4.74 4.76 4.76 4.76 3.15 2.67 2.62 3.15 2.67 3.15 2.67 3.15 2.67 3.15 3.15 3.15 3.15 3.15 3.15 3.15 3.15	X = 0.50	- 0.003 4 NGLE 3.453 3.472 3.406 4.72 4.72 4.72 4.73 4.70 3.70 3.10 3.70 3.12 2.00 3.12 2.10 2.01 2.01	Avgl. 2 3.34 4.10 4.10 4.10 4.10 4.10 4.10 4.10 4.1	NGC_E A 3.36 3.36 3.36 4.37 4.97 4.91 4.92 4.92 4.92 4.92 4.92 4.92 4.92 4.92	MGLE ANGLE 3.25 3.25 3.25 3.25 3.25 3.25 3.25 3.20 3.20 3.20 3.20 3.20 3.20 3.20 3.20	AMGLE 3-135 3-35 3-36 3-06 4-30 4-46 4-30 4-46 4-30 4-30 4-30 4-30 4-30 4-30 4-30 4-30
WHITCOMM A 7 0.1707 0.2707 0.1707	# # 0 - 25 # 0 - 25 # 0,25 # 0,66 # 0,12 \$ - 0,75 # 0,00 \$ - 0,12 \$ - 0,75 # 0,00 \$ - 0,75 # 0,00 # 0,00	x = 0.30 x = 0.30 AMSUE 3.93 4.31 4.00 5.27 5.00 5.61 4.71 4.70 1.00 1.00 1.00 1.00 1.00 1.00 1.00 1	2=19.85 X = 0.35 ANGLE 3.92 4.17 4.18 5.19 5.19 5.19 5.40 4.01 4.23 3.00 7.19 7.19 7.19 7.19 7.19 7.19 7.19 7.19	DATA FOR ATI 2 Y 0.40 ANGLE 3.72 4.00 4.00 4.00 5.13 5.27 5.25 5.27 5.22 5.22 7.22 4.00 4.01 4.02	ANGLE 302 ANGLE 302 ANGLE 302 A51 A77 A98 5.10 5.110 5.110 347 A44 A11 346 A71 A98 A71 A72 A78 A78 A78 A79 A	X = 0.30 A ANGLE A 3.93 3.7.11 4.137 4.637 4.64.37 4.64.37 4.657 4.67 4.67 4.67 4.67 4.67 4.67 4.67 4.6	- 0.00 A A A A A A A A A A A A A A A A A	Avg.L. J.	NGC.E A 3.31 3.56 3.31 3.56 4.51 4.51 4.52 4.57 4.51 4.52 4.57 4.51 5.66 5.76 5.76 5.76 6.66 6.76 6.66 6.76 6.7	MGLE ANGLE 3.25 3.25 3.25 3.25 3.25 3.25 3.25 3.25	ANGLE 3-15 3-35 3-06 3-09 4-09 4-30 4-40 4-31 4-48 4-31 4-48 3-56 3-29 3-03 2-70 2-57 2-17 2-17 2-19 2-19 2-19 3-100 3-1
VHITCHM A 7 0. 170 0. 25 c 0. 270 0. 25 c 0. 270 0. 05 c 0. 150 0. 05 c 0. 150 0. 15	X = 0.25 ANGLE 4.05 4.05 6.01 5.12 5.00 5.07 5.00 5.07 5.00 5.07 5.00 5.07 7.00 7	x = 0.30 AMGLE 3.09 5.60 5.60 5.60 5.61 5.22 5.10 1.72 2.85 2.31 2.10 AMGLE 3.30 AMGLE 3.30 3.30 AMGLE 3.30	2=19.85 X = 0.35 ANGLE 3.92 4.17 4.51 5.40 5.42 5.40 5.42 5.40 5.42 5.25 4.90 3.17 2.17	DATA FOR ATI 2 * G.+G. ANGLE 3-72 4-36 4-36 5-15 5-27 5-25 5-10 4-84 6-15 5-27 5-25 5-10 4-84 6-16 7-16	LIV A W 0.40 ANGLE 3.62 3.92 4.72 4.98 5.10 5.11 4.98 4.74 4.98 5.15 2.17 2.62 2.87 2.62 2.62 2.62 2.62 2.62 2.62 2.62 2.6	X = 0.30 A ANGLE A 3.93 3.7.11 4.137 4.637 4.64.37 4.64.37 4.657 4.67 4.67 4.67 4.67 4.67 4.67 4.67 4.6	- 0.093 4 NGLE 3.45 3.47 3.47 4.76 4.76 4.76 4.76 4.76 4.76 4.78 3.70 3.12 2.86 2.01 2.10 3.10 3.10 3.10 3.10 3.10 3.10 3.10 3	AVSLE J 3.39 3.40 3.40 4.41 4.41 4.41 4.41 4.47 4.41 4.77 4.62 4.79 4.22 4.79 4.22 4.79 4.22 4.79 4.79 4.79 4.79 4.79 4.79 4.79 4.79	NGC.E A 3.331 3.361 3.361 3.361 3.371 4.97 4.91 4.97 4.91 4.97 4.97 4.97 4.97 4.97 4.97 4.97 4.97	MGLE ANGLE 3.4.3 3.4.3 3.4.3 3.4.3 3.4.4 4.37 4.5.9 4.52 4.5.4 4.5 4.5 4.5 4.5 4.5 4.5 4.5 4.5 4	AMGLE 3-135 3-35 3-36 4-30 4-46 4-33 4-46 4-33 4-46 3-36 4-33 4-33
VHITCHM A 7 0 170 0 125 0 126 0 12	X = 0.25 ANGLE A.05 A.60 A.07 S.07 S.07 S.07 S.07 S.07 S.07 S.07 S	x = 0.30 AMGLE 3.09 5.60 5.60 5.60 5.61 5.22 5.10 1.72 2.85 2.31 2.10 AMGLE 3.30 AMGLE 3.30 3.30 AMGLE 3.30	2=19.85 X = 0.35 ANGLE 3.92 4.17 4.51 5.40 5.42 5.40 5.42 5.40 5.42 5.25 4.90 3.17 2.17	DATA FOR ATI X Y G0 ANGLE 3-72 4-72 4-90 4-90 5-15 5-27 5-25 5-27 5-25 3-40 4-12 4-12 3-10 4-17 3-10 3-10 4-17 3-10 3-10 4-17 3-10	ANGLE 302 ANGLE 302 ANGLE 302 A51 A77 A98 5.10 5.110 5.110 347 A44 A11 346 A71 A98 A71 A72 A78 A78 A78 A79 A	X = 0.30 A ANGLE A 3.93 3.7.11 4.137 4.637 4.64.37 4.64.37 4.657 4.67 4.67 4.67 4.67 4.67 4.67 4.67 4.6	- 0.000 A NGLE 3.457 3.457 4.261 4.261 4.261 4.261 4.261 4.271 4.261 4.271 4.261 4.271 4.261 4.271 4.261 4.271 4.261 4.271 4.261 4.271	AVSLE J 3.39 3.40 3.40 4.41 4.41 4.41 4.41 4.47 4.41 4.77 4.62 4.79 4.22 4.79 4.22 4.79 4.22 4.79 4.79 4.79 4.79 4.79 4.79 4.79 4.79	NGC.E A 3.31 3.56 3.51 3.56 4.51 4.51 4.52 4.57 4.51 4.52 4.57 4.51 5.66 6.66 6.76 6.66 6.76 6.76 6.76 6.76	MGLE ANGLE 3.25 3.25 3.25 3.25 3.25 3.26 3.26 3.26 3.26 3.26 3.26 3.26 3.26	ANGLE 3-15 3-35 3-36 3-66 4-30 4-40 4-30 4-40 3-16 3-16 3-16 3-16 3-16 3-16 3-16 3-16
VHITCHM A 7 0 170 0 125 0 126 0 12	X = 0.25 ANGLE 4.05 4.05 4.05 4.07 5.02 5.02 5.02 5.02 5.02 5.02 5.03 5.02 7.04 1.02 1.03 1.04 1.05 1.06 1	X = 0.30 AMGLE 3.93 4.31 6.70 5.60 5.61 5.62 5.60 5.61 1.90 3.51 2.03 2.03 2.03 2.03 2.03 2.03 2.03 2.03	2=19.85 X = 0.35 ANGLE 3.82 4.17 4.51 5.30 5.42 5.40 5.42 5.40 3.17 2.27 2.39 3.17 2.31 1.77 ANGLE 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 2.31 3.00 3.17 3.00 3.17 3.00 3.00 3.00 3.00 3.00 3.00 3.00 3.0	DATA FOR ATI X * G.*G ANGLE 3.72 4.36 4.36 5.27 5.25 5.15 5.27 5.25 5.10 4.84 2.87 5.21 5.10 3.46 3.16 2.87 2.87 1.79 X * 1.00 1.79 X * 1.00 1.79 1.79 1.70	TY ANGLE 3.02 3.92 4.72 4.77 4.98 5.10 5.11 4.76 3.4.76 3	X = 0.50	- 0.553 4 NGLE 3.453 3.493 3.496 4.754 4.754 4.754 4.753 4.753 4.753 4.753 2.7	AVSLE J 3.39 3.40 4.10 4.10 4.10 4.10 4.10 4.10 4.10 4	NGC_E A 3.36 3.36 3.36 4.27 4.97 4.91 4.92 4.92 4.92 4.92 4.92 4.92 4.92 4.92	MGLE ANGLE 3.25 3.25 3.25 3.25 3.25 3.25 3.25 3.25	AMGLE 3-135 3-35 3-35 3-36 4-30 4-46 4-30 4-46 4-33 4-11 3-86 3-26 3-27 2-37 2-17 2-17 2-17 2-17 2-17 2-17 2-17 2-1
WHITCOMM A 7 0.1707 0	## 0.25 # 0.25 # 0.66 # 0.56 # 0.56 # 0.56 # 0.51 # 0.51 # 0.75 # 0.7	x x 0.30 x x 0.30 AMGLE 3.03 4.31 4.00 5.07 5.00 5.07 5.00 5.07 5.00 1.00 1.00 1.00 1.00 1.00 1.00 1.00	2=19.65 X = 0.35 ANGLE 3.92 4.17 4.18 5.19 5.15 5.40 5.425 4.01 4.23 3.00 4.01 4.23 3.00 2.31 1.70 X = 0.95 ANGLE 3.02 3.70 3.70 3.70 3.70 3.70 3.70 3.70 3.70	DATA FOR ATI 2 Y 0.40 3 Y 0.40 4 4.04 4 4.05 4 .06 4 .06 4 .07 5 .27 5 .27 5 .26 2 .07 2	ANGLE 302 ANGLE 302 A51 A77 A98 A77 A98 A77 A98 A74 A44 A44 A11 376 A78 A78 A78 A78 A78 A79 A78 A79	X = 0.50	- 0.553 4 NGLE 3.453 3.493 3.496 4.754 4.754 4.754 4.753 4.753 4.753 4.753 2.7	AVSLE J 3.39 3.40 4.10 4.10 4.10 4.10 4.10 4.10 4.10 4	NGC_E A 3.36 3.36 3.36 4.27 4.97 4.91 4.92 4.92 4.92 4.92 4.92 4.92 4.92 4.92	MGLE ANGLE 3.25 3.25 3.25 3.25 3.25 3.25 3.25 3.25	ANGLE 3-15 3-35 3-36 3-66 4-30 4-40 4-31 4-40 4-31 4-40 3-56 3-29 3-50 2-77 2-19 2-19 2-19 2-19 2-19 3-60 3-60 3-71 3-60 3-60 3-60 3-60 3-60 3-60 3-60 3-60
VMITCOMM A 7 0. 1700 0. 1254 0. 1700 0. 1254 0. 1700 0. 1254 0. 1700 0. 1256 0. 1700 0. 1256 0. 1700 0. 1256 0. 1700 0. 1256 0. 1700 0. 1256 0. 1700 0. 1256 0. 1700 0. 1256 0. 1700 0. 1256 0. 1700 0. 1256 0. 1700 0. 1256	X = 0.25 ANGLE A.05 A.05 A.07 S.07 S.07 S.07 S.07 S.07 S.07 S.07 S	x = 0.30 x = 0.30 AMGLE 3.03 4.31 5.00 5.07 5.00 5.01 7.00 7.00 7.00 7.00 7.00 7.00 7.00 7	2=19.85 X = 0.35 ANGLE 3.92 4.17 5.16 5.40 5.42 4.17 5.15 5.40 6.01 4.27 3.86 1.25 4.27 3.86 1.27 2.37 3.67 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.17 3.17 3.17 3.17 3.17 3.17 3.17	DATA FOR ATI X Y 0.40 ANGLE 3-72 4-30 5-17 5-27 5-25 5-27 5-25 5-27 5-26 4-104 4-104 4-104 4-104 4-107 3-46 3-1	ANGLE 302 4.51 472 473 475 510 511 376 444 411 376 411 4	X = 0.30 X ANGLE A 3.93 3.7.11 4.137 4.637 4.64.77 4.667 4.67 4.67 4.67 4.67 4.67	- 0.553 4 NGLE 3.453 4.70 4.70 4.70 4.70 4.70 4.70 4.70 4.70	AVGLE J J J J J J J J J J J J J J J J J J J	NGC.E A 3.331 3.56 3.371 3.56 4.57 4.57 4.57 4.57 4.57 4.57 4.57 4.57	MGLE ANGLE 3.25 3.25 3.25 3.25 3.25 3.25 3.25 3.25	ANGLE 3-15 3-35 3-36 3-66 4-30 4-40 4-31 4-46 4-33 4-48 3-16 3-16 3-17 2-77 2-17 2-17 2-17 2-17 2-17 2-17 2
VHITCOMM A 7 0. 170 0. 25 c 0. 27 c 0. 170 0. 0. 150 0.	X = 0.25 ANGLE A.05 A.05 A.07 S.07 S.07 S.07 S.07 S.07 S.07 S.07 S	x = 0.30 x = 0.30 AMGLE 3.03 4.31 5.00 5.07 5.00 5.01 7.00 7.00 7.00 7.00 7.00 7.00 7.00 7	2=19.85 X = 0.35 ANGLE 3.92 4.17 5.16 5.40 5.42 4.17 5.15 5.40 6.01 4.27 3.86 1.25 4.27 3.86 1.27 2.37 3.67 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.10 3.17 3.17 3.17 3.17 3.17 3.17 3.17 3.17	DATA FOR ATI 2 Y G.40 ANGLE 3-72 4-10 4-30 4-10	ANGLE 3.62 3.62 3.792 4.22 4.29 4.29 4.29 4.30 5.10 5.11 4.36 4.74 4.18 3.15 2.17 2.62 2.18 1.01 1.01 1.01 1.01 1.01 1.01 1.01	X = 0.50 X ANGLE A 3-53 A 3-73 A 4-10 A 4-17 A 4-67 A 4-68 A 3-73 A 4-81 A 2-87 A 4-88 A 3-13 A 3-14 A 3-15	- 0.000 A NGLE 3.457 3.477 4.261 4.261 4.261 4.363 4.271 3.102 2.861 2.2	AVGLE J J J J J J J J J J J J J J J J J J J	NGC.E A 3.331 3.56 3.371 3.56 4.57 4.57 4.57 4.57 4.57 4.57 4.57 4.57	MGLE ANGLE 3.43 3.43 3.43 3.43 3.49 3.49 3.40 4.31 4.59 4.50 4.50 4.50 4.50 4.50 4.50 4.50 4.50	ANGLE 3-15 3-35 3-36 3-36 4-30 4-40 4-30 4-40 3-56 3-29 3-60 2-29 2-27 2-19 2-02 1-96 ANGLE 2-77 2-19 2-02 1-96 ANGLE 2-77 2-19 2-02 1-96 ANGLE 3-71 3-83 4-02 3-83
VHIT COMM A 7 0. 170 0. 120 c. 120	X = 0.25 ANGLE 4.05 4.05 4.05 5.07 5.07 5.07 5.07 5.07 5.07 7.09 1.02 2.07 2.07 2.07 2.07 2.07 2.07 2.07 3.02 2.07 2.07 2.07 2.07 2.07 3.02 2.07 2.07 2.07 3.02 3.03 3.02 3.03 3.03 3.03 3.04 3.04 3.05 4	x = 0.30 AMGLE 3.93 4.31 6.70 5.60 5.61 5.60 5.61 7.72 7.80 7.80 7.80 7.80 7.80 7.80 7.80 7.80	2=19.85 X = 0.35 ANGLE 3.92 4.17 4.51 5.15 5.40 5.42 4.07 3.80 7.20 3.10 7.20 7.20 7.20 7.20 7.20 7.20 7.20 7.2	DATA FOR ATI X * 00 ANGLE 372 A.30 490 490 5.15 5.27 5.25 5.27 5.25 3.40 4.17 3.42 3.16 3.	ANGLE 3.62 3.62 3.7.92 4.72 4.77 4.98 4.77 4.98 4.77 4.98 4.78 4.78 4.11 3.78 3.45 3.45 3.45 3.45 3.45 3.45 3.45 3.45	X = 0.30 X ANGLE A 3.33 7.71 4.127 4.62 4.64 4.97 4.64 4.97 4.65 4.67 4.67 4.67 4.67 4.67 4.67 4.67 4.67	- 0.000 A NGLE 3.457 3.477 4.261 4.261 4.261 4.363 4.271 3.102 2.861 2.2	AMSLE J J.39 3.49 4.10 4.10 4.10 4.10 4.10 4.10 4.10 4.10	NGC.2 A 3.36 3.36 3.36 4.37 4.97 4.91 4.92 4.97 4.91 4.92 4.97 4.97 4.97 4.97 4.97 4.97 4.97 4.97	MGLE ANGLE 3.25 3.25 3.25 3.25 3.25 3.25 3.25 3.25	ANGLE 3-15 3-35 3-36 3-36 4-30 4-40 4-30 4-40 3-56 3-29 3-60 2-29 2-27 2-19 2-02 1-96 ANGLE 2-77 2-19 2-02 1-96 ANGLE 2-77 2-19 2-02 1-96 ANGLE 3-71 3-83 4-02 3-83
VHITCOMM A 7 0. 170 0. 25 c 0. 27 c 0. 170 0. 0. 150 0.	# = 0.25 # = 0.25 # ANGLE # -0.5 # -0.5 # -0.5 # -0.5 # -0.75 # -0.	x = 0.30 x = 0.	2=19.85 X = 0.35 ANGLE 3.82 4.17 4.51 5.30 5.42 5.40 5.42 6.07 1.50 3.17 2.31 1.77 ANGLE 3.00 3.17 2.31 1.77 ANGLE 3.00 3.17 2.31 1.77 ANGLE 4.00 3.17 2.31 1.77 ANGLE 4.00 3.17 3.00 3.17 2.31 1.77 ANGLE 4.00 3.17 3.00 3.17 3.10 3.10 3.10 3.10 3.10 3.10 3.10 3.10	DATA FOR ATI X * G.+G ANGLE 3.72 4.06 4.16 5.17 5.27 5.25 5.10 4.84 6.17 6.10 7.10	TY ANGLE J.02 J.02 A.27 A.20 A.27 A.30 S.10 S	X = 0.50	- O. DD 3 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	AVSLE J 3.494 3.494 4.194 4.194 4.194 4.194 4.194 4.194 4.197	NGC. 2 A 3.331 3.336 3.331 3.336 4.377 4.311 4.372 4.377 4.371 4.372 4.372 4.373 3.374 3.374	MGLE ANGLE 3.25 3.25 3.25 3.25 3.25 3.25 3.20 3.20 3.20 3.20 3.20 3.20 3.20 3.20	AMGLE 3-135 3-35 3-36 4-30 4-46 4-30 4-46 4-30 4-46 3-36 4-37 2-37 2-17 2-17 2-102 1-50 AMGLE 2-97 3-18 3-88 3-88 3-88 3-88 3-88 3-88 3-88
VHITCHM A 7 0. 170 0. 225 0. 276 0. 150 0.	X = 0.25 ANGLE 4.05 4.05 4.05 5.07 5.07 5.07 5.07 5.07 5.07 7.09 1.02 2.07 2.07 2.07 2.07 2.07 2.07 2.07 3.02 2.07 2.07 2.07 2.07 2.07 3.02 2.07 2.07 2.07 3.02 3.03 3.02 3.03 3.03 3.03 3.04 3.04 3.05 4	x = 0.30 AMGLE 3.09 4.31 4.70 5.60 5.60 5.61 5.22 4.10 4.10 4.10 1.00 1.72 2.05 2.31 2.00 1.72 3.00 4.10 4.	2=19.85 X = 0.35 ANGLE 3.92 4.17 4.51 5.40 5.42 5.40 5.42 5.25 4.90 4.23 1.70 2.17 2.59 2.17 2.19 1.70 X = 0.95 ANGLE 3.70 3.70 3.70 3.70 3.70 3.70 3.70 3.70	DATA FOR ATI 2 Y 0.40 3 Y 0.40 4 4.04 4 4.06 4 .06 4 .07 5 .12 7 5.22 7 5.22 7 5.22 7 1.20 8 4.52 4 1.52 4 1.52 4 1.52 4 1.52 4 1.52 4 1.52 4 1.52 4 1.52 4 1.52 4 1.52 4 1.52 4 1.52 4 1.52 4 1.52 4 1.53 1 1.79 X = 1.00 1 1.79 X = 1.00 1 1.79 X = 1.00 3 1.42 4 1.52 4 1.53 4 1.53 4 1.53 5 1.77 5 1.50 5 1.77 5 1.70	AMGLE 362 AMGLE 362 A-51 A-77 A-98 A-77 A-98 A-77 A-98 A-74 A-44 A-44 A-74 A-74 A-74 A-74 A-74	X = 0.50	- NGL 2 - N	AVSLE J 3.34 3.35 3.36 3.36 4.10 4.10 4.10 4.10 4.10 4.10 4.10 4.10	NGC.E A 3.331 3.361 3.361 4.917 4.91	MGLE ANGLE 3.25 3.25 3.25 3.25 3.25 3.25 3.25 3.25	AMGLE 3-15 3-35 3-36 3-36 4-39 4-40 4-31 4-11 3-16 3-29 3-29 2-79 2-79 2-19 2-02 1-96 AMGLE 2-77 2-10 2-02 1-96 AMGLE 2-77 3-10 3-83 4-15 4-11 3-84 3-83 4-02 4-11 3-83 4-12 3-83 4-02 4-11 3-83 3-93 3-93 3-93 3-93 3-93 3-93 3-93

Figure A-3. Continued.

z	X = 1.45	X = 1.50	X = 1.55	X = 1.60	X = 1.68	x = 1.70	X = 1.75
	ANGLE	ANGLE	ANGLE	ANGLE	ANGLE	AMBLE	ANGLE
0.300	2.75	2.74	2.72	2.70	Z.69	2.67	2.66
0-250	2.95	2.93	2.91	2.49	2.50	2.86	2.84
0.230	3.10	3.13	3.11	3.09	3.68	3.06	7.04
0.150	3.37	3. 35	3.33	3.31	3.29	3.27	3.25
0.198	3.59	3.57	3.55	3.52	3.50	3.48	3.46
0.030	3.91	3.78	3.76	3.74	3.72	3.76	3.66
-0.000	4.00	3.97	3.95	3.93	3.71	3.09	3.67
-0.050	4-17	4-11	4.49	4.07	4-05	4.03	4.02
-0.100	4.17	4.15	4.14	4.13	4.11	4.10	4.69
-0.150	4.10	4. 07	4.08	4.08	4.67	4.86	4.06
-0.200	3.94	3.93	3.93	3.43	3,93	3.92	3,92
-0-250	3.71	3.71	3.71	3.71	3.71	3.71	3.71
-0.302	3.45	3.45	3.45	3.46	3.46	3.46	3.46
-0.350	3.19	7.19	3.19	3.19	3.20	3.20	3.20
-0.400	2.94	2.94	2.94	2.74	2.94	2.95	2.95
-0.450	2.71	2.71	2.71	2.71	2.71	2.71	2.71
-0.500	2.50	2.50	2.50	2.50	2.50	2.50	2.50
-0.550	2.31	2.30	2.30	2.30	2.70	2.30	2.30
-0.600	2.13	2.13	2.13	2.12	2.12	2.12	2.12
-0.650	1.97	1.97	1.97	1.97	1.90	1.74	1.76
-0.630	1.03	1.02	1.62	1.02	1.02	1.02	1.25

DOMMAN	INFORMATIC	N FOR THE	REGATIVE X	-ARIS AT 1	HE PLANE C	SYMMETRY	. Y=0				
#H TCOMB	AIRFOIL CL	-1.2217	2-19-85	DATA FOR A	TLIT						
2	x=-0.256	x=-0.306	X=-0.356	X =-0.406	K=-0.456	x=-0.504	x=-0.356	x=-0.506	X0.656	X=-0.706	x=-0.758
-	ANGLE	ANGLE	ANGLE	ANGLE	ANGLE	ANGLE	AMGLE	ANGLE	ANG. T	ANGLE	ANGLE
0.295	0.20	-0.62	-1-15	-1.42	-1-51	-1.50	-1.43	-1.34	-1.24	-1.14	-1 - 05
0.245	-0.31	-1.38	-1.91	-2.07	-5:03	-1.01	-1.74	-1.56	-1.42	-1.28	-1-14
0.195	-1.40	-2.79	-3.04	-2.92	-2.65	-2.34	-2.06	-1.51	-1.50	-1.41	-1 - 26
0.145	-1.97	-5.00	-4-60	-3.92	-3.29	-2.76	-2.35	-2.0t	-1.74	-1.52	-1-34
0.095	-10.41	-6-45	-6.33	-4-84	-3.62	-3.09	-2.56	-2.16	-1.94	-1.59	-1.39
0.045	-20.55	-11.25	-7.38	-5.33	-4.08	-3.24	-2.65	-2.22	-1.99	-1.62	-1-41
-0.025	-15.24	-10-00	-6.93	-5.12	-3.96	-3-10	-2.51	-2.19	-1.40	-1.61	-1.40
-0.055	-6.07	-6.38	-5.35	-4.33	-3.52	-2.91	-Z.44	-2.07	-1.78	-1.55	-1.38
-0.125	-2.15	-3.50	-3.63	-3.31	-2.90	-2.51	-2.17	-1.R9	-1.55	-1.45	-1.29
-0.155	-9.55	-1.78	-2.29	-2.37	-2.25	-2.04	-1.86	-1.66	-1.40	-1.37	-1-19
-0.133		1			-1.40	-1-41	-1.84	41.42	-1-10	-1.19	-1.08

Figure A-3. Continued.

APPENDIX B - WAKE PROGRAM

User Instructions

The program is written in FORTRAN IV and is designed to run in double precision on an IBM 370-165 computer. Using a finite difference technique this program evaluates the velocity profile downstream of a wing trailing edge given the upper and lower surface profile shapes at the wing trailing edge. All the input information can be obtained from the two-dimensional airfoil program in Reference 4. Using 1601 points in the η or normal direction with an initial stepsize of .00005 in $\xi(x/c)$ and an increment in stepsize of .05, an average execution time of 2 minutes and 42 seconds was required to integrate the boundary layer equations downstream two wing chord lengths. The program requires the specification of the following input data:

<u>Card</u> Number	Variable Name	<u>Variable</u> <u>Description</u>
1	TITLE	The 80 character array which is used as a header to identify output. Termination of execution is achieved by following the last set of profile data to be analyzed by a title card having only the word END in the first three spaces.
2	DETA	Stepsize in the η -direction. A value of .00125 was found satisfactory for most cases, and using this value with a constant stepsize, the total number of η -points, NPTS, can be estimated using the equations given in the text.
2	DX	Stepsize in the X-direction. Best results were obtained for cases analyzed in this report using a very small stepsize, .00005 (specified in chords), and unequal spacing using the variable DXSTEP on card 3.
3	X(1)	The station in chords at which the initial velocity profile solution is assumed. A value of .01 was found satisfactory for most wake solutions.
3	CEDDY	A constant used to evaluate the eddy viscosity model required to solve for the velocity profile. A value of .03 correlated best with experimental data.
3	Т	The thickness at the spanwise station of interest in chords.
3	CD	The drag coefficient at the spanwise station of interest.
3	CDMIN	The minimum drag coefficient of the wing section at the spanwise station of interest.

<u>Card</u> Number	<u>Variable</u> <u>Name</u>	<u>Variable</u> <u>Description</u>
3	DXSTEP	Stepsize increment in the X-direction. The stepsize in the X-direction is increased by the factor $DX_{step\ n} = (DX_{step\ n})(1 + DXSTEP)$. A table is given in Figure 30 which will help in determining the X-value at any station using unequal step increments of .05, .075, and .10.
4	NXPRNT	The NXPRT station numbers at which the user desires to have the velocity profile printed. The maximum number of stations which may be printed is 20 unless the solution is printed at every station (NXPRT=0 and all values of NXPRNT are specified as 0). The station number corresponds to a specific value of X downstream; if equal stepsize in the X-direction is used then the NXPRNT values at the desired X-station are easily calculated. However, for unequal stepsize which is the more useful case Figure 30 will help in determining the step number nearest the X-station at which the velocity profile is desired. The NXPRT values of NXPRNT are read using a 2014 format. If only two stations were of interest then only columns 1-4 and 5-8 would contain integers representing the station numbers. The stations must be specified in the order of increasing station number.
5	DELTAU	The boundary layer thickness in chords at the trailing edge on the upper surface at the station of interest.
5	DELTAL	The boundary layer thickness in chords at the trailing edge on the lower surface at the station of interest.
5	HÜ	Form factor on the upper surface at the station of interest = boundary layer displacement thickness divided by the momentum thickness at the trailing edge.
5	HL	Form factor on the lower surface at the station of interest = boundary layer displacement thickness divided by the momentum thickness at the trailing edge.

Cards 1 through 5 represent a complete data set for the WAKE Program. Several data sets may be executed for a single program compile by placing subsequent data sets behind the first. The entire program execution is terminated when the END title card is encountered. The format specification for the above data is given in Figure B-1. A sample data set is given in Figure B-2, and the output of this data set is presented in Figure B-3.

- + 	2 31 32 33 34 35 36 37 38 39 40 41 42 43 44,46 46 47 48 49 T.T.T.T.E.	9 50 51 52 53 54 56 56 57 58 59 60 81 62 63 64 66 65 67 68 69 70 71 72 73 74 76 76 77 70 70 60
I 10 I 1	N.X.P.R.T. A.K	F10.5 F10.5 F10.5
CEDDY T	F.1.05 F.1.05	DXSTEP.
NXPRNT(I), I-1, NXPRT		
DELTAU DELTAL HU F10.5 F10.5 F10.5 1.2345678910.1112131415161718192021222124252627282930	H, L, F, 1, O, ., 5	8 50 51 52 53 54 55 55 75 58 58 60 61 52 63 64 65 65 67 68 68 76 71 72 73 74 75 76 77 76 78 76 78 76 76

Figure B-1. Format specification of input data for the WAKE program.

Ę	ND	. 4 7 1	9 10 11	17 13 14	15 16 17	10 19 20	21 27 2	3 24 25	26 27 2	29 30	31 22 23	34 35 36	37.36	33 49 4	11 42 4	2 4 45	46 47	404	0 51 52 5	1985	6 57 58 ·3	សពខ	ยผล	40	La	:8t	: C	ar	1
/	DEL	TAU		DE	LTA	L	_	HU	_			HL	_									-							
•	9 243	P 7 P	ם ה ה ה ה	724	287	PO 20	n n n	13	9 D O	29 30 3	נע עוו	139 * 15 K	PQ	39 40 41	142 0	. 4 45	46 47 4	E 19 50	51 57 5	54 55 5	5 57 58 59	60 61 62	ឆ អ ស	66 67 E	69 /0	11 12	nn	15/5	. 7 78 79
		NT(128					21 27 21	1 24 25	% 27 ZI	29 30 3	נענ	N 35 %	37 38	37 44 (1	1424	4 45	46 17 4	4 +9 50	51 52 5	1 24 25 24	5 5/ 58 59	60 E3 E2 I	U 64 65 4	66 67 64	s 69 70	11111		15 /6	וו וו
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		NP	TS		NI	ETA	PT		NX	STI	ΕP		N	XPE	lT.	AK				EI	P S		DE	TA	- ,-			DX	
ı	2 3 4 5	,] 6	01 , 10 11	17 13 14 1	15 16 12 T	20) 21 22 2:	3 24 25	x 21 71	56	נניגוו	u n m	37 38	4	1 42 43	. D	Ď.,	4 49 50	ر د به اد	999) Do	សព ដំ	DOI:	25 D	10 /0	กก็	90	00	Ş D Q
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	2 2 2 2	2 2 2											11	111	3 3	3 3	1 3	6	3			291			3 3	3 3	1 3	3 3	3 3 3
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3 4 5	3 3 3 3 4 4 4 4 5 5 5 5 6 6 6 6	3 3 3 4 4 4 5 5 5 6 6 6	3 3 3 3 4 4 4 4 5 5 5 5	4 4 4 4 5 5 5 5 6 6 6 1	4 4 4 4 5 5 5 5 6 6 6 6	4 4 4 5 5 5 6 6 6	4 4 4 5 5 5 6 6 6	4 4 4 5 5 5 6 6 1	4 4 4 5 5 5 6 6 6	4 4 4 5 5 5 6 6 8	1 4 4 5 5 5 6 6 6	4 4 4 5 5 5 6 6 6	4 4 5 5 6 6	4 4 4 5 5 5 6 6 6	5 5	5 5 5	5 5		COM	-	ING		TER	2	5 6 6	5 5 6 6	5 5 6 6	5 5 6 6	5 5 5
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Figure B-2. Example data set for the WAKE program.

Program Listing

	USING A FINITE DIFFERENCE METHOD THIS PROGRAM CALCULATES THE 2-0	FIN	ı	WRITE (IWRITE.35) AK.EPS.DETA.DX.X(I).CEDDY.812.T.UMUDEL.CD.DXST	F11	N 62
	VELOCITY PROFILE IN THE WAKE OF AN AIRFOIL GIVEN THE BOUNDARY	FIN	2	1.C1 35 FORMAT (5x-0HAK = .D15.8-/5X-9HEPS = .D15.8-/5X-9HDETA	= F11	
	LAYER INFORMATION ON THE UPPER AND LOWER SURFACES OF THE AIRFOIL	FIN	3	TO THE PARTY OF TH	= F11	
C+++	AT THE TRAILING EDGE.	FIN	4			
	IMPLICIT REAL+8(A-H, 0-Z)	FIN	5		= F1	
	COMMON A.B.C.R.X(300).F(2001.3).W(2001.3).WOLD(2001).CAPE(2001).SM		6		FI	
	IALE(2001);ETA(2001);WALBC;QEBC;AK;Dx11;Dx12;Dx13;88;C1;1TER;NXS;N;		7	1,015.8//)	FI	
	INPTS.NEND	FIN	8	WRITE (IWRITE.40) DELTAU.DELTAL.HU.HL 40 FORMAT (5X.9HDELTAU = .D15.8,/5X.9HDELTAL = .D15.8,/5X.9HHU	= FI	
	DIMENSION TITLE(20).NXPRNT(20)	FIN	9		FI	
	DATA END/4HEND /	FIN	10	1.D15.8./5x.9HHL = .D15.8//)	FL	
	[READ=1	FIN	11	C+++ CALCULATE ETA(1)	FI	
	IPUNCH=2		12	ETA(NMID)=0.00	FI	
	IWRITE=3		13	ETA(NMID-1)=-DETA		N 74
	READ TITLE CARD		14	ETA(NMID+1)*DETA	FI	
	READ (IREAD-10) (TITLE(I)-1=1-20)	FIN	15	J=MMID-1	FI	
10	FORMAT (20A4)	FIN	16	JJ=NMID+2		N 77
	IF (TITLE(I).EQ.END) GO TO 170		17	DO 45 I=JJ. NPTS	FI	
C***	INPUT BASIC CONSTANTS		18	J≖J-1 ETA([)=ETA([-1)+AK+(ETA([-1)-ETA([-2)]	FI	
Cess	NPTS=NUMBER OF ETA POINTS DESCRED		19		FI	
Cess	NETAPT=NUMBER OF STEPS BETWEEN ETA POINTS PRINTED	FIN	20	45 ETA(J)=-ETA(I)	FI	
Ceee	NXSTEP+NUMBER OF STEPS IN X DIRECTION	FIN	51	DO 50 I=1.NPTS		SE N
C+++	NXPRT=NUMBER OF STATIONS AT WHICH SOLUTION IS TO BE PRINTED	FIN	22	F(1.2)=0.0D0	Fi	
C+++	(NXPRT=0 PRINTS EVERY SOLUTION AT EVERY STATION)	FIN	23	F(1.3)=0.000	FI	
Ceee	(THERE IS A MAXIMUM OF 20 STATIONS)	FIN	24	¥(1.2)=0.000	FI	
C***	(THE FIRST STATION IS ALWAYS PRINTED)	FIN	25	50 w([.3)=0.000 00 55 t=2,300	-	N 86
C+++	(THE STATIONS MUST BE SPECIFIED IN ORDER OF INCREASING	FIN	26	1F (1.EQ.2) GO TO 55	FI	
C	STATION NUMBER)	FIN	27	Dx=Dx*(1.D0+DxSTEP)	FI	
C+++	T=THICKNESS TO CHORD RATIO OF WING	FIN	29		FI	
C***	812=WAKE WIDTH FACTOR	FIN	29	55 X(I)=X(I-1)+DX C+++ INITIAL PROFILE GUESS	Ft	
Cass	UNUDEL=VELUCITY DEFICIT FACTOR	FIN	30	CU=(HU-1.00)/2.00	FI	N 91
Ceee	CK=CONSTANT USED IN EDDY VISCOSITY MODEL	FIN	31	CL=(HC-1+D0)/2+D0	FI	IN 92
C+++	And the control of th	FIN	32 33	DELTAU=DELTAU/DSQRT(T+X(NXS)+100+D0+CD)	FI	N 93
C***	EPS=ACCURACY FOR SOLUTION CONVERGENCE	FIN	33	DELTAL=DELTAL/DSORT(T+X(NXS)+100+00+C0)	FI	
Cees	DETA-INITIAL STEPSIZE IN ETA DIRECTION	FIN	15	CALL PROFIL (DELTAL. DELTAL. CU.CL. DETA. NMID)	FI	N 95
C+++	DX=STEPSIZE IN X DIRECTION (INPUT AS RATIO TO CHORD LENGTH)	FIN	36	OG 60 I=1.NPTS	FI	IN 96
	READ (IREAD. 15) NOTS. NETAPT. NXSTEP. NXPRT. AK. EPS. DETA. DX			60 #OLD(I)=#([-1)	FI	IN 97
15	FORMAT (4110,4F10.5)	FIN	37 38	65 [F (NXS-2) 75,75,70	FI	IN 98
	READ ([READ.20] X(1).CEDDY.T.CD.CDMIN.DXSTEP	FIN	39	70 DX11=((1.0D0/(X(NXS)-X(NXS-1)))+(1.0D0/(X(NXS)-X(NXS-2))))	FI	IN 99
20	FORMAT (8F10+5)	FIN	40	Dx12=(x(nxs)-x(nxs-2))/((x(nxs)-x(nxs-1))*(x(nxs-1)-x(nxs-2)))	FI	N 100
	NXPRT1=HXPRT	FIN	41	Dx13=(x(Nx5)-x(Nx5-1))/((x(Nx5)-x(Nx5-2))+(x(Nx5-1)-x(Nx5-2)))	FI	IN 101
	IF (NXPRT.EQ.O)NXPRTI=1	FIN	42	75 CONTINUE	FI	IN 102
	READ (IREAD.25) (NXPRNT(I).I=I.NXPRT1)		43	F(NMID-1)=0.D0	FI	ED 103
25	FQRNAT (2014)	FIN	44	C*** START SOLUTION AT FIRST STATION		IN 104
	READ (IREAD+20) DELTAU+DELTAL+HU+HL	FIN	45	ITER=1	F.	IN 105
	NEND=NPTS-1	FIN	46	80 N=1		IN 106
	INXPRT*1	FIN	47	CALL GETF(NMID)	FI	IN 107
C+++	SET OUTER EDGE BOUNDARY CONDITION AT 1.0	FIN	48	IF (NXS,EQ.1) GO TO 110	FI	IN 106
	OEBC=1.0D0	FIN	4.9	85 N=N+1	FI	IN 109
	PU=2.D0/(HU-1.D0)	FIN	50	COOO CALCULATE MATRIX CUEFFICIENTS	F)	IN 110
	PL=2.D0/(HL-1.D0)	FIN	51	CALL ABCR	FI	IN 111
	812=.5D0+(.7500+PU+DELTAU+.75D0++PL+DELTAL)	FIN	52	CALL COEFF	FI	IN 112
	UMUDEL=(CO-CDMIN)/CD	FIN	52	[# (N-NEND) 85.90.90		IN 113
	C1=T+CD+100.D0/(812+CEODY+(1.D0-UMUDEL))	FIN	54	C*** CALCULATE NEW W ARRAY PROFILES	FI	IN 114
	NXS=1	FIN	55	90 CALL SOLVE	FI	IN 115
	NNID=(NPTS-1)/2+1		56	CARE TEST FOR CONVERGENCE OF SCCESSIVE PROFILES	FI	IN 116
	WRITE (IWRITE.30) (TITLE([].[=1.20].NPTS.NMID.NETAPT.NXSTEP.NXPRT.	FIN	57	DO 95 1=2, NEND	FI	IN 117
	I(NXPRNT(I), I=1, NXPRTI) FORMAT (IH1.//5x.2044.//5x.9HNPTS = .14./5x.9HNMID = .14./5x.5		58	(F (DABS(1.0D0-(#QLD([]/#([.1]))-EPS) 95.95.100	FI	IN 118
30	FORMAT { 1H1, //5x, 20A4, //5x, 9HNPTS = .14, /5x, 9HNMID = .14, /5x, 9HNETAPT = .14, /5x, 9HNXPRT = .14, /5x, 9HNXPRT = .14, /5x, 9HNXPRT = .14, /5x, 9HNXPRT			95 CONTINUE	FI	IN 119
		FIN	60	COOR CONVERGENCE ATTAINED	FI	IN 120
	1 .20[4//)					

	GO TO 110	FIN			- INL-0-00	SE T	7
C***	CONVERGENCE NOT ATTAINED-ITERATION SOLUTION	FIN			- 140-0400	SET	8
100		FIN	153		33-44(04)		9
	1F (!TER.GT.99) GO TO 160	FIN			J-4810	SE T	
		FIN			335-3 2		11
	DO 105 1=1.NPTS	FIN			Weight and and		12
	AOFD(1)=A(1'1)	FIN			00 3 1-00 pm-15-1	GET GET	13
105		FIN			Thos more period and a second	GET	
		FIN		5	, (1117-1110		
C+++		FIN			55 10 1-11555		16
110		FIN			J-J-1		17
		FIN				GE Y GE T	19
	IF (NXS.EQ.NXPRNT([NXPRT)) GO TO 115	FIN					
		FIN			F(NPTS.1)=F(NEND.1)+(W(NPTS.1)+W(NEND.1))*(ETA(NPTS)-ETA(NPTS-1))/		
115	WRITE (IMPITE, 135) ITER	FIN			2.00		21
	WRITE (IMRITE,120) HXS.X(HXS)	FIN				GET	
1 20	FORMAT (/10x.23HRESULTS FOR X/C STATION.14.5X.4HX = .D15.8)	FIN				GET GET	
	WRITE (IWR(TE,125) (TITLE(I),I=1,20)		138		END	GEI	2.
125	FORMAT (/-1X-20A4-/)	FIN					
	WRITE (IWRITE,140)		140				
	CYETA=DSQRT(T*x(NX5)+100.D0+CD)		141				_
	L=NPTS+NETAPT	FIN	142			ABC	1
	OO 130 I=1.NPTS.NETAPT		143			ABC	
	L=L-NETAPT		144			ABC	3
	YETA=ETA(L) CYETA		145		COMMON A.B.C.R.X(300).F(2001.3).W(2001.3).WOLD(2001).CAPE(2001).SM		•
	A20=A([*1)*A([*1)		146		ALE(2001).ETA(2001).WALBC.DEBC.AK.DX11.DX12.DX13.BB.C1.ITER.MXS.N.		5
	WRITE ([WRITE,[45] ETA(L).W(L.1).F(L.1).YETA.WSO		147			ABC	6
1 30	CONTINUE		145			ABC	7
	IF (NXS.NE.1)INXPRT=INXPRT+1		149			ABC	8
	IF (NXPRT.NE.O.AND.INXPRT.GT.NXPRT) GO TO 5		150			ABC	9
1 35	FORMAT (IHI-/-10%-26HCONVERGENCE ATTAINED AFTER-14-11H ITERATIONS)	FIN	151	C+++		ABC	
	l .		152			ABC	
140	FORMAT (/6x,3HETA,12x,6HU/UDEL,13x,1HF,14x,3HY/C,9x,11H(U/UDEL)**2	FIN	153	5		ABC	
	1)		154			ABC	
	FORMAT (5016.8)		155			ABC	
	SET UP FOR NEXT X STATION		156			ABC	
150	00 155 I=1.NPTS		157			ABC	
	#(1.3)=#(1.2)		156			ABC	
	F(1.3)=F(1.2)		159			ASC	
	A([°5)=A([°1)		160		ALPHA(1)=(F(N.1)/2.D0+X(NXS)+(F(N.1)-F(N.2))/(X(NXS)-X(NXS-1)))+C1		
	F(1,2)=F([,1)		161			ABC	
	AOF0413-A444-13		162			ABC	
155	CONTINUE		163		B=-2.0D0*{1.0D0+AK}/D2-{1.0D0-AK*AK}*ALPHA(1)/D1+ALPHA(2)/(X(NXS)-		
	NX S=NX 5+ 1		164			ABC	
	[F (NXS-2.GE.NXSTEP) GO TO 5		165			ABC	
	GO TO 65		166			ABC	
160	WRITE ([WRITE.165) NXS	FIN	167			ABC	
165	FORMAT (/.5x.JOHITER EXCEEDS 75 AT STEP NXS # +14)	FIN	168	15	ALPHA(1)=(F(N.1)/2.D0+X(NXS)*(DX11*F(N,1)-DX12*F(N,2)+DX13*F(N.3))		
	GD TO 5		169			ABC	
170	CALL EXIT	FIN	170	li .		ABC	
	END	FIN	171			ABC	
						ABC	
						ABC	
						ABC	
	SUBROUTINE GETF(NMID)	GE T				ABC	
C***	THIS SUBROUTINE INTEGRATES THE DERIVATIVE OF F TO OBTAIN F	GET			END	ABC	35
	IMPLICIT REAL #8 (A-H, O-Z)	GE T					
	COMMON A.B.C.R.X(300).F(2001,3).W(2001.3).WOLD(2001).CAPE(2001).SM						
	1ALE(2001), ETA(2001). WALBC. DEBC. AK. DX11, DX12, DX13, BB. C1. ITER, NXS. N.	GET	5	i			
	INPTS. NEND	GET	6	•	SUBROUTINE COEFF	COF	1

5 10	COEFF COMPUTES RECURSION COEFFICIENTS FOR TRIDIAGIONAL MATRIX SYSTEMS IMPLICIT REAL-94(A-H-0-Z) COMMON A-8-C-R-X(300)+F(2001-3)+W(2001-3)+W0LD(2001)+CAPE(2001)+S-M ALE(2001)+ETA(2001)+WALBC-0DEBC-AK-DX11-DX12-DX13-88-CI-TER-NXS-N-N-N-N-N-N-N-N-N-N-N-N-N-N-N-N-N-N		2 3 4 5 6 7 8 9 10 11 12 13 14 15
5	SUBROUTINE SCLVE THIS SUBROUTINE SOLVES A TRIDIAGIONAL MATRIX SYSTEM BY BACK-SUBSTITUTION IMPLICIT REAL-84(A-H.O-2) COMMON A-8.C-R.X.(3001).F(2001-3).W(2001-3).WOLD(2001).CAPE(2001).SM LALE(2001).ETA(2001).WALBC.OEBC.AK.DX11.DX12.DX13.98.C1.ITER.NXS.N. IMPTS.NREN N=N+1 W(N.1)=OEBC NWM-1 W(N.1)=OEBC NWM-1 If (N-2) 10.10.5 W(1).1)=OEBC	50L 50L 50L 50L 50L 50L 50L 50L 50L 50L	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
5	SUBROUTINE PROFIL(DELTAU, DELTAL, CU, CL, DETA, NMID) THIS SUBROUTINE EVALUATES THE INITIAL VELOCITY PROFILE FOR THE FINITE DIFFERENCE SOLUTION GIVEN THE BOUNDARY LAYER THICKNESS AND FORM FACTOR FOR BOTH UPPER AND LOYER SURFACES IMPLICIT REAL-8/14-H,O-2) COMHON A. B.C.R.X.(3001).*WALBC.OEBC.AK.OX11, DX12, DX13, DB.C1.ITCR.NKS, N. INDTS.NEDD NSTART#MNID DELETA—DETA OD 10 IMPSTARTS.NPTS DELETA—DELTA OD 10 IMPSTARTS.NPTS DELETA—GLETA/DETA IF (OELETA/GE.DELTAU).**CU GU TO 10 E(1.1)=1.0C CONTINUE DELETA—ODD NEND=NSTART-1 NCNT=NSTART NCNT=NSTART NCNT=NSTART OC 20 1=1.NNEND NCNT=NCNT-1 DCLETA-ODD NCNT=NCNT-1 COLETA-ODETA IF (OELETA-ODETA IF (OELETA-OD		12345678910112314516171692021223425

	GO TO 20
15	#(NCNT.1)=1.D0
20	CONT INUE
	RETURN
	END

PRO 26 PRO 27 PRO 28 PRO 29 PRO 30



Sample Output

```
JOUKCUSKI AIRFOIL/A=0/RN=.21/FREE TRANSITION/M=.05/CEODY=.03/
               NPTS = 1601
NM10 = 801
NETAPT = 20
NASTEP = 156
NAPPRT = 13 128 136 157
AK = 0.10000000D-01
EPS = 0.1000000D-02
OK = 0.2500000D-02
OK = 0.5000000D-01
CEDDY = 0.3000000D-01
                                                                 R12 = 0.60486614D-02
T = 0.118000000 00
UMUDEL = 0.0
C0 = 0.10378000D-01
OXSTEP = 0.5000000D-01
C1 = 0.674862270 03
              CONVERGENCE ATTAINED AFTER 1 ITERATIONS
RESULTS FOR X/C STATION 1 X # 0.10000000D-01
  JOUKCESK! AIRFOIL/A=0/RN=.21/FREE TRANSITION/P=.05/CEDDY=.03/
```

Figure B-3. Sample output of the WAKE program.

CONVERGENCE ATTAINED AFTER A ITERATIONS RESULTS FOR X/C STATION 113 X = 0.24515737D 00 JOUKOVSKI AIRFOIL/A=0/RN=.21/FREE TRANSITION/M=.05/CEODY=.03/

ETA	U/UDEL		r	Y/C	(U/UDEL)++2
0.100000000 01	0-10000000D	01	0.98000460D 00	0.17326878D 00	0.10000000D 01
0.97500000D 00	0.100000000	Q i	0.955004600 00	0.16893706D 00	0.100000000 01
0.9500000D 00	0.100000000	01	0.9300046UD 00	0.16460534D 00	0.1000000000
0.92500000D 00	0.10000000D	01	0.90500460D 00	0.160273620 00	0.100000000 01
	0.100000000	01	0.880004600 00	0.155941900 00	0.1000000000 81
0.900000000 00					
0.87500000D 00	0.100000000	01	0.85500460D 00		0.10000000D 01
0.850000000 00	0.1000000D	01	0.830004600 00	0.14727846D 00	0.10000000D 01
0.82500000D 00	0.100000000	01	0.605004600 00	0.14294674D 00	0-10000000D 01
0.80000000D 00	0.1000000D	01	0.78000460D 00	0.13861502D 00	0.10000000D 01
0.775000000 00	0.100000000	01	0.755004600 00	0.134283300 00	0.100000000 01
0.75000000D 00	0.100000000	01	0.73000460D 00	0.12995158D 00	0.100000000 01
0.725000000 00	0.100000000	01	0.70500460D 00	0.12561986D 00	0-10000000D 01
0.70000000 00	0.100000000	o i	0.68000460D 00	0.121288140 00	0.1000000000 01
0.67500000D 00	0.100000000	01	0.65500460D 00	0.11695642D 00	0.100000000 01
0.650000000 00	0.100000000	01	0.63000460D 00	0.11262471D 00	0.10000000D 01
0.6250000D 00	0.100000000	01	0.60500460D 00	0.10529299D 00	0.10000000D 01
0.600000000 00	0.10000000D	01	0.58000460D 00	0.10396127D 00	0.1000000000
0.57500000D 00	0.1000000000	01	0.555004600 00	0.99629547D-D1	0.100000000 01
0.550000000 00	0.100000000	91	0.53000460D 00	0.952978270-01	0.10000000D 01
0.52500000D 00	0.100000000	01	0.50500460D 00	0.909661080-01	0.10000000D 01
0.50000000D 00	0.100000000	õi	0.48000460D 00	0.86634388D-01	0.100C0C00D 01
0.47500000D 00	0.100000000	01	0.455004600 00	0.823026690-01	0.10000000D 01
0.450000000 00	0.10000000D	01	0.43000460D 00	0.77970950D-01	0.1000000000
0.425000000 00	0.100000000	01	0.40500460D 00	0.73639230D-01	0.100000000 01
0.40000000D 00	0.10000000D	01	0.380004600 00	0.693075110-01	0.999999990 00
0.37500000D 00	0.999999960	00	0.355004600 00	0.649757910-01	0.9999993D 00
0.350000000 00	0.999999630	00	0.33000461D 00	0.606440720-01	0.999999250 00
0.32500000D 00	0.999996970	90	0.305004640 00	0.563123530-01	0.99999395D 00
	0.999980160	00	0.28000487D 00	0.51980633D-01	0.9999903950 00

0.275000000 00	0.99989448D	00	0.255006170 00	0.47648914D-01	0.99978898D 00
0.250000000 00	0.999541050	00	0.230012280 00	0.433171940-01	0.99908232D 00
0.22500000D 00	0.998352190	00	0.20503590D 00	0.38985475D-01	9.99670710D 00
0.2000000D 00	0.99505955D	00	0.180111980 00	0.346537550-01	0.990143510 00
0.175000000 00	0.987462500	00	0.155318680 00	0.303220360-01	0.975082190 00
0-150000000 00	0.972668450	00	0.13079906D 00	0.259903170-01	0.946083910 00
0.125000000 00	0.948072950	00	0.106767720 00	0.216585970-01	0.59884232D 00
0. L0000000D 00	0.912991800	00	0.834841380-01	0.173268780-01	0.833554030 00
0.750000000-01	0.870425920	00	0.611820628-01	0.12995158D-01	0.757641290 00
0.50000000D-01	0.82788386D	٥٥	0.399636620-01	0.86634388D-02	0.68539169D 00
0.250000000-01	0.79589517D	00	0.19699579D-01	0.433171940-02	0.63344913D 00
0.0	0.78395130D	00	0.0	0.0	0.61457963D 00
-0.25000000D-01	0.795895170	00	-0.196995790-01	-0.43317194D-02	0.633449130 00
-0.500000000-01	0.82788386D	00	-0.399636620-01	-0.866343680-02	0.685391690 00
-0.75000000D-01	0.870425920	00	-0.61182062D-01	-0.129951580-01	0.75764129D 00
-0.100000000 00	0.91299180D	00	-0.834841380-01	-0.173268780-01	0.83355403D 00
-0.12500000D 00	0.945072950	00	-0.10676772D 00	-0+21658597D-01	0.898842320 00
-0.150000000 00	0.97266845D	00	-0.13079906D 00		
				-0.259903170-01	0.94608391D 00
-0.17500000D 00	0.987462500	00	-0.15531868D 00	-0.30322036D-01	0.975082190 00
-0.20000000 00	0.995059550	00	-0.18011198D 00	-0.34653755D-01	0.99014351D 00
-0.2250000D 00	0.99505955D 0.99635219D	00	-0.18011198D 00 -0.205035900 00	-0.346537550-01 -0.389854750-01	
-0.2250000D 00					0.99014351D 00 0.99670710D 00 0.99908232D 00
-0.2250000D 00	0.99635219D 0.99954105D	00	-0.205035900 00	-0.389854750-01	0.99014351D 00 0.99670710D 00 0.99908232D 00
-0.22500000D 00 -0.25000000D 00 -0.27500000D 00	0.99635219D 0.99954105D 0.99989448D	00	-0.205035900 00 -0.230012280 00 -0.255006170 00	-0.38985475D-01 -0.43317194D-01 -0.47648914D-01	0.99014351D 00 0.99670710D 00 0.99908232D 00 0.99978898D 00
-0.22500000D 00 -0.25000000D 00 -0.27500000D 00 -0.3000000D 00	0.99635219D 0.99954105D 0.99989448D 0.99998016D	00 00 00	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.280004870 00	-0.38985475D-01 -0.433171940-01 -0.476489140-01 -0.51980633D-01	0.99014351D 00 0.99670710D 00 0.99908232D 00 0.99978898D 00 0.99996032D 00
-0.22500000D 00 -0.25000000D 00 -0.27500000D 00 -0.3000000D 00 -0.3250000D 00	0.99635219D 0.99954105D 0.99989448D 0.99998016D 0.99999697D	00	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.280004870 00 -0.305004640 00	-0.389854750-01 -0.433171940-01 -0.476489140-01 -0.519806330-01 -0.563123530-01	0.99014351D 00 0.99670710D 00 0.99908232D 00 0.99978898D 00 0.99996032D 00 0.999993950 00
-0.22500000D 00 -0.25000000D 00 -0.27500000D 00 -0.3000000D 00 -0.32500000D 00 -0.3500000D 00	0.99635219D 0.99954105D 0.9995448D 0.99998016D 0.99999697D 0.99999963D	00	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.280004870 00 -0.305004640 00 -0.330004610 00	-0.38985475D-01 -0.43317194D-01 -0.47648914D-01 -0.51980633D-01 -0.56312353D-01 -0.60644072D-01	0.99014351D 00 0.99670710D 00 0.99908232D 00 0.99978898D 00 0.99996032D 00 0.99999395D 00 0.99999925D 00
-0.22500000D 00 -0.25000000D 00 -0.27500000D 00 -0.32500000D 00 -0.32500000D 00 -0.37500000D 00	0.99635219D 0.99954105D 0.9995448D 0.99998016D 0.9999967D 0.9999963D 0.9999996D	00 00 00 00 00	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.280004670 00 -0.305004640 00 -0.335004600 00	-0.38985475D-01 -0.43317194D-01 -0.47648914D-01 -0.51980633D-01 -0.56312353D-01 -0.60644072D-01 -0.60975791D-01	0.99014351D 00 0.99670710D 00 0.99908232D 00 0.99978898D 00 0.99999395D 00 0.9999995D 00 0.99999990 00
-0.225000000 00 -0.250000000 00 -0.275000000 00 -0.30000000 00 -0.350000000 00 -0.350000000 00 -0.375000000 00 -0.40000000 00	0.99835219D 0.99954105D 0.99989448D 0.99998016D 0.99999697D 0.99999960 0.99999960	00 00 00 00 00 00	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.280004870 00 -0.305004640 00 -0.335004640 00 -0.335004600 00	-0.38985475D-01 -0.433171940-01 -0.476489140-01 -0.51980633D-01 -0.563123530-01 -0.60644072D-01 -0.64975791D-01 -0.69307511D-01	0.99014351D 00 0.99670710D 00 0.99908232D 00 0.99978898D 00 0.99999395D 00 0.99999995D 00 0.99999990 00
-0.22500000 00 -0.25000000 00 -0.275000000 00 -0.36000000 00 -0.355000000 00 -0.375000000 00 -0.40000000 00 -0.425000000 00	0.99635219D 0.99954105D 0.9998948D 0.99998016D 0.99999697D 0.99999963D 0.99999996D 0.10000000D	00 00 00 00 00 00	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.255006470 00 -0.330500640 00 -0.335500460D 00 -0.335000460D 00 -0.36000460D 00	-0.38985475D-01 -0.4733171940-01 -0.476889140-01 -0.519806330-01 -0.563123530-01 -0.60644072D-01 -0.6064975791D-01 -0.69307511D-01 -0.736392300-01	0.99014351D 00 0.996707100 00 0.99908232D 00 0.9990839D 00 0.9999395D 00 0.9999935D 00 0.9999993D 00 0.99999990 00 0.99999900 01
-0.225000000 00 -0.250000000 00 -0.275000000 00 -0.30000000 00 -0.325000000 00 -0.375000000 00 -0.475000000 00 -0.425000000 00 -0.425000000 00	0.99835219D 0.99954105D 0.99989448D 0.99998016D 0.99999697D 0.99999960 0.99999960	00 00 00 00 00 00	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.280004870 00 -0.305004640 00 -0.335004640 00 -0.335004600 00	-0.38985475D-01 -0.433171940-01 -0.476489140-01 -0.51980633D-01 -0.563123530-01 -0.60644072D-01 -0.64975791D-01 -0.69307511D-01	0.99014351D 00 0.99670710D 00 0.99908232D 00 0.99978898D 00 0.99999395D 00 0.99999995D 00 0.99999990 00
-0.22500000 00 -0.25000000 00 -0.275000000 00 -0.36000000 00 -0.355000000 00 -0.375000000 00 -0.40000000 00 -0.425000000 00	0.99635219D 0.99954105D 0.9998948D 0.99998016D 0.99999697D 0.99999963D 0.99999996D 0.10000000D	00 00 00 00 00 00	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.255006470 00 -0.330500640 00 -0.335500460D 00 -0.335000460D 00 -0.36000460D 00	-0.38985475D-01 -0.4733171940-01 -0.476889140-01 -0.519806330-01 -0.563123530-01 -0.60644072D-01 -0.6064975791D-01 -0.69307511D-01 -0.736392300-01	0.99014351D 00 0.996707100 00 0.99908232D 00 0.9990839D 00 0.9999395D 00 0.9999935D 00 0.9999993D 00 0.99999990 00 0.99999900 01
-0.225000000 00 -0.250000000 00 -0.275000000 00 -0.30000000 00 -0.325000000 00 -0.375000000 00 -0.475000000 00 -0.425000000 00 -0.425000000 00	0.99635219D 0.99954105D 0.9999448D 0.99998016D 0.99998070 0.9999996D 0.10000000D 0.1000000D 0.1000000D	00 00 00 00 00 01 01	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.255004670 00 -0.305004640 00 -0.355004600 00 -0.355004600 00 -0.55004600 00 -0.405004600 00 -0.405004600 00	-0.389854750-01 -0.433171940-01 -0.476489140-01 -0.5519806330-01 -0.563123530-01 -0.606440720-01 -0.649757910-01 -0.693075110-01 -0.736392300-01 -0.779709500-01 -0.823026690-01	0.9014351D 00 0.996707100 00 0.997908232D 00 0.99996032D 00 0.99999395D 00 0.99999925D 00 0.99999991D 00 0.99999990 01 0.10000000D 01 0.10000000D 01
-0.225000000 00 -0.250000000 00 -0.275000000 00 -0.30000000 00 -0.350000000 00 -0.375000000 00 -0.40000000 00 -0.45000000 00 -0.45000000 00 -0.45000000 00	0.99835219D 0.99954105D 0.9995948D 0.99998016D 0.99999697D 0.9999996D 0.1000000D 0.1000000D 0.1000000D	00 00 00 00 01 01 01	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.255004640 00 -0.330004610 00 -0.355004600 00 -0.355004600 00 -0.355004600 00 -0.430004600 00 -0.435004600 00	-0.38985475D-01 -0.43317194D-01 -0.47648914D-01 -0.51980633D-01 -0.564312353D-01 -0.60644072D-01 -0.604975791D-01 -0.69307511D-01 -0.73639230D-01 -0.77970950D-01	0.9014351D 00 0.996707100 00 0.997908232D 00 0.99996032D 00 0.99999395D 00 0.99999925D 00 0.99999991D 00 0.99999990 01 0.10000000D 01 0.10000000D 01
-0.225000000 00 -0.25000000 00 -0.275000000 00 -0.325000000 00 -0.350000000 00 -0.350000000 00 -0.45000000 00 -0.45000000 00 -0.45000000 00 -0.45000000 00 -0.55000000 00	0.99931050 0.999541050 0.9999481050 0.99994070 0.999996970 0.999999630 0.10000000 0.10000000 0.100000000 0.100000000	00 00 00 00 00 01 01 01 01	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.2850004870 00 -0.3350004610 00 -0.355004600 00 -0.355004600 00 -0.350004600 00 -0.430004600 00 -0.455004600 00 -0.455004600 00	-0.389854750-01 -0.43171940-01 -0.476489140-01 -0.519806330-01 -0.561823530-01 -0.606440720-01 -0.609757910-01 -0.693075110-01 -0.736392300-01 -0.779709500-01 -0.823026690-01 -0.866343880-01 -0.909661080-01	0.990143510 00 0.995701700 00 0.995701700 00 0.9950322 00 0.9950320 00 0.99590325 00 0.995903250 00 0.99590990 00 0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01
-0.225000000 00 -0.225000000 00 -0.275000000 00 -0.325000000 00 -0.350000000 00 -0.375000000 00 -0.45000000 00 -0.45000000 00 -0.45000000 00 -0.45000000 00 -0.55000000 00 -0.55000000 00	0.99835219D 0.99954105D 0.9998948D 0.99998016D 0.9999963D 0.99999963D 0.1000000D 0.1000000D 0.1000000D 0.1000000D 0.1000000D	00 00 00 00 00 01 01 01 01 01	-0.205035900 00 -0.230012280 00 -0.255006170 00 -0.255006460 00 -0.355004660 00 -0.355004600 00 -0.355004600 00 -0.455004600 00 -0.455004600 00 -0.455004600 00 -0.455004600 00 -0.455004600 00 -0.555004600 00	-0.389854750-01 -0.473889140-01 -0.476889140-01 -0.563123530-01 -0.563123530-01 -0.606440720-01 -0.693975910-01 -0.736392300-01 -0.779709500-01 -0.23226900-01 -0.866343860-01 -0.995278270-01	0.90143510 00 0.99670100 00 0.999082120 00 0.999082130 00 0.9999900 00 0.99999900 00 0.99999900 00 0.10000000 01 0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01
-0.22500000 00 -0.27500000 00 -0.27500000 00 -0.32500000 00 -0.335000000 00 -0.335000000 00 -0.45000000 00 -0.45000000 00 -0.455000000 00 -0.555000000 00 -0.555000000 00	0.99835210 0.999541050 0.99989480 0.99998070 0.99999630 0.999999630 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000	00 00 00 00 00 00 00 00 00 00 00 00 00	-0.205033900 00 -0.2301220 00 -0.255006170 00 -0.305004640 00 -0.330004640 00 -0.335004660 00 -0.35504600 00 -0.35504600 00 -0.45504600 00 -0.45504600 00 -0.55504600 00 -0.55504600 00	-0.389854750-01 -0.43171940-01 -0.476489140-01 -0.519806330-01 -0.563123530-01 -0.606440720-01 -0.693075110-01 -0.736392300-01 -0.779709500-01 -0.823026690-01 -0.866343880-01 -0.906261080-01 -0.9962978270-01	0.990143510 00 0.996701700 00 0.999082320 00 0.99960320 00 0.999993350 00 0.999999350 00 0.999999930 00 0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01
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Figure B-3. Continued.

CONVERGENCE ATTAINED AFTER 4 ITERATIONS RESULTS FOR X/C STATION 128 X * 0.499954200 00

ETA	U/UDEL		F	Y/C	(U/UDEL]**2
C.1000000000 01	0.100000000	01	0.986592130 00	0.247436040 00	0.1000000000 01
0.975000000 00	0.100000000	01	0.961592130 00	0.241250130 00	2-10000000D OT
0.9500C000D 00 0.925C0000D 00	0.100000000	O t	0.936592130 00	0.235064239 00 0.22887833D 00	0.100000000 01 2.10000000D 01
0.900000000 00	0.100000000	01	C+886592130 00	G.22887833D 00 0.22269243D 00	0.10000000D 01
0.87500000D 00	0.100000000	01	0.861592130 00	0.21650653D 00	0.100000000 01
0.5500000D 00	0.100000000	01	C.83659213D 00	0.21032063D 00	0.1000000000 01
0.825000000 00	C.100000000	01	0.911592130 00	0.204134730 00	2.190000000 01
0.800000000 00	0.100000000	01	0.786592130 00	0.197949830 00	7.10000700D 01
0.77500000D 00	0.100000000	Эl	0.761592130 00	0.191762930 00	7.10000000D 01
0.750000000 00	0.100000000	01	C.73659213D 00	0.185577C3D 00	^. LOOCOOOOD OL
0.72500000D DO	0.100000000	01	C.71159213D 00	0.179391130 00	3.1000000000 01
0.700000000 00	0.100000000	01	0.68659213D 00	0.173205220 00	0.100000000 01
0.6750000000 00	0.100000000	01	0.661592130 00	0.16701932D 00 0.16083342D 00	0.1000000000 01 2.100000000 01
0.625070000 00	0.100000000	21	0.611592130 00	0.15464752D 00	0.100000000 01 0.100000000 01
0.403000000 00	0.100000000	01	0.586592130 00	0.148461620 00	2.1000000000 01
0.57500000D 00	0.100000000	01	0.561592130 00	0.142275720 00	C.1000000000 01
0.550000000 00	0.100000000	10	0.536592130 00	C.13608982D 00	9.10000000D 01
0.525090000 09	0.100000000	01	0.51159213D 00	0.129903920 00	7.1000000000 01
0.500000000	0.100000000	01	0.486592130 00	0.123718020 00	0-100000000 01
0.475000000 00	0.106000000	01	0.461592130 00	0.117532120 00	C.100000000 01
0.450000000 00	0.100000000	01	0.43659213D 00	0.11134622D 00	0.100000000 01
0.42300000D 00	0.10000000D	01	0.41159213D 00 0.38659713D 00	0.105160127 00	0.1000000000 01
0.375000000 00	0.100000000	01	0.386597130 00	0.989744140-01 0.92788513D-01	0.1000000000 01
0.350000000 00	0.999999980	00	0.334592130 00	C.86602612D-01	0.999999960 00
0.32500000D 00	0.999999800	00	C.31159213D 00	0.804167129-01	0.999999600 00
0-3000000D 00	0.999998290	00	0.286592150 00	0.742304110-01	1.99999659D 10
0.275000000 00	0.999988130	00	0.261592290 00	0.680449100-01	0.999976250 00
0.250000000 00	0.999932240	00	0.236593100 00	0.618590090-01	3.99986448D 00
0.225000000 00	0.999681260	00	0.211597220 00	0.556731080-01	0.999362620 00
0.200000000 00	0.998756660	၇၁	0.140014400 00	0.494872070-01	0.997514860 00
0.175000000 00 0.150000000 00	0.9959515JD	00	0.16167475D 90	0.433013060-01	0.99191944D 00
0.15000000D 00	0.98892198D 0.97436009D	00	0.13685184D 00 0.11229164D 00	0.37115405D-01 0.309295040-01	0.9779666AD 00 G.9493775BD 00
0.10000000000000	0.949511110	00	0.882206730-01	0.24743604D-01	0.901571760 00
C.750000000-01	0.914986670	00	0.649985710-01	0.185577030-01	0.83720061D 00
0.5000000D-01	0.877081590	00	0.425010700-01	0.123718020-01	0.769272120 00
0.250000000-01	0.846877810	00	0.209802540-01	0.618590090-02	0.717202020 00
0.0	0.83528683D	00	0.0	0.0	0.69770409D 00
-0.257000000-01	0.846877810	00	-0.209802540-01	-0.618590090-02	0.71720202D 90
-0.50000000D-01	0.A77081590	00	-0.425010700-01	-0.123718C2D-01	0.769272120 00
-0.7500000000-01	0.91498667D	00	-0.64898571D-01 -0.68220673D-01	-0.18557703D-01 -0.247436940-01	0.837200610 00
-0.12500000D 00	0.97436009D	00	-0.11229164D 00	-0.309295040-01	0.949377590 00
-0.150000000 00	0.988921980	00	-0.13685184D 00	-0.171154C5D-01	0.977966680 00
-0.17500000D 00	0.995951530	00	-0.16167475D 00	-0.43301306D-01	0.991919440 00
-0.200000000 00	0.998756660	00	-0.18661446D 00	-0.494872970-01	0.99751486D 00
-0.2250000D 00	0.999681260	00	-0.211597220 00	-0.556731080-01	0.999362629 00
-0.250000000 00	0.999932240	00	-0.236593100 00	-0.618590090-01	0.99986446D 00
-0.27500000D 00	0.999988130	00	-0.26159229D 00	-0.68044910D-01	0.99997625D 00
-0.300000000 00	0.999998290	90	-0.286592150 00	-0.742305110-01	0.999996590 00
-0.325000000 00 -0.350000000 00	0.99999980	00	-0.31159213D 00 -0.33659213D 00	-0.804167120-01	0.999999600 00
~0.3750000000 00	0.100000000	01	-0.33659213D 00 -0.36159213D 00	-0.866026120-01	0.1000000000000000000000000000000000000
-0.40000000 00	0.100000000	o i	-0.38659213D 00	-0.989744140-01	0.1000000000001
-0.42500000D 00	0.100000000	01	-0.411592130 00	-0.105160320 00	2.100000000000000
-0.450000000 00	0.100000000	01	-0.436592130 00	-0.111346220 00	0.1000000000 01
-0.475000000 00	0.100000000	01	-0.46159213D 00	-0.11753212D 00	0.1000000000 01
-0.500000000 00	0.100000000	01	-0.48659213D 00	-0.123718020 00	0.100000000 01
-0.52300000D 00	0.100000000	01	-0.51159213D 00	-0.129903920 00	7.100000000
-0.550C0000D 00	0.10000000D	01	-0.536592130 00	-0.13608982D 00	C.100000000 01
-0.57500000D 00	0.10000000D	01	-0.56159213D 00	-0.14227572D 00	0.100000000 01
-0.623000000 00	0.100000000	01	-0.58659213D 00 -0.61159213D 00	-0.14846162D 00 -0.15464752D 00	0.100000000 01 0.100000000 01
-0.650000000 00	0.10000000D	01	-0.63659213D 00	-0.160833420 00	0.1000000000000000
-0.675000000 00				-0-16701932D 00	9.10000000D OI
	0.100000000	01	-0.66159213D 00		
-C.70000000D 00		01	-0.66159213D 00	-0.173205220 00	2.1000000000 01
-0.72500000D QO	0.100000000 0.100000000 0.100000000	01	-0.68659213D 00 -0.71159213D 00	-0.17320522D 00 -0.17939113D 00	0.100000000 01
-0.72500000D Q0 -0.75000000D 00	0.10000000 0.10000000 0.10000000 0.10000000	01 01	-0.68659213D 00 -0.71159213D 00 -0.73659213D 00	-0.173205220 00 -0.179391130 00 -0.185577030 00	0.100000000 01 0.100000000 01
-0.72500000D 00 -0.75000000D 00 -0.77500000D 00	0.10000000 0.10000000 0.10000000 0.10000000 0.10000000	01 01 01	-0.68659213D 00 -0.71159213D 00 -0.73659213D 00 -0.76159213D 00	-0.173205220 00 -0.179391130 00 -0.185577030 00 -0.191762930 00	0.100000000 01 0.100000000 01 0.100000000 01
-0.725000000 00 -0.750000000 00 -0.775000000 00 -0.800000000 00	0.10000000 0.10000000 0.10000000 0.10000000 0.10000000	01 01 01 01	-0.68659213D 00 -0.71159213D 00 -0.73659213D 00 -0.76159213D 00 -0.76659213D 00	-0.173205220 00 -0.179391130 00 -0.185577030 00 -0.191762930 00 -0.197948830 00	0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01
-0.725000000 00 -0.750000000 00 -0.775000000 00 -0.800000000 00 -0.825000000 00	0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000	01 01 01 01 01	-0.68659213D 00 -0.71159213D 00 -0.73659213D 00 -0.76159213D 00 -0.76659213D 00 -0.76159213D 00	-0.17320522D 00 -0.17939113D 00 -0.18557703D 00 -0.19176293D 00 -0.19794883D 00 -0.20413473D 00	0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01
-0.725000000 00 -0.750000000 00 -0.775000000 00 -0.800000000 00	0.10000000 0.100000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000	01 01 01 01	-0.68659213D 00 -0.71159213D 00 -0.73659213D 00 -0.76159213D 00 -0.78659213D 00 -0.81159213D 00 -0.83659213D 00	-0.173205220 00 -0.179391130 00 -0.185577030 00 -0.191762930 00 -0.191764830 00 -0.204134730 00 -0.210320039 00	0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01
-0.725000000 00 -0.750000000 00 -0.775000000 00 -0.8000000000 00 -0.825000000 00 -0.850000000 00	0.10000000 0.100000000 0.10000000 0.100000000	01 01 01 01 01 01	-0.68659213D 00 -0.71159213D 00 -0.73659213D 00 -0.76159213D 00 -0.78659213D 00 -0.81159213D 00 -0.83659213D 00	-0.173205220 00 -0.179391130 00 -0.185577030 00 -0.191762930 00 -0.191764830 00 -0.204134730 00 -0.210320039 00	0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01
-0.725000000 00 -0.750000000 00 -0.775000000 00 -0.800000000 00 -0.825000000 00 -0.875000000 00 -0.875000000 00	0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000	01 01 01 01 01 01	-0.68659213D 00 -0.71159213D 00 -0.73659213D 00 -0.76159213D 00 -0.76659213D 00 -0.76659213D 00 -0.83659213D 00 -0.83659213D 00	-0.173205220 00 -0.179391130 00 -0.185577030 00 -0.191762930 00 -0.191762930 00 -0.204134730 00 -0.210320030 00 -0.21032030 00 -0.210506530 00 -0.222692430 00	0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01
-0.725000000 00 -0.750000000 00 -0.775000000 00 -0.800000000 00 -0.825000000 00 -0.875000000 00 -0.875000000 00	0.10000000 0.100000000 0.10000000 0.100000000	01 01 01 01 01 01	-0.68659213D 00 -0.71159213D 00 -0.73659213D 00 -0.76659213D 00 -0.76659213D 00 -0.76659213D 00 -0.63659213D 00 -0.666159213D 00 -0.66659213D 00	-0.173205220 00 -0.179391130 00 -0.185577030 00 -0.191762930 00 -0.191762930 00 -0.204134730 00 -0.210320030 00 -0.210506530 00 -0.222692430 00	0.10000000 01 0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01
-0.725000000 0 -0.775000000 00 -0.875000000 00 -0.850000000 00 -0.85000000 00 -0.87500000 00 -0.90500000 00 -0.92500000 00 -0.92500000 00	0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000	01 01 01 01 01 01 01 01 01	-0.68592130 00 -0.71592130 00 -0.736592130 00 -0.761592130 00 -0.76592130 00 -0.69592130 00 -0.69592130 00 -0.69592130 00 -0.69592130 00 -0.691592130 00 -0.91592130 00 -0.91592130 00	-0.173205220 00 -0.17939113D 00 -0.18557703D 00 -0.19176293D 00 -0.19176293D 00 -0.20413473D 00 -0.21032003D 00 -0.21650653D 00 -0.22687633D 00 -0.22687633D 00 -0.23506423D 00 -0.2350643D 00	0.10000000 01 0.10000000 01 0.100000000 01 0.100000000 01 0.100000000 01 0.100000000 01 0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01
-0.725000000 00 -0.75000000 00 -0.77500000 00 -0.800000000 00 -0.85000000 00 -0.85000000 00 -0.97500000 00 -0.97500000 00	0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000	01 01 01 01 01 01 01 01	-0.68659213D 00 -0.71159213D 00 -0.73659213D 00 -0.78659213D 00 -0.78659213D 00 -0.81159213D 00 -0.83659213D 00 -0.8659213D 00 -0.8659213D 00 -0.93659213D 00 -0.93659213D 00	-0.173205220 00 -0.179391130 00 -0.185577030 00 -0.191762930 00 -0.191762930 00 -0.204134730 00 -0.210320030 00 -0.210320030 00 -0.210320030 00 -0.22687430 00 -0.22687430 00 -0.23876330 00	0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01 0.10000000 01

Figure B-3. Continued.

CONVERGENCE ATTAINED AFTER 3 ITERATIONS

RESULTS FOR X/C STATION 157 X = 0.202963410 01

JOUKOWSKI AIRFOIL/A=0/RN=.21/FREE TRANSITION/M=.05/CEDDY=.03/

ETA	U/UDEL		F	∀ /C	(U/UDEL)**2
0.1000000000		01	0.99375446D 00	0.498572250 00	0.10000000D 01
0.97500000D 0		01	0.96875446D 00 0.94375446D 00	0.48610795D 00	0.100000000 01
0.92500000000000000000000000000000000000		01	0.91875446D 00	0.461179330 00	0.1000000000 01
0.9000000D 0		01	0.89375446D 00	0.448715030 00	0.10000000D 01
0.87500000D 0		01	0.86875446D 00	0.436250720 00	0.100000000 01
0.85000000D 0	0 0.10C00000D	01	0.843754460 00	0.42378642D 00	0.1000000000 01
0.8250000D 0		01	0.81875446D 00	0.411322110 00	0.100000000 01
0.8000000000		01	0,79375446D 00	0.398857600 00	0.10000000D 01
0.77500000D 0		01	0.76875446D 00 0.74375446D 00	0.38639350D 00 0.37392919D 00	0.100000000 01
0.725000000 0		01	0.71875446D 00	0.36146488D 00	0.10000000000000
0.70000000D 0		01	0.693754460 00	0.349000580 00	0.10000000D 01
0.67500000D 0		01	0.66875446D 00	0.336536270 00	0.100000000 01
0.6500000000		0 1	0.64375446D 00	0.324071960 00	0.10000000D 01
0.6250000D 0		01	0.61875446D 00	0.31160766D 00 0.29914335D 00	0.10000000D OL
0.600000000 0 0.575000000 0		01	0.59375446D 00 0.56875446D 00	0.28667905D DO	0.10000000D 01
0.55000000D 0		0.1	0.54375446D 00	0.27421474D 00	0.10000000000000
0.525000000 0		01	0.51875446D 00	0.26175043D 00	0.100000000 01
0.50000000 p		01	0.49375446D 00	0.24928613D 00	0.1000000000 01
0.47500000D 0		01	0.46875446D 00	0.236821820 00	0.10000000D 01
0.45000000D 0		01	0.44375446D 00	0.22435751D 00	9.1000000000 01
0.425000000 0		01	0.418754460 00	0.211893210 00	0.1000000000 01
0.40000000D 0		01	0.39375446D 00 0.36875446D 00	0.199428900 00	0.1000000000 01
0.37500000D 0		01	0.368754460 00 0.34375446D 00	0.18696460D 00 0.17450029D 00	0.1000000000 01 0.1000000000 01
0.325000000		00	0.318754460 00	0.162035980 00	0.99999999D 00
0.300000000		00	0.29375446D 00	C.14957168D 00	0.999999840 00
0-27500000D 0	0 0.99999926D	00	0.26875447D 00	0.13710737D 00	0.999998520 00
0.2500000000		00	0.24375453D 00	0.124643060 00	0.99998855D 00
0.225000000		00	0.218754950 00	0.112178760 00	0.999927350 00
0.200000000		00	0.19375730D 00	0.99714451D-01	0.999622320 00
0.175000000 0 0.150000000 0		00	0.16876811D 00 0.14380692D 00	0.87250144D-01 0.74785838D-01	0.998390820 00
0.125000000 0		00	0.118935880 00	0.623215320-01	0.983897870 00
0.100000000		00	0.942613560-01	C-49857225D-01	0.962193060 00
0.75000000D-0	1 0.962900600	00	0.699499890-01	0.373929190-01	0.927177570 00
0.5000000D-0	0.940508080	00	0.46154516D-01	0.249286130-01	0.88455545D 00
0.250000000-0		00	0.229000510-01	0.124643060-01	0.84846430D 00
0.0	0.91336616D	00	0.0	0.0	0.83423774D 00
-0.25000000D-0		00	-0.229000510-01 -0.461545160-01	-0.12464306D-01 -0.24928613D-01	0.84846430D 00 0.88455545D 00
-0.75000000D-0		00	-0.69949989D-01	-0.373929190-01	0.927177570 00
-0.10000000 0		00	-0.94261356D-01	-0.498572250-01	0.962193060 00
-0.12500000D 0	0.991916260	00	-0.11893588D 00	-0.62321532D-01	0.983897870 00
-0.15000000D 0		00	-0.143808920 00	-0.747858390-01	0.99437832D 00
-0.17500000D 0		00	-0.16876811D 00	-0.872501440-01	0.998390820 00
-0.200000000 or		00	-0.19375730D 00	-0.99714451D-01	0.999622320 00
-0.225000000 00 -0.250000000 00		00	-0.21875495D 00 -0.24375453D 00	~0.11217876D 00 -0.12464306D 00	0.999927350 00 0.99998855D 00
-0.275000000 0		00	-0.26875447D 00	-0.124643060 00	0.9999998520 00
-0.30000000 0		00	-0.29375446D 00	-0.14957168D 00	0.99999984D 00
-0.325000000 00		00	-0.31875446D 00	-0.16203598D 00	0.999999990 00
-0.350000000 00	0.10000000D	01	-0.34375446D 00	-0.174500290 00	0.100000000 01
-0.37500000D 00		01	-0.36875446D 00	-0.18696460D 00	0.10000000D CI
-0.400000000 00		01	-0.39375446D 00	-0.19942890D 00	0.10000000D 01
-0.42500000D 00		01	-0.41875446D 00 -0.44375446D 00	-0.21189321D 00 -0.22435751D 00	0.10000000D 01
-0.475000000 00		01	-0.46875446D 00	-0.23682182D 00	0.1000000000 01
-0.5000000D 00		01	-0.49375446D 00	-0.24928613D 00	0.1000000000 01
-0.5250000D 00		01	-0.518754460 00	-0.26175043D 00	0.100000000 01
-0.550000000 00		01	-0.54375446D 00	-0.27421474D 00	0.1000000000 01
-0.57500000D 00		0 t	-0.56875446D 00	-0.28667905D 00	0.10000000D 01
-0.60000000 00		01	-0.59375446D 00	-0.299143350 00	0.10000000D 01
-0.625000000 00 -0.650000000 00		01	-0.61875446D 00 -0.64375446D 00	-0.31160766D 00	0.100000000 01
-0.650000000 00		01	-0.64375446D 00 -0.66875446D 00	-0.324071960 00 -0.336536270 00	0.1000000000 01
-0.70000000D 00		o i	-0.69375446D 00	-0.34900058D 00	0.100000000 01
-0.72500000D 00		01	-0.71875446D 00	-0.3614648BD 00	0.100000000 01
-0.750000000 00		01	-0.74375446D 00	-0.37392919D 00	0.10000000D 01
-0.775000000 00		01	-0.76975446D 00	-0.386393500 00	0.100000000 01
-0.000000000		01	-0.79375446D 00	-0.39885780D 00	0.1000000000 01
-0.825000000 00		01	-0.81875446D 00	-0.41132211D 00	0.10000000D 01
-0.850000000 00		01	-0.843754460 00 -0.868754460 00	-0.42378642D 00 -0.43625072D 00	0.100000000 01 0.100000000 01
-0.900000000 00		01	-0.89375446D 00	-0.44671503D 00	0.1000000000 01
-0.9250000D 00		oi.	-0.91875446D 00	-0.461179330 00	0.1000000000 01
-0.95000000D 00	0.100000000	οi	-0.94375446D 00	-0.47364364D 00	0.1000000000 01
-0.97500000D Q		01	-0.968754460 00	-0.48610795D 00	0.100000000 01
-0.100030000 01	0.10000000D	01	-0.99375446D 00	-0.49857225D 00	0.1000000000 01

Figure B-3. Continued.